


Sheet (1)

Geometric Concepts


[1] The line segment:

It is the set of points between two distinct points and denoted by

\overline{AB} or \overline{BA} 


$AB = 6\text{ cm}$, $C \in \overline{AB}$, $D \notin \overline{AB}$

[2] The ray:

It is a line segment extended from only one of its terminals infinitely and denoted by \overrightarrow{AB} 

$C \in \overrightarrow{AB}$, $D \in \overrightarrow{AB}$, $E \notin \overrightarrow{AB}$, $\overline{AB} \subset \overrightarrow{AB}$, $\overrightarrow{AB} \neq \overrightarrow{BA}$

[3] The straight line:

It is a line segment extended from its two terminals infinitely and denoted by \overleftrightarrow{AB} or \overleftrightarrow{BA} 

$C \in \overleftrightarrow{AB}$, $D \in \overleftrightarrow{AB}$, $E \in \overleftrightarrow{AB}$, $\overline{AB} \subset \overleftrightarrow{AB} \subset \overleftrightarrow{AB}$

[4] The plane:

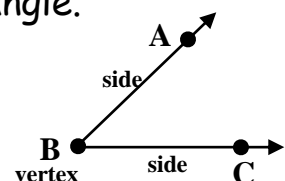
A plane is a flat unbounded surface and it is extended without limit in all directions.

[5] The angle:

It is the union of two rays having the same starting point (vertex of the angle) the two rays are called two sides of the angle.

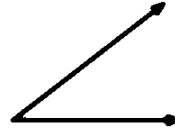
$\angle ABC$, $\angle CBA$ or $\angle B$

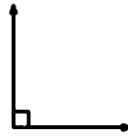
$\overrightarrow{BC} \cup \overrightarrow{BA} = \angle ABC$



Types of angles:

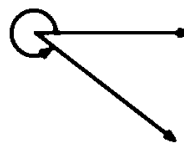
(1) **Zero angle:** Its measure = 0° . 

(2) **Acute angle:** $0^\circ < \text{its measure} < 90^\circ$. 

(3) **Right angle:** Its measure = 90° . 

(4) **Obtuse angle:** $90^\circ < \text{its measure} < 180^\circ$. 

(5) **Straight angle:** Its measure = 180° . 

(6) **Reflex angle:** $180^\circ < \text{its measure} < 360^\circ$. 

[1] Complete the following table:

$m(\angle B)$	50°	105°	179°	$115^\circ 46'$
$m(\text{reflex } \angle B)$	330°	237°	350°	$200^\circ 19' 30''$

[2] Mention the type of the angle whose measure is as follows:

(1) 57° (2) 117°

(3) 90° (4) 200°

(5) 180° (6) $43\frac{1}{2}^\circ$

(7) $179^\circ 62'$ (8) $90\frac{2}{5}^\circ$

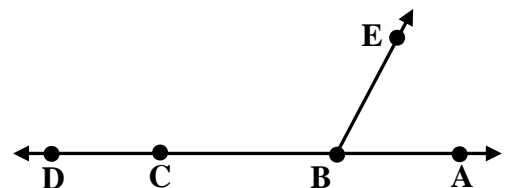
[3] From the opposite figure, complete using (\in), (\notin), (\subset) or ($\not\subset$):

(1) A \overrightarrow{DC} (2) D \overrightarrow{AC}

(3) C \overrightarrow{AB} (4) A $\angle EBC$

(5) \overrightarrow{DC} \overrightarrow{AB} (6) \overrightarrow{BC} \overrightarrow{BA}

(7) \overrightarrow{BA} \overrightarrow{DC} (8) \overrightarrow{AC} \overrightarrow{AD}



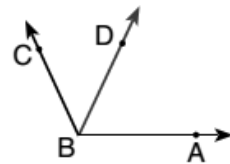
Sheet (2)

Some Relations Between Angles

Adjacent angles

Two angles are said to be adjacent if they have a common vertex, a common side and the other two sides are on opposite sides of the common side.

$\angle ABD$, $\angle DBC$ are adjacent

**Complementary angles**

Two angles are said to be complementary if their sum is 90° .

And the two outer sides are perpendicular

[1] Write the measure of the angle which complements each of the angles whose measures are as follow:

(1) 30°

(2) 60°

(3) 48°

(4) 0°

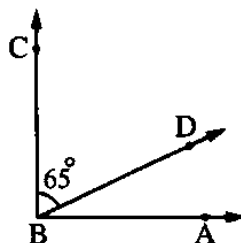
(5) 90°

(6) $22\frac{1}{2}^\circ$

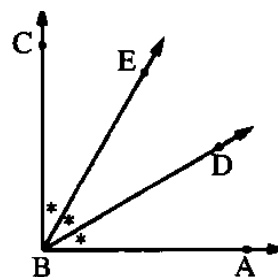
(7) $25^\circ 30'$

(8) $53\frac{1}{4}^\circ$

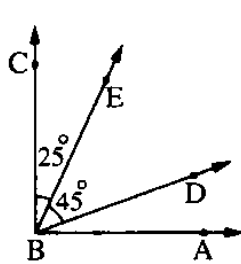
[2] In each of the following figures $\overline{BA} \perp \overline{BC}$, Complete:



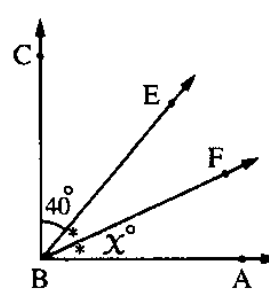
(1) $m(\angle ABD) = \dots\dots\dots^\circ$



(2) $m(\angle DBC) = \dots\dots\dots^\circ$



(3) $m(\angle ABD) = \dots\dots\dots^\circ$

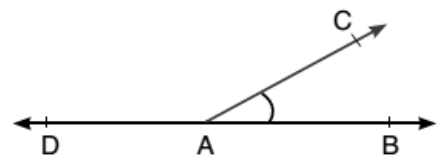


(4) $x = \dots\dots\dots^\circ$

Supplementary angles

Two angles are said to be supplementary if their sum is 180° .

Two adjacent angles formed by a straight line and a ray with a starting point on this straight line are supplementary



$$m(\angle BAC) + m(\angle CAD) = 180^\circ$$

[3] Write the measure of the angle which supplements each of the angles whose measures are as follow:

(1) 20°

(2) 90°

(3) 152°

(4) 0°

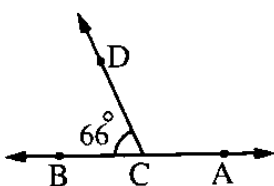
(5) 180°

(6) $92\frac{1}{2}^\circ$

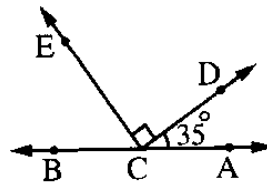
(7) $141^\circ 24'$

(8) 10°

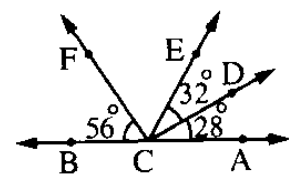
[4] In each of the following figures $C \in \overleftrightarrow{AB}$, Complete:



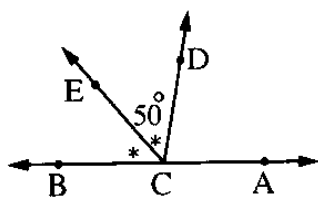
(1) $m(\angle ACD) = \dots\dots\dots^\circ$



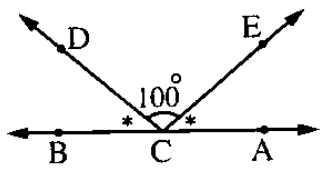
(2) $m(\angle ECB) = \dots\dots\dots^\circ$



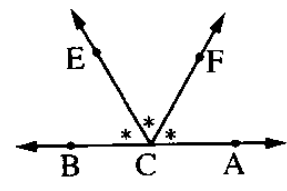
(3) $m(\angle ECF) = \dots\dots\dots^\circ$



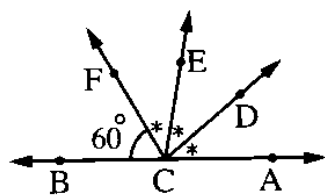
(4) $m(\angle ACD) = \dots\dots\dots^\circ$



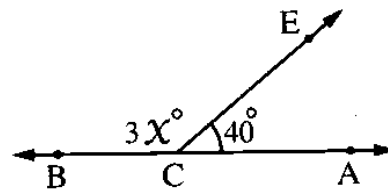
(5) $m(\angle DCB) = \dots\dots\dots^\circ$



(6) $m(\angle FCB) = \dots\dots\dots^\circ$



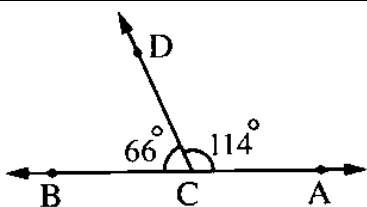
(7) $m(\angle DCB) = \dots\dots\dots^\circ$



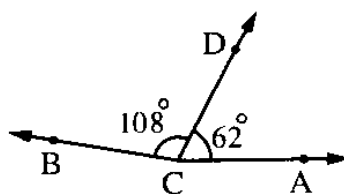
(8) $X = \dots\dots\dots^\circ$

If two adjacent angles are supplementary then their outer sides are on the same straight line.

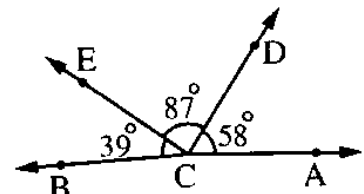
[5] In each of the following figures, state if \overline{CA} and \overline{CB} are on the same straight line or not, and why?



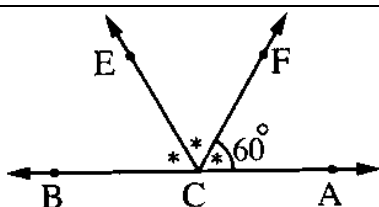
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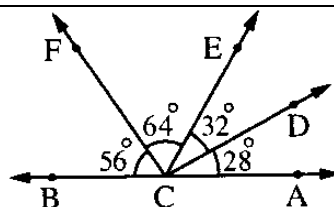
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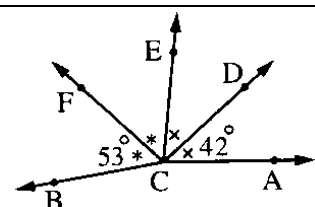
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[6] Complete the following:

(1)	The angle is
(2)	The measure of the straight angle = ° and the measure of zero angle is °
(3)	The measure of the right angle = °
(4)	The acute angle is the angle whose measure is less than and more than
(5)	The two complement angles are the two angles whose sum of their measures is
(6)	The two supplement angles are the two angles whose sum of their measures is
(7)	The two adjacent angles formed by a straight line and a ray with a starting point on this straight line are
(8)	If the two outer sides of two adjacent angles are perpendicular , then these two adjacent angles are
(9)	If the two outer sides of two adjacent angles are on the same straight line , then these two adjacent angles are
(10)	If the two adjacent angles are supplementary , then their outer sides are
(11)	If the sum of measures of two adjacent angles does not equal 180° , then their outer sides are
(12)	The measure of the angle which is equivalent to two right angles = and it is called angle.
(13)	The angle whose measure is 50° complements an angle of measures and supplements the angle whose measure is
(14)	The angle whose measure complements the angle whose measure is 30° and supplements the angle whose measure is
(15)	The angle whose measure complements the angle whose measure is and supplements the angle whose measure is 150°
(16)	The acute angle complements angle and supplements angle.
(17)	Zero angle is complemented by angle and is supplemented by angle.
(18)	The right angle is complemented by angle and is supplemented by angle.

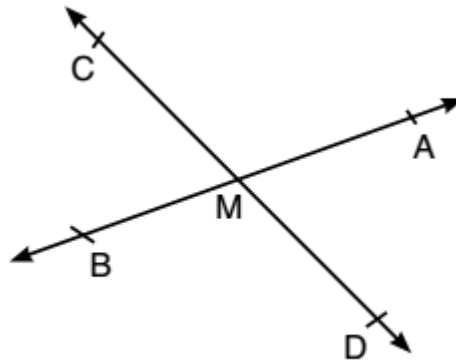
[7] Choose the correct answer:

(1)	The obtuse angle supplements angle. (a) obtuse (b) right (c) acute (d) straight
(2)	Between any two distinct points we can draw straight line passing through them. (a) zero (b) 1 (c) 2 (d) 3
(3)	If : $m(\angle A) + m(\angle B) = 180^\circ$, then $\angle A$ and $\angle B$ are (a) equal in measure. (b) complementary. (c) supplementary. (d) adjacent.
(4)	If : $\overrightarrow{BA} \perp \overrightarrow{BC}$, then $m(\angle ABC) = \dots\dots\dots$ (a) 40° (b) 90° (c) 180° (d) 360°
(5)	If : $\angle A$ supplements $\angle B$, $\angle A$ supplements $\angle C$, then $\angle B$ and $\angle C$ are (a) equal in measure. (b) complementary. (c) supplementary. (d) adjacent.
(6)	If : $m(\angle X) = 15^\circ$, then the two angles whose measures are $2m(\angle X)$, $4m(\angle X)$ are (a) complementary. (b) supplementary. (c) equal in measure. (d) obtuse angles.
(7)	If : $m(\angle A) = 2m(\angle B)$, $\angle A$ supplements $\angle B$, then $m(\angle B) = \dots\dots\dots$ (a) 30° (b) 60° (c) 120° (d) 90°
(8)	$\overline{AB} \dots\dots\dots \overrightarrow{AB}$ (a) \in (b) \notin (c) \subset (d) $\not\subset$
(9)	If : $m(\angle X) = 2m(\angle Y)$ and $\angle Y$ is an obtuse angle , then $\angle X$ is (a) acute. (b) right. (c) obtuse. (d) reflex.

Sheet (3)

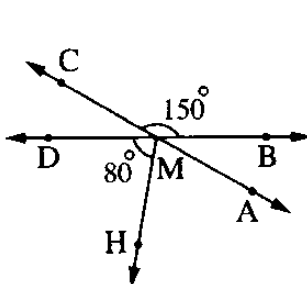
Some Relations Between Angles (follow)

vertically opposite angles

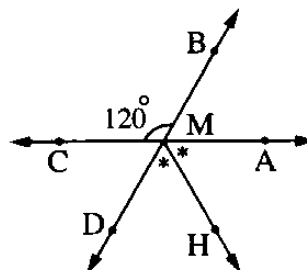


If two straight lines intersect, then the measures of each two vertically opposite angles are equal.

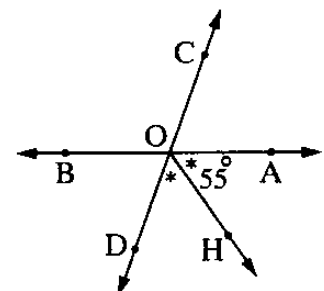
[1] In each figure, find the measure of the required angle:



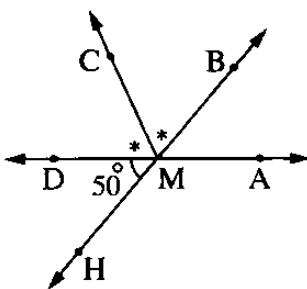
(1) $m(\angle AMH) = \dots\dots\dots^\circ$



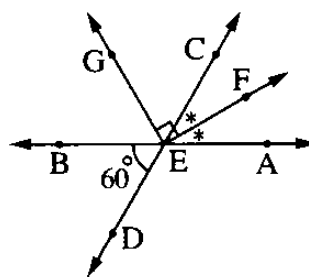
(2) $m(\angle HMD) = \dots\dots\dots^\circ$



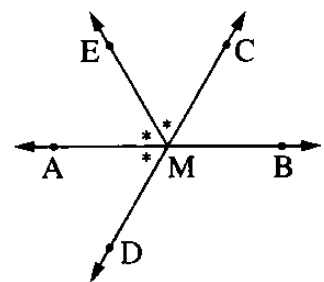
(3) $m(\angle COB) = \dots\dots\dots^\circ$



(4) $m(\angle AMC) = \dots\dots\dots^\circ$



(5) $m(\angle GEB) = \dots\dots\dots^\circ$

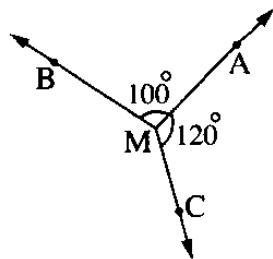


(6) $m(\angle DMB) = \dots\dots\dots^\circ$

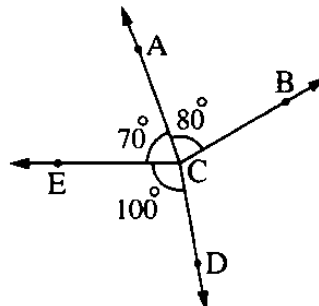
Accumulative angles at a point

The sum of the measures of the accumulative angles at a point is 360°

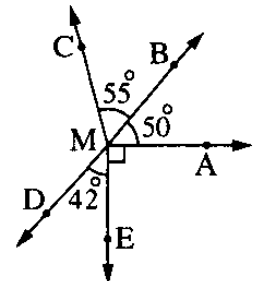
[2] In each figure, find the measure of the required angle:



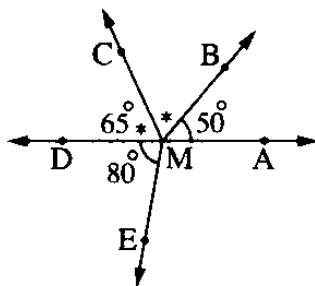
(7) $m(\angle BMC) = \dots\dots\dots^\circ$



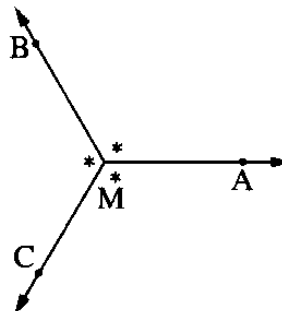
(8) $m(\angle BCD) = \dots\dots\dots^\circ$



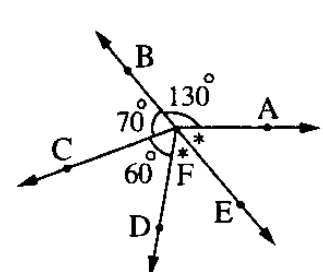
(9) $m(\angle CMD) = \dots\dots\dots^\circ$



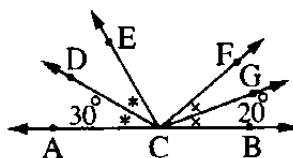
(10) $m(\angle AME) = \dots\dots\dots^\circ$



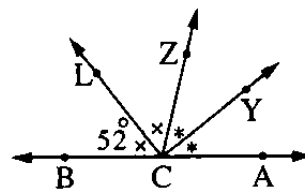
(11) $m(\angle AMC) = \dots\dots\dots^\circ$



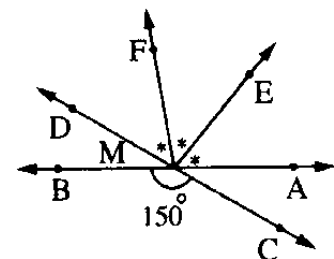
(12) $m(\angle EFD) = \dots\dots\dots^\circ$



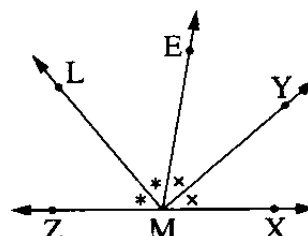
(13) $m(\angle FCE) = \dots\dots\dots^\circ$



(14) $m(\angle YCA) = \dots\dots\dots^\circ$

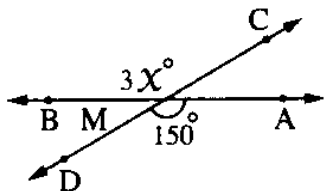
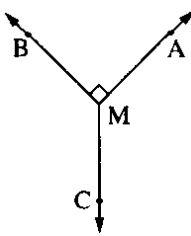
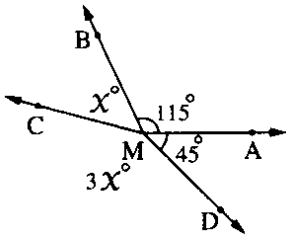


(15) $m(\angle CMF) = \dots\dots\dots^\circ$



(16) $m(\angle YML) = \dots\dots\dots^\circ$

[3] Complete:

(1)	If two straight lines intersect , then each of two vertically opposite angles are
(2)	The sum of the measures of the accumulative angles at the point equals°
(3)	<p>In the opposite figure :</p> <p>$\overleftrightarrow{AB} \cap \overleftrightarrow{CD} = \{M\}$, then $x = \dots\dots\dots^\circ$</p> 
(4)	<p>In the opposite figure :</p> <p>$\overrightarrow{MB} \perp \overrightarrow{MA}$ and \overrightarrow{MC}</p> <p>bisects the reflexed angle AMB</p> <p>, then $m(\angle AMC) = \dots\dots\dots^\circ$</p> 
(5)	<p>In the opposite figure :</p> <p>$x = \dots\dots\dots^\circ$</p> 

The angle bisector:

It is the ray that divides the angle into two halves.

If \overrightarrow{BD} bisects $\angle ABC$

and $m(\angle ABD) = 35^\circ$, then $m(\angle ABC) = \dots\dots\dots^\circ$

[4] Choose the correct answer:

(1)	<p>The sum of the measures of the accumulative angles at the point equals angles.</p> <p>(a) 2 right (b) 3 right (c) 4 right (d) 5 right</p>
(2)	<p>The sum of measures of 4 accumulative angles at the point the sum of measures of 5 accumulative angles at the point.</p> <p>(a) = (b) < (c) > (d) ≠</p>

(3)	<p>The two bisectors of two adjacent supplementary angles</p> <p>(a) are perpendicular. (b) are parallel. (c) are coincident (d) included an acute angle between them.</p>
(4)	<p>In the opposite figure : If ABC is a triangle in which \overrightarrow{CD} bisects $\angle ACB$, $m(\angle A) = 58^\circ$, $m(\angle B) = 60^\circ$, then $m(\angle ADC) = \dots\dots\dots$</p> <p>(a) 62° (b) 89° (c) 91° (d) 130°</p> <div data-bbox="1085 302 1372 582"> </div>
(5)	<p>In the opposite figure : If \overrightarrow{CD} bisects $\angle BCA$, $m(\angle A) = m(\angle ADC) = 70^\circ$, then $m(\angle B) = \dots\dots\dots$</p> <p>(a) 70° (b) 30° (c) 80° (d) 40°</p> <div data-bbox="1069 638 1372 851"> </div>
(6)	<p>In the opposite figure : ABC is triangle , $D \in \overline{AC}$ and \overrightarrow{BD} is a bisector of $\angle B$, what is the measure of $\angle C$?</p> <p>(a) 25° (b) 30° (c) 45° (d) 55°</p> <div data-bbox="1069 896 1372 1086"> </div>
(7)	<p>In the opposite figure : $m(\angle A) = 80^\circ$, \overrightarrow{BE} is the bisector of $\angle B$, \overrightarrow{CD} is the bisector of $\angle C$ what is the measure of the shown angle BFC ?</p> <p>(a) 80° (b) 100° (c) 120° (d) 130°</p> <div data-bbox="1053 1120 1388 1344"> </div>

[4] Answer the following:

(1)	<p>In the opposite figure: If $B \in \overline{AC}$, $m(\angle DBC) = 135^\circ$ and \overrightarrow{BA} bisects $\angle DBE$ Find each of : $m(\angle ABD)$, $m(\angle DBE)$, $m(\angle CBE)$</p> <div data-bbox="1085 1545 1420 1792"> </div>
(2)	<p>In the opposite figure: If $\overline{AB} \cap \overline{CE} = \{M\}$, $\overline{MD} \perp \overline{CE}$, and \overline{MB} bisects $\angle DME$ Find the measures of the following angles : $\angle BME$, $\angle DME$, $\angle AMC$ and $\angle AME$</p> <div data-bbox="1085 1814 1420 2038"> </div>

(3)

In the opposite figure:

$$m(\angle AMB) = 60^\circ, m(\angle AME) = 120^\circ,$$

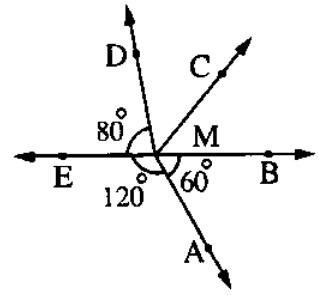
$$m(\angle EMD) = 80^\circ$$

and \overrightarrow{MC} bisects $\angle BMD$

Find :

(1) $m(\angle CMD)$

(2) $m(\angle AMC)$



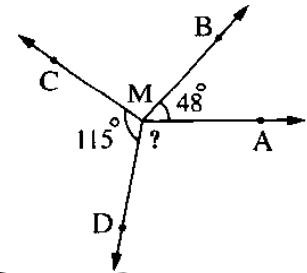
(4)

In the opposite figure:

$$m(\angle BMC) = 2 m(\angle AMB),$$

$$m(\angle AMB) = 48^\circ$$

$$\text{and } m(\angle DMC) = 115^\circ$$

Find : $m(\angle AMD)$ 

لا تنس الاشتراك في
قنواتنا على
تطبيق التليجرام

تابع جديدنا على
فيسبوك
تويتر
واتس اب
تليجرام

Sheet (4) Congruence

- (1) Two line segments are congruent if they are equal in length.
if $AB = XY$ then $\overline{AB} \equiv \overline{XY}$.
- (2) Two angles are congruent if they are equal in measure.
if $m(\angle A) = m(\angle B)$ then $\angle A \equiv \angle B$.
- (3) Two polygons are congruent if each side and each angle in one of them are congruent to their corresponding elements in the other.
- (4) Two squares are congruent if the side length of one of them is congruent to the side length of the other.
- (5) Two rectangles are congruent if the dimensions of one of them are congruent to the dimensions of the other.

[1] Complete the following:

(1)	The two line segments are congruent if
(2)	The two angles are congruent if
(3)	The two polygons are congruent if there is a correspondence between their vertices such that each and each in the first polygon is congruent to its corresponding element in
(4)	The axis of symmetry of a polygon divides it into two polygons.
(5)	If $\overline{AB} \equiv \overline{CD}$, then $AB = \dots\dots\dots$
(6)	If $\overline{AB} \equiv \overline{XY}$, then $AB - XY = \dots\dots\dots$
(7)	If $\angle A \equiv \angle B$ and $m(\angle A) = 50^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
(8)	If $\angle A$ supplements $\angle B$ and $\angle A \equiv \angle B$, then $m(\angle B) = \dots\dots\dots^\circ$
(9)	If $\angle A$ complements $\angle B$ and $\angle A \equiv \angle B$, then $m(\angle A) = \dots\dots\dots^\circ$
(10)	If C is the midpoint of \overline{AB} , then $\overline{AC} \dots\dots\dots \overline{BC}$

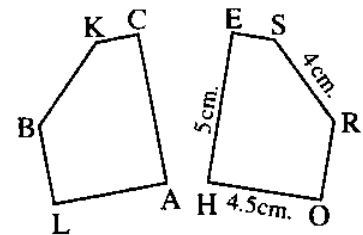
(11)	If the polygon $ABCD \cong$ the polygon $XYZL$, then $\overline{DA} \cong \dots\dots\dots$, $m(\angle BCD) = m(\angle \dots\dots\dots)$
(12)	The two squares are congruent if $\dots\dots\dots$ are equal in length , while the two rectangles are congruent if $\dots\dots\dots$ are equal.

[2] Answer the following:

- (1) In the opposite figure:
The two pentagons shown are congruent

Complete :

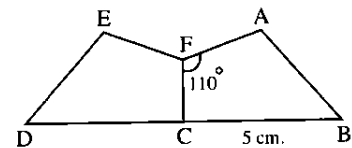
- (1) B corresponds to $\dots\dots\dots$
 (2) The polygon BLACK is congruent to the polygon $\dots\dots\dots$
 (3) $KB = \dots\dots\dots$ cm. (4) $m(\angle E) = m(\angle \dots\dots\dots)$
 (5) $CA = \dots\dots\dots$ cm. (6) $m(\angle A) = m(\angle \dots\dots\dots)$



- (2) In the opposite figure:
If $C \in \overline{BD}$, $m(\angle AFC) = 110^\circ$, $BC = 5$ cm.
and the polygon $ABCF \cong$ the polygon $EDCF$

Complete the following :

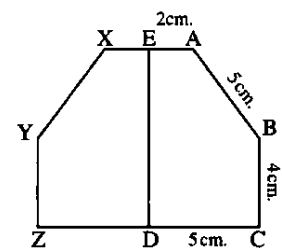
- (1) $AB = \dots\dots\dots$ (2) $AF = \dots\dots\dots$ (3) $CD = \dots\dots\dots$
 (4) \overline{CF} is $\dots\dots\dots$ side. (5) $m(\angle E) = m(\angle \dots\dots\dots)$ (6) $m(\angle B) = m(\angle \dots\dots\dots)$
 (7) $m(\angle FCD) = m(\angle \dots\dots\dots)$ (8) $m(\angle EFC) = \dots\dots\dots^\circ$ (9) $BD = \dots\dots\dots$ cm.
 (10) $m(\angle FCD) = \dots\dots\dots^\circ$ (11) $m(\angle AFE) = \dots\dots\dots^\circ$
 (12) The axis of symmetry of the polygon $ABDEF$ is $\dots\dots\dots$



- (3) In the opposite figure:
If : $D \in \overline{CZ}$ and the figure $ABCDE \cong$ the figure $XYZDE$,
 $AE = 2$ cm. , $BC = 4$ cm. and $AB = CD = 5$ cm.

Find :

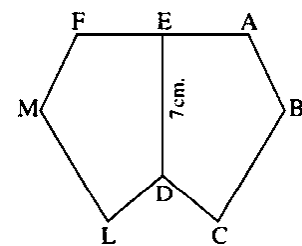
The perimeter of the figure $ABCZYX = \dots\dots\dots$ cm.



- (4) In the opposite figure:
If : $E \in \overline{AF}$, the perimeter of the figure $ABCDE = 27$ cm. ,
 $DE = 7$ cm.

and the polygon $ABCDE \cong$ the polygon $FMLDE$

Find : The perimeter of the figure $ABCDLMF = \dots\dots\dots$ cm.



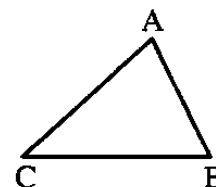
Sheet (5)

Congruent triangles

We know that any triangle has three sides and three angles which are known as the six elements of the triangle.

For example :

$\triangle ABC$ has three sides which are : \overline{AB} , \overline{BC} and \overline{AC} and
it has three angles which are : $\angle A$, $\angle B$ and $\angle C$



Therefore :

The two triangles are congruent if each element of the 6 elements of one of them is congruent to the corresponding element in the other triangle and vice versa.

- To test whether two triangles are congruent or not, you don't need to test all the three sides and the three angles.

The cases of congruence of two triangles

In the following, we will show the cases of congruence of two triangles. We will find that it is not necessary to prove congruence of the six elements of one of them to the corresponding elements of the other. But it is enough to prove congruence of three elements of the first to the corresponding elements of the other, one of them at least is a side, then the remained three elements in one of them are congruent to their corresponding elements in the other.

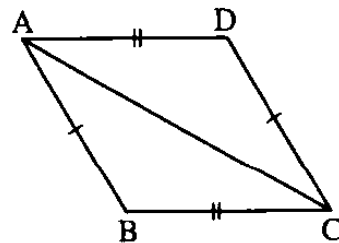
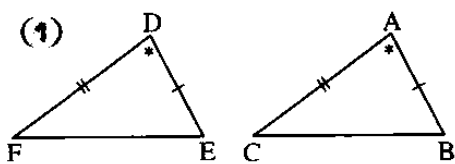
Cases of congruence of two triangles

Case (1)	Case (2)	Case (3)	Case (4)
Two sides and the included angle	Two angles and one side	Three sides	Hypotenuse and one side in the right-angled triangle
S. A. S.	A. S. A.	S. S. S.	R. H. S.
Two triangles are congruent if <u>two sides and the included angle</u> of one triangle are congruent to the corresponding parts of the other triangle	Two triangles are congruent if <u>two angles and the side drawn between their vertices</u> of one triangle are congruent to the corresponding parts of the other triangle	Two triangles are congruent if <u>each side</u> of one triangle is congruent to the corresponding side of the other triangle	Two <u>right-angled</u> triangles are congruent if <u>the hypotenuse and a side</u> of one triangle are congruent to the corresponding parts of the other triangle

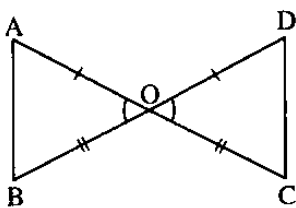
Remark

If each angle of one triangle is congruent to the corresponding angle of the other triangle, it is not necessary for the two triangles to be congruent.

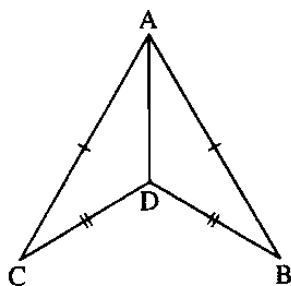
- [1] In each of the following figures, show if the two triangles are congruent or not. If they are congruent, name the case of congruence. If they aren't congruent, give reason. (given that the similar signs denoted the congruency of the elements marked by these signs).



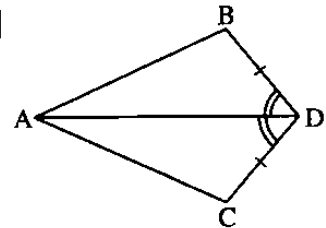
(3)



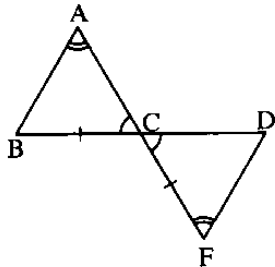
(4)



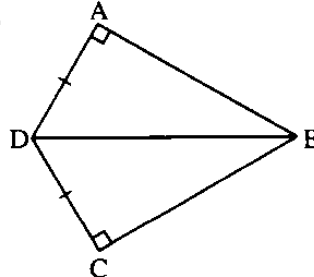
(5)



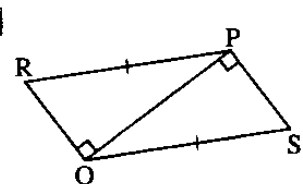
(6)



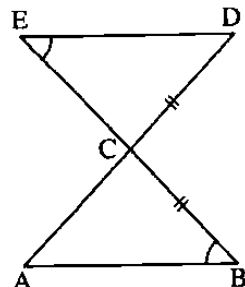
(7)



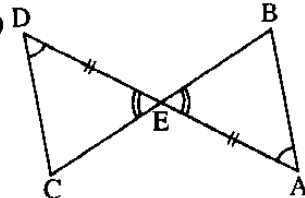
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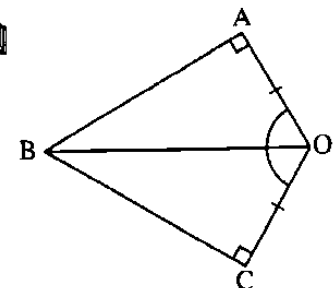
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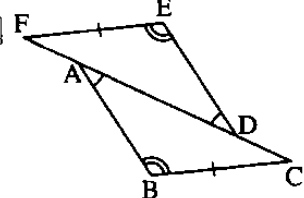
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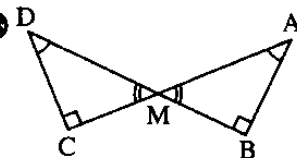
(11)



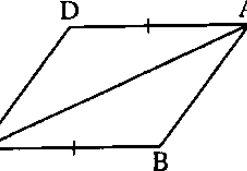
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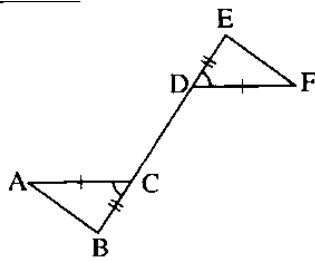
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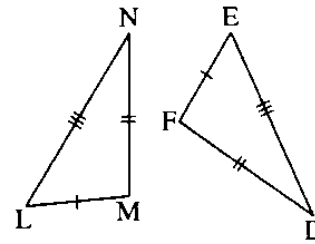
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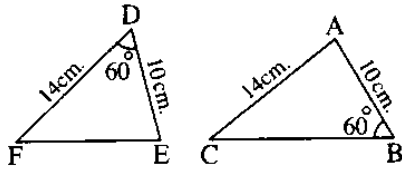
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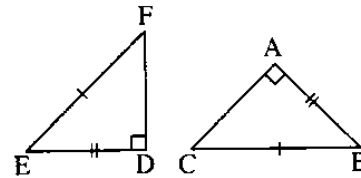
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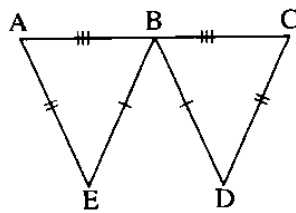
(17)



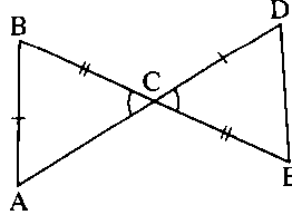
(18)



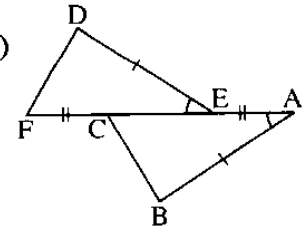
(19)



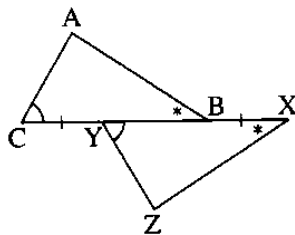
(20)



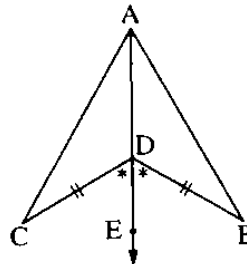
(21)



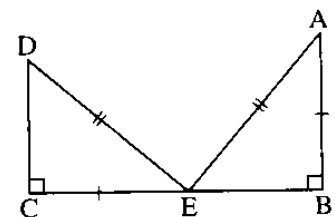
(22)



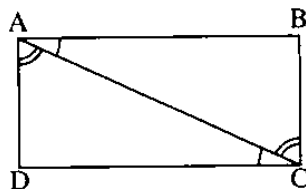
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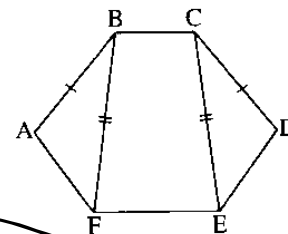
(24)



(25)

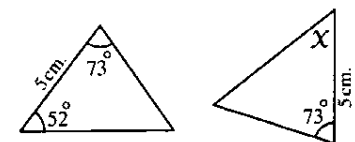


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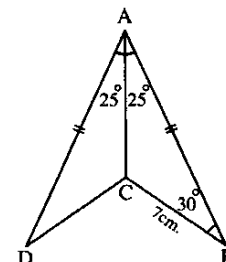


[2] Answer the following:

- (1) In the opposite figure:
These triangles are congruent
, then $X = \dots\dots\dots^\circ$

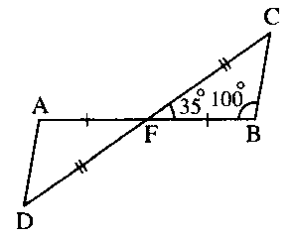


- (2) In the opposite figure:
If : $AB = AD$, $BC = 7$ cm. , $m(\angle BAC) = m(\angle DAC) = 25^\circ$
and $m(\angle B) = 30^\circ$
Complete the following :
- (1) $\triangle ACB \cong \triangle \dots\dots\dots$ (2) $m(\angle D) = \dots\dots\dots^\circ$
(3) $CD = \dots\dots\dots$ cm. (4) $m(\angle ACD) = \dots\dots\dots^\circ$



(3) In the opposite figure:

If : $\overline{CD} \cap \overline{BA} = \{F\}$, $FA = FB$, $CF = FD$,
 $m(\angle CFB) = 35^\circ$ and $m(\angle B) = 100^\circ$,
 then $m(\angle D) = \dots\dots\dots^\circ$

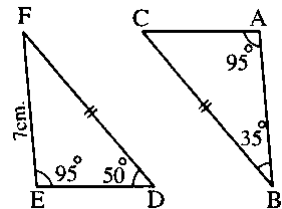


(4) In the opposite figure:

If : $BC = FD$, $m(\angle A) = m(\angle E) = 95^\circ$,
 $m(\angle B) = 35^\circ$, $m(\angle D) = 50^\circ$ and $FE = 7$ cm.

Complete the following :

- (1) $m(\angle C) = \dots\dots\dots^\circ$ (2) $m(\angle F) = \dots\dots\dots^\circ$ (3) $\triangle ABC \equiv \dots\dots\dots$
 (4) $\overline{AC} \equiv \dots\dots\dots$ (5) $AB = \dots\dots\dots$ cm.

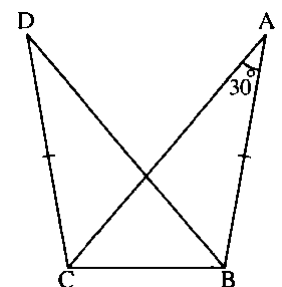


(5) In the opposite figure:

If : $AB = DC$, $AC = DB$ and $m(\angle A) = 30^\circ$

Complete the following :

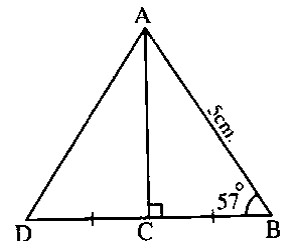
- (1) $\triangle ABC \equiv \triangle \dots\dots\dots$
 (2) $m(\angle D) = \dots\dots\dots^\circ$
 (3) $m(\angle DBC) = m(\angle \dots\dots\dots)$



(6) In the opposite figure:

C is the midpoint of \overline{BD} , $\overline{AC} \perp \overline{BD}$,
 $AB = 5$ cm. and $m(\angle B) = 57^\circ$

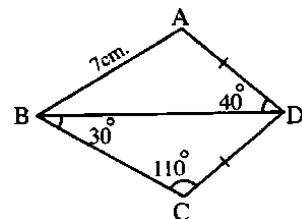
Find : (1) The length of \overline{AD}
 (2) $m(\angle DAC)$



(7) In the opposite figure:

$AD = DC$, $m(\angle ADB) = 40^\circ$, $m(\angle DBC) = 30^\circ$,
 $m(\angle BCD) = 110^\circ$ and $AB = 7$ cm.

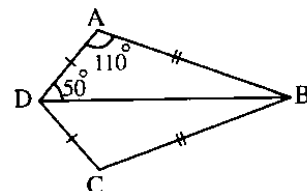
Find : (1) The length of \overline{BC} (2) $m(\angle BAD)$



(8) In the opposite figure:

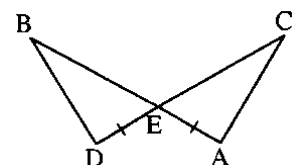
$BA = BC$, $DA = DC$,
 $m(\angle ADB) = 50^\circ$ and
 $m(\angle BAD) = 110^\circ$

Find : $m(\angle ABC)$



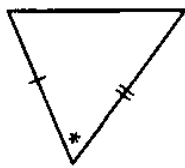
(9) In the opposite figure:

$\overline{AB} \cap \overline{CD} = \{E\}$, $AE = ED$ and $\angle A \equiv \angle D$
 Is $\triangle ACE \equiv \triangle DBE$? Why ?
 Prove that : $CE = EB$

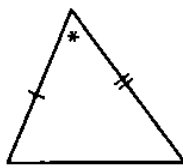


[3] Choose the correct answer:

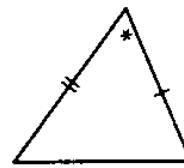
(1) The following triangles are congruent except



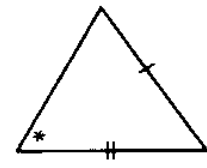
(a)



(b)

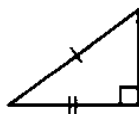


(c)

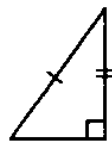


(d)

(2) The following triangles are congruent except



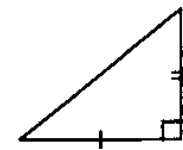
(a)



(b)

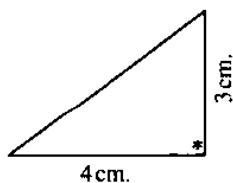


(c)

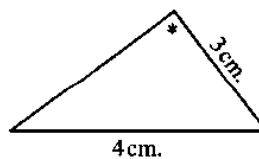


(d)

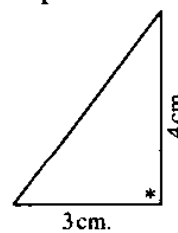
(3) The following triangles are congruent except



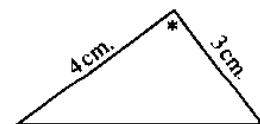
(a)



(b)

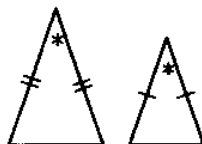


(c)

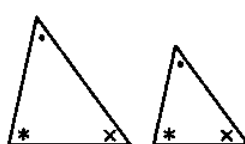


(d)

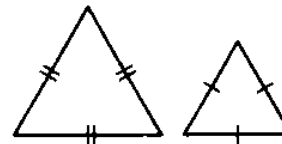
(4) The pair of congruent triangles of the following triangles is



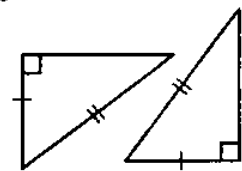
(a)



(b)



(c)



(d)

(5) In the opposite figure :

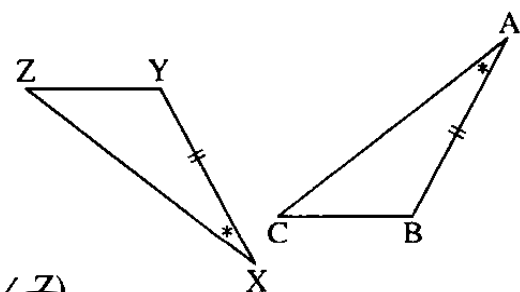
The necessary and enough condition which makes the two triangles ABC and XYZ be congruent is

(a) $BC = YZ$

(b) $AC = XZ$

(c) $m(\angle C) = m(\angle Z)$

(d) $m(\angle B) = m(\angle Z)$



[4] Complete the following:

(1) If : $\triangle ABC \equiv \triangle XYZ$, $m(\angle A) = 50^\circ$ and $m(\angle B) = 60^\circ$, then : $m(\angle Z) = \dots\dots\dots^\circ$

(2) If : $\triangle ABC \equiv \triangle LMN$, $m(\angle L) = 40^\circ$ and $m(\angle B) = 90^\circ$, then : $m(\angle C) = \dots\dots\dots^\circ$

(3) If : $\triangle ABC \equiv \triangle XYZ$ and $m(\angle A) + m(\angle B) = 120^\circ$, then : $m(\angle Z) = \dots\dots\dots^\circ$

(4) If : $\triangle ABC \equiv \triangle DEF$ and $m(\angle C) = 90^\circ$, then : $m(\angle D) + m(\angle E) = \dots\dots\dots^\circ$

(5) If : $\triangle ABC \equiv \triangle XYZ$, the perimeter of $\triangle ABC = 12$ cm. , $XY = 4$ cm. and $YZ = 5$ cm. , then : $AC = \dots\dots\dots$


(6) Any two triangles are congruent if each $\dots\dots\dots$ is congruent to its corresponding side in the other triangle.

(7) Any two triangles are congruent if two angles and $\dots\dots\dots$ in one of the triangles are congruent to their corresponding elements in the other.

(8) The diagonal of the rectangle divides its surface into two $\dots\dots\dots$ triangles.

(9) If $\triangle ABC \equiv \triangle XYZ$, then $AB = \dots\dots\dots$ and $m(\angle Z) = m(\angle \dots\dots\dots)$

(10) If : $AB = LM$, $BC = MN$ and $m(\angle B) = m(\angle M)$, then the two triangles $\dots\dots\dots$ and $\dots\dots\dots$ will be congruent.



Sheet (6)

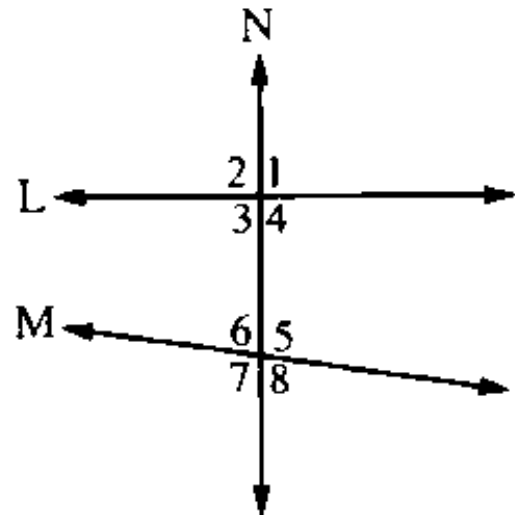
parallelism

Angles Formed from two straight lines and a transversal:

If a straight line N cuts two straight lines L and M as shown in the opposite figure, then we get eight angles.

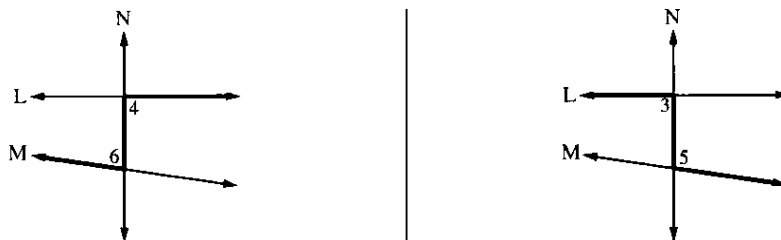
We can classify these angles into pairs of angles:

- Alternate angles.
- Corresponding angles.
- Interior angles on the same side of the transversal.

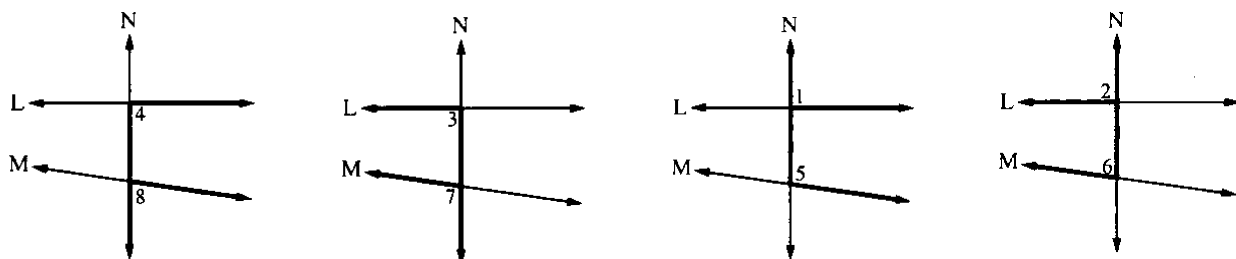


As follows

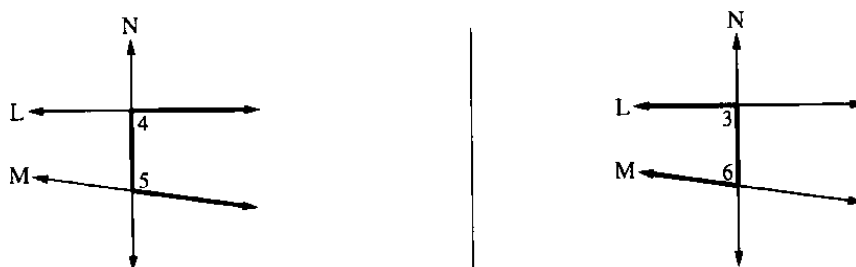
(1) Pairs of alternate angles:



(2) Pairs of corresponding angles:



(3) Pairs of interior angles on the same side of the transversal

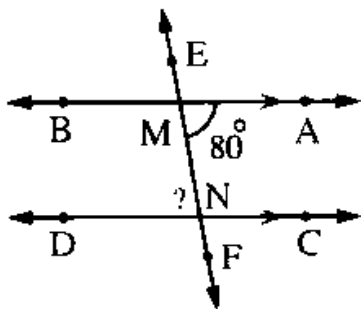


Relation between pairs of angles formed from two parallel straight lines and a transversal to them

If a straight line intersects two parallel lines, then:

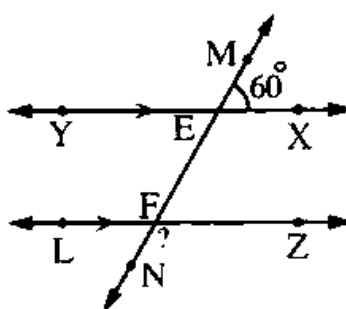
- (1) Each two alternate angles are equal in measure.
- (2) Each two corresponding angles are equal in measure.
- (3) Each two interior angles in the same side of the transversal are supplementary.

In each of the following figures, find the measure of the angle which is marked by (?) giving reason:



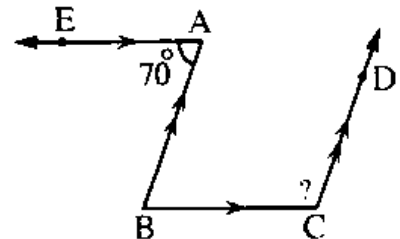
(1)

.....



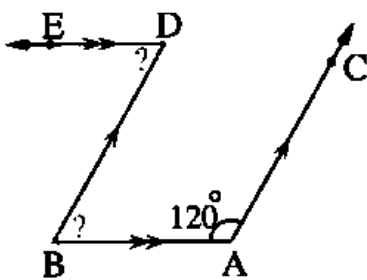
(2)

.....



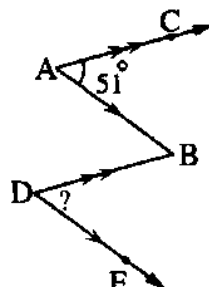
(3)

.....



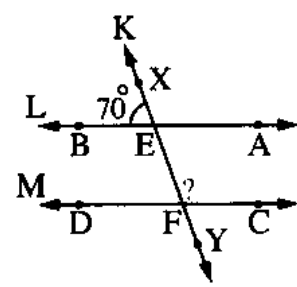
(4)

.....



(5)

.....



(6)

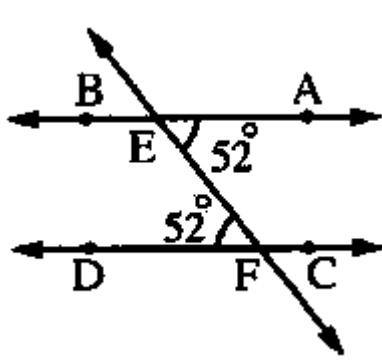
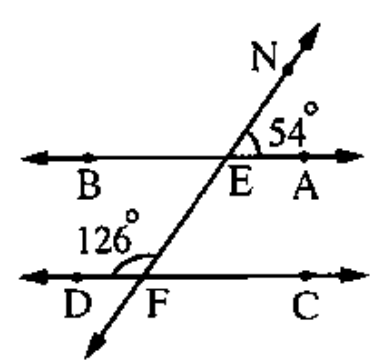
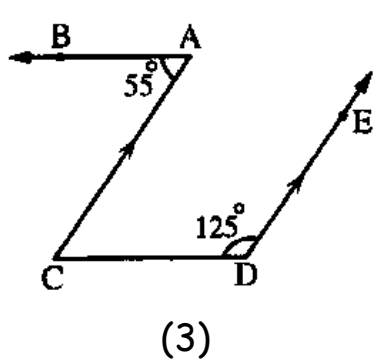
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The condition of parallelism of two straight lines

The two straight lines are parallel if a third straight line intersects them (as a transversal) and one of the following cases satisfied:

- (1) Two alternate angles have the same measure.
- (2) Two corresponding angles have the same measure.
- (3) Two interior angles in the same side of the transversal are supplementary.

In each of the following figures, why is $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$?

 <p>(1)</p> <p>.....</p> <p>.....</p> <p>.....</p>	 <p>(2)</p> <p>.....</p> <p>.....</p> <p>.....</p>	 <p>(3)</p> <p>.....</p> <p>.....</p> <p>.....</p>
--	--	--

Geometric facts

- (1) The perpendicular to one of two parallel straight lines is perpendicular to the other.
- (2) If two straight lines are perpendicular to a third one, then the two straight lines are parallel.
- (3) If two straight lines are parallel to a third one, then the two straight lines are parallel.
- (4) If parallel straight lines divide a straight line into segments of equal lengths, then they divide any other line into segments of equal lengths.

If $L_1 \parallel L_2 \parallel L_3 \parallel L_4$,

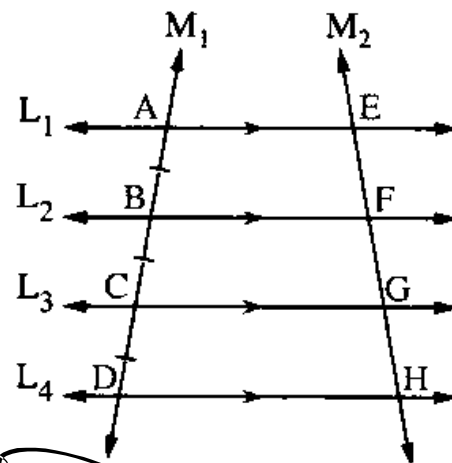
and M_1 and M_2 are two transversal

in which:

$$AB = BC = CD,$$

then:

$$EF = FG = GH$$



Complete using the given shown in the following figures:

<p>DY = cm</p>	<p>AC = cm</p>	<p>AC = cm</p>
----------------------	----------------------	----------------------

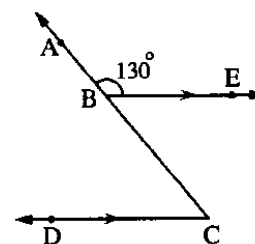
[1] Choose the correct answer:

(1) In the opposite figure:

$B \in \overline{AC}$, $\overrightarrow{BE} \parallel \overrightarrow{CD}$ and $m(\angle ABE) = 130^\circ$

Then $m(\angle C) = \dots\dots\dots$

- (a) 130° (b) 40°
 (c) 50° (d) 90°

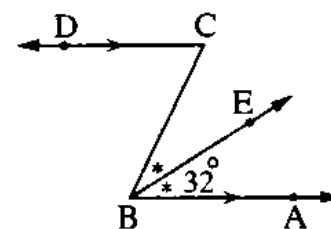


(2) In the opposite figure:

\overrightarrow{BE} bisects $\angle ABC$, $\overrightarrow{BA} \parallel \overrightarrow{CD}$ and

$m(\angle ABE) = 32^\circ$, then $m(\angle C) = \dots\dots\dots$

- (a) 32° (b) 64°
 (c) 60° (d) 80°

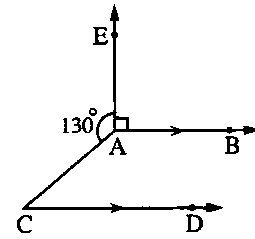


(3) In the opposite figure:

$$\overrightarrow{AB} \parallel \overrightarrow{CD}, m(\angle EAC) = 130^\circ$$

and $m(\angle EAB) = 90^\circ$, then $m(\angle C) = \dots\dots\dots$

- (a) 90° (b) 130°
(c) 140° (d) 40°

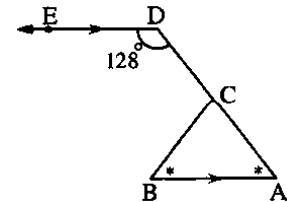


(4) In the opposite figure:

$$\overrightarrow{AB} \parallel \overrightarrow{DE}, m(\angle D) = 128^\circ,$$

$m(\angle A) = m(\angle B)$ and $C \in \overline{AD}$, then $m(\angle B) = \dots\dots\dots$

- (a) 64° (b) 128°
(c) 52° (d) 26°

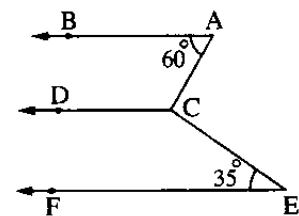


(5) In the opposite figure:

$$\overrightarrow{AB} \parallel \overrightarrow{CD}, \overrightarrow{AB} \parallel \overrightarrow{EF}, m(\angle A) = 60^\circ \text{ and}$$

$m(\angle E) = 35^\circ$, then $m(\angle ACE) = \dots\dots\dots$

- (a) 60° (b) 35°
(c) 95° (d) 85°

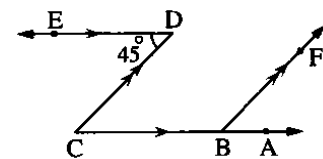


(6) In the opposite figure:

$$m(\angle D) = 45^\circ, \overrightarrow{DE} \parallel \overrightarrow{CA} \text{ and}$$

$\overrightarrow{CD} \parallel \overrightarrow{BF}$, then $m(\angle ABF) = \dots\dots\dots$

- (a) 45° (b) 90°
(c) 135° (d) 40°



(7) In the opposite figure:

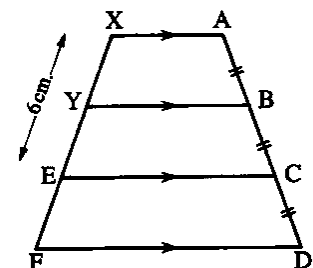
$$\overrightarrow{AX} \parallel \overrightarrow{BY} \parallel \overrightarrow{CE} \parallel \overrightarrow{DF},$$

$$AB = BC = CD$$

and $XE = 6 \text{ cm}$.

, then the length of $\overline{YF} = \dots\dots\dots$

- (a) 3 cm. (b) 6 cm.
(c) 12 cm. (d) 9 cm.



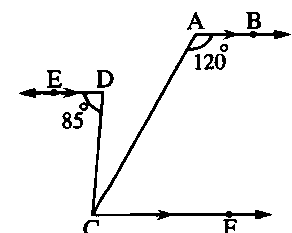
(8) In the opposite figure:

$$\overrightarrow{AB} \parallel \overrightarrow{CF} \parallel \overrightarrow{DE},$$

$m(\angle A) = 120^\circ$ and $m(\angle D) = 85^\circ$,

then $m(\angle ACD) = \dots\dots\dots$

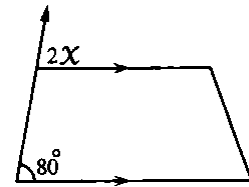
- (a) 60° (b) 85°
(c) 25° (d) 120°



(9) In the opposite figure:

What is the value of X ?

- (a) 40° (b) 60°
(c) 80° (d) 100°

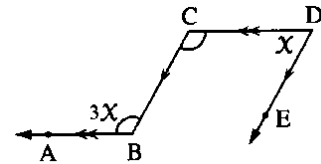


(10) In the opposite figure:

$\overline{CD} \parallel \overline{BA}$, $\overline{DE} \parallel \overline{CB}$

, then : $X = \dots\dots\dots$

- (a) 60° (b) 45°
(c) 120° (d) 90°



[2] Complete:

- (1) The straight line which is perpendicular to one of two parallel straight lines is to the other straight line in the plane.
- (2) If two straight lines are parallel to a third straight line , then they are
- (3) If a straight line cuts two parallel straight lines , then each two alternate angles are
- (4) If a straight line cuts two parallel straight lines , then each two corresponding angles are
- (5) If a straight line cuts two parallel straight lines , then each two interior angles in the same side of the transversal are
- (6) If a straight line cuts two straight lines and there are two corresponding angles having the same measure , then the two straight lines are
- (7) If a straight line cuts two straight lines and there are two alternate angles having the same measure , then the two straight lines are
- (8) If a straight line cuts two straight lines and there are two interior angles in the same side of the transversal are supplementary , then the two straight lines are
- (9) If a straight line cuts several parallel lines and the intercepted parts of this transversal between these parallel straight lines are equal in length , then the intercepted parts for any transversal are

[3] Answer the following:

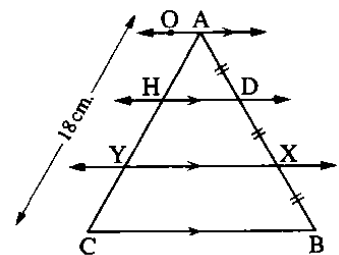
(1) In the opposite figure:

$$\overrightarrow{AO} \parallel \overrightarrow{HD} \parallel \overrightarrow{YX} \parallel \overrightarrow{CB}$$

$$, AD = DX = XB$$

$$\text{and } AC = 18 \text{ cm.}$$

Find the length of \overline{AY}

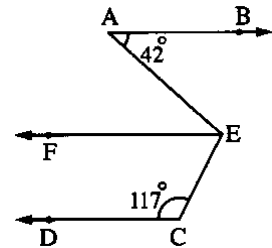


(2) In the opposite figure:

$$\overrightarrow{AB} \parallel \overrightarrow{CD}, \overrightarrow{EF} \parallel \overrightarrow{CD}$$

$$, m(\angle A) = 42^\circ \text{ and } m(\angle C) = 117^\circ$$

Determine : $m(\angle AEC)$

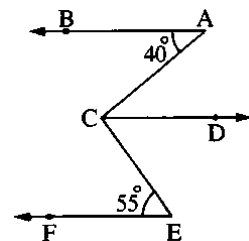


(3) In the opposite figure:

$$m(\angle A) = 40^\circ, m(\angle E) = 55^\circ$$

$$\overrightarrow{AB} \parallel \overrightarrow{EF} \text{ and } \overrightarrow{AB} \parallel \overrightarrow{CD}$$

Find : $m(\angle ACE)$

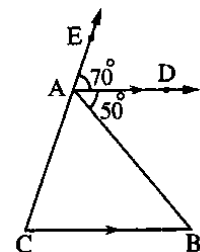


(4) In the opposite figure:

$$\overrightarrow{AD} \parallel \overrightarrow{BC}, E \in \overrightarrow{CA},$$

$$m(\angle DAE) = 70^\circ \text{ and } m(\angle DAB) = 50^\circ$$

Find the measures of the triangle ABC



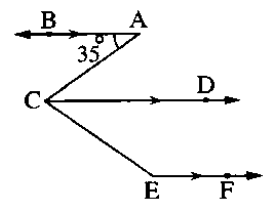
(5) In the opposite figure:

$$\overrightarrow{AB} \parallel \overrightarrow{CD} \parallel \overrightarrow{EF}, m(\angle A) = 35^\circ \text{ and}$$

$$\overrightarrow{CD} \text{ bisects } \angle ACE$$

Find : (1) $m(\angle DCE)$

(2) $m(\angle CEF)$

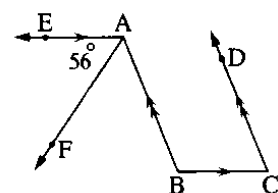


(6) In the opposite figure:

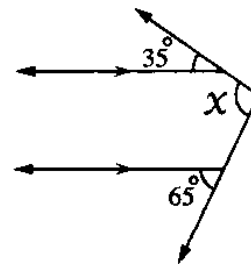
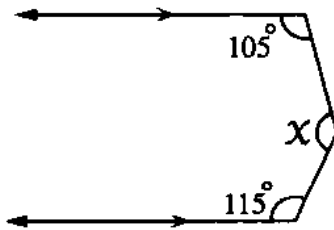
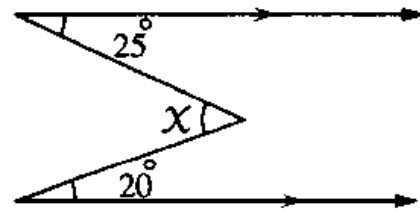
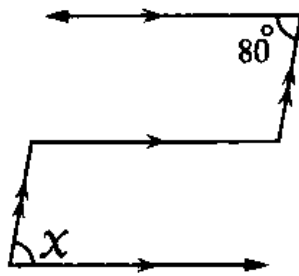
$$\overrightarrow{AE} \parallel \overrightarrow{CB}, \overrightarrow{BA} \parallel \overrightarrow{CD},$$

$$\overrightarrow{AF} \text{ bisects } \angle BAE \text{ and } m(\angle EAF) = 56^\circ$$

Find : $m(\angle C)$



[4] Find the value of x :



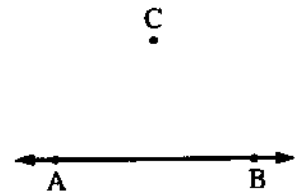
Sheet (7)

Geometric constructions

First: Constructing a perpendicular from a point outside a straight line:

If \overleftrightarrow{AB} is a given straight line , $C \notin \overleftrightarrow{AB}$
as shown in fig. (1)

The required is constructing the perpendicular to \overleftrightarrow{AB} from C



Steps:

Step (1)	Step (2)	Step (3)

Second: Constructing a perpendicular from a point on a straight line:

If : \overleftrightarrow{AB} is a given straight line.

$C \in \overleftrightarrow{AB}$ as shown in fig. (1)

The required is drawing a perpendicular to \overleftrightarrow{AB} from the point C

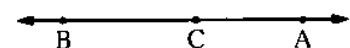


Fig. (1)

Steps:

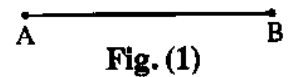
Step (1)	Step (2)	Step (3)

The axis of symmetry of a line segment

It is the straight line perpendicular to it from its midpoint.

Third: Bisecting a given line segment:

If \overline{AB} is a given line segment as shown in fig. (1)



The required is constructing the symmetry axis of the line segment \overline{AB} (The perpendicular to \overline{AB} from its midpoint).

Steps:

Step (1)	Step (2)	Step (3)

Fourth: Bisecting a given angle:

If $\angle ABC$ is a given angle as shown in fig. (1)

The required is constructing the bisector of $\angle ABC$

“Using the compasses and the ruler”

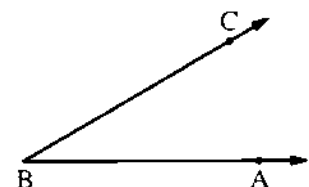


Fig. (1)

Steps:

Step (1)	Step (2)	Step (3)

Fifth: Constructing an angle to be congruent to a given angle:

$\angle ABC$ is a given angle as shown in fig. (1)

The required is drawing $\angle XYZ$ such that $\angle XYZ$ is congruent to $\angle ABC$

i.e.: $m(\angle XYZ) = m(\angle ABC)$

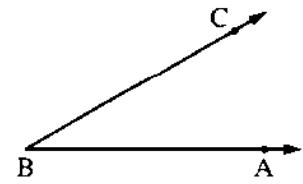


Fig. (1)

Steps:

Step (1)	Step (2)	Step (3)
Step (4)	Step (5)	

Using the ruler and the compasses, draw $\triangle ABC$ in which $AB = AC = 5$ cm. , $BC = 6$ cm. , then draw $\overline{AD} \perp \overline{BC}$ where $\overline{AD} \cap \overline{BC} = \{D\}$
Then find by measuring the length of \overline{AD} (Don't remove the arcs)

Sixth: Drawing a straight line from a given point parallel to given straight line:

\overleftrightarrow{AB} is a given straight line and $C \notin \overleftrightarrow{AB}$ as shown in fig. (1)

C.

Required: The drawing a straight line passing through the point C parallel to \overleftrightarrow{AB}

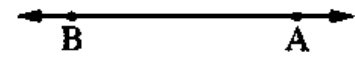
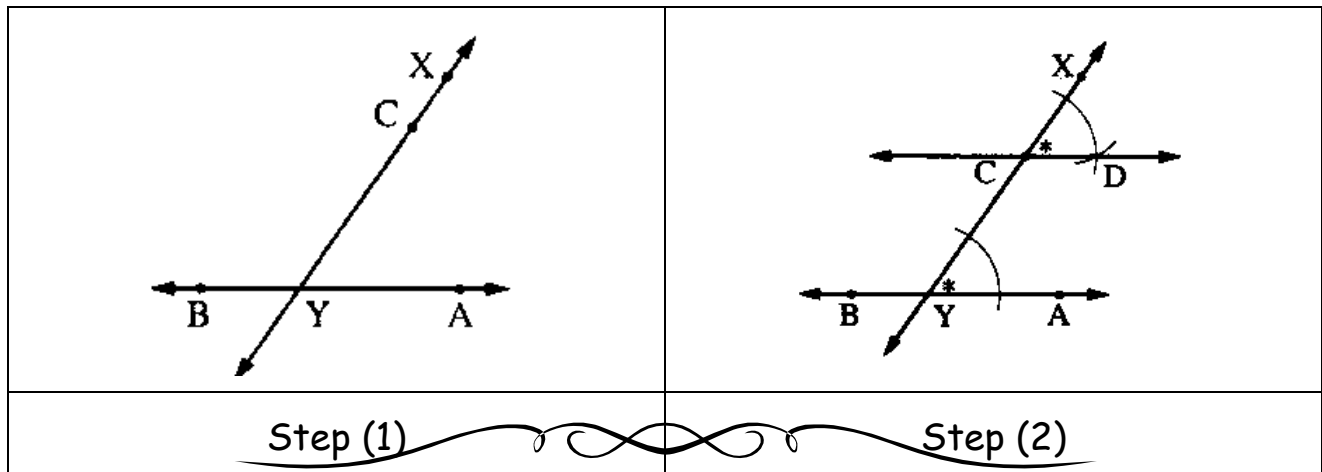



Fig. (1)

Steps:



Using the ruler and the compasses , draw the line segment \overline{BC} with length 7 cm. , then draw the straight line L as an axis of symmetry of it. (Don't remove the arcs)

 Draw an angle whose vertex is A and its measure is 130° , use a ruler and a compasses to divide the angle A into 4 equal angles in measure. (Don't remove the arcs)



Using the geometric instruments, draw an angle of measure 120° and bisect it (Don't remove the arcs).



Using the geometric tools, draw an angle of measure 75° and bisect it (Don't remove the arcs).



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Unit [4] : Geometry And Measurement

Lesson [1] : Geometric Concepts – The Relations Between Angles

1 The line segment

It is a set of points consisting of two distinct points and all points between them when we join them by a ruler.

2 The straight line

If we extend the line segment in both directions infinitely , we will get a straight line.

3 The ray

It is a line segment extended from only one of its terminals without limit.

Remarks

- Each of line segment , straight line and ray is an infinite set of points.
- $\overline{AB} \subset \overleftrightarrow{AB}$, $\overleftrightarrow{AB} \subset \overrightarrow{AB}$ i.e. $\overline{AB} \subset \overleftrightarrow{AB} \subset \overrightarrow{AB}$

4 The plane

A plane is a flat and unbounded surface , and it is extended without limit in all directions

5 The angle

It is the union of two rays with the same starting point , and this point is called the vertex of the angle , and the two rays are called the two sides of the angle.

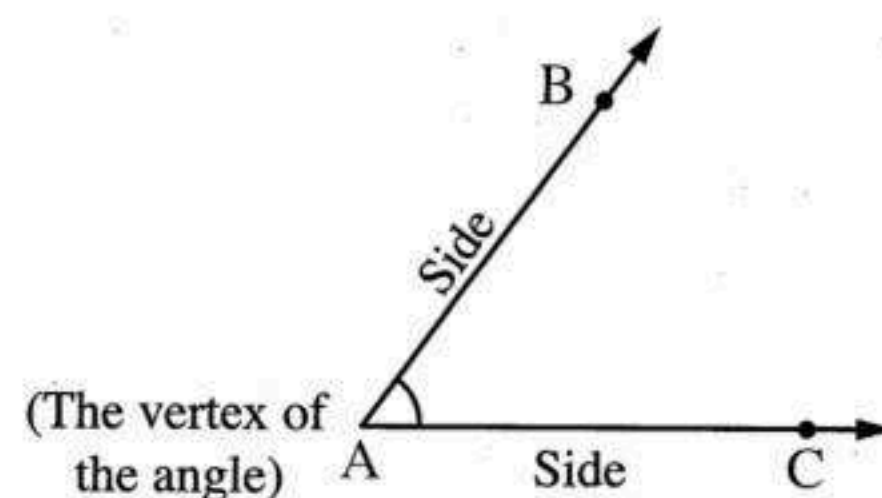
For example :

In the opposite figure :

\overrightarrow{AB} and \overrightarrow{AC} are two rays having the same starting point A , then :

$\overrightarrow{AB} \cup \overrightarrow{AC} = \text{the angle CAB}$

* A is the vertex of the angle CAB



Measurement of the angle

- A degree is divided into parts smaller than it , and they are minute (') and second ('') where the degree equals 60 minutes and the minute equals 60 second and we can change the units of measuring angle by using the calculator.

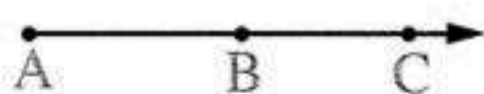
For example :

$$23\frac{1}{2}^{\circ} = 23^{\circ} 30' \quad , \quad 65\frac{1}{4}^{\circ} = 65^{\circ} 15' \quad , \quad 81\frac{1}{8}^{\circ} = 81^{\circ} 7' 30''$$

The types of angles

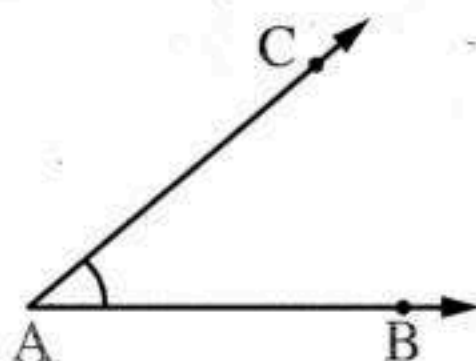
The angles are classified according to their measures as follows :

1 Zero angle



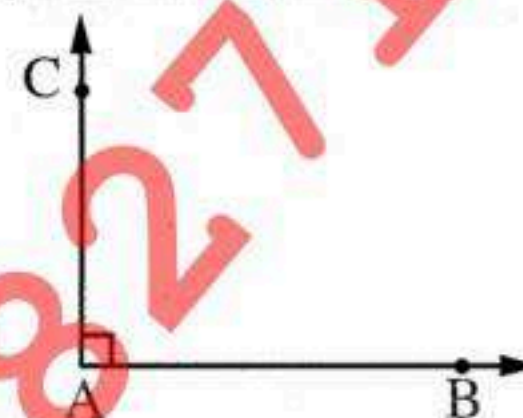
Its measure = 0°
Its sides are coincident.

2 Acute angle



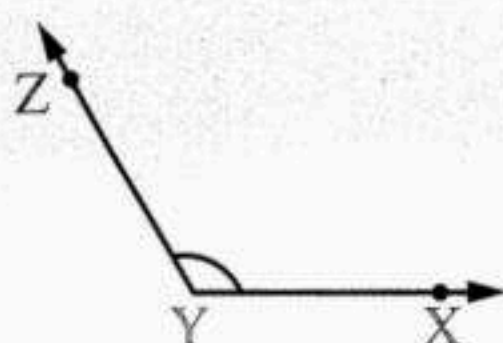
Its measure is more than 0° and less than 90°
i.e. $0^\circ < \text{measure of acute angle} < 90^\circ$

3 Right angle



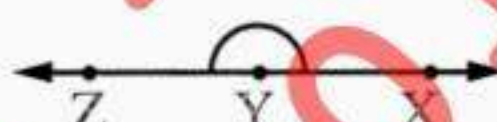
Its measure = 90°

4 Obtuse angle



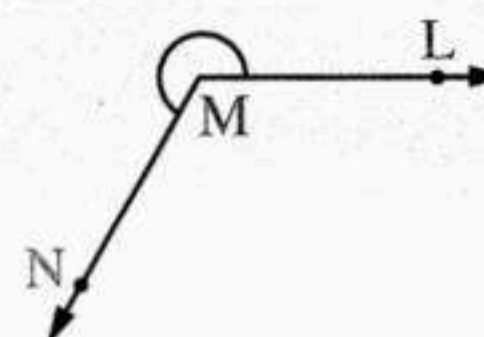
Its measure is more than 90° and less than 180°
i.e.
 $90^\circ < \text{measure of obtuse angle} < 180^\circ$

5 Straight angle



Its measure = 180°
Its sides are forming one straight line.

6 Reflex angle



Its measure is more than 180° and less than 360°
i.e.
 $180^\circ < \text{measure of reflex angle} < 360^\circ$

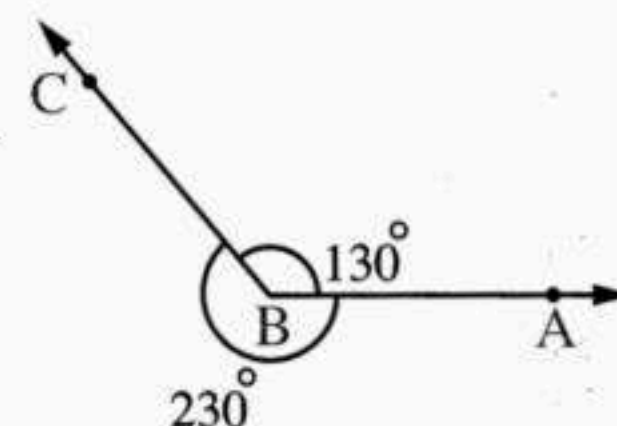
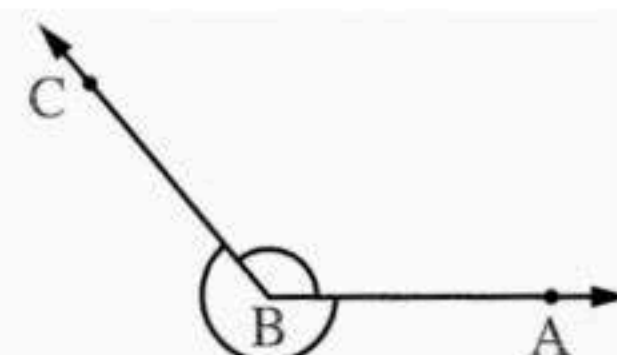
Remark : -

• In the opposite figure :

$$m(\angle ABC) + m(\text{reflex } \angle ABC) = 360^\circ$$

For example :

$$\begin{aligned} \text{If } m(\angle ABC) &= 130^\circ \\ \text{, then } m(\text{reflex } \angle ABC) &= 360^\circ - 130^\circ = 230^\circ \end{aligned}$$



Some relations between the angles

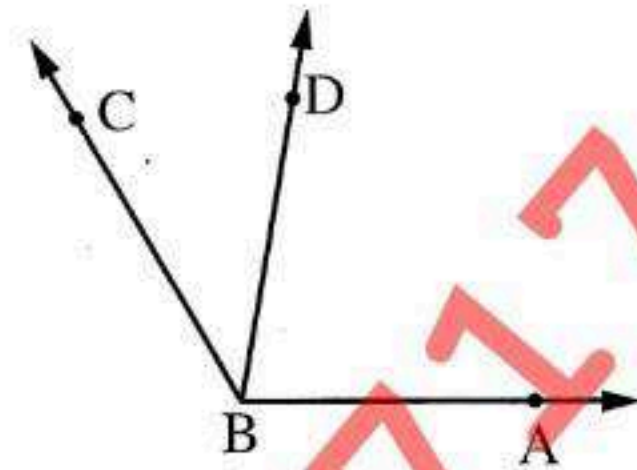
Adjacent angles

Two angles are said to be adjacent if they have a common vertex and a common side and the other two sides are on opposite sides of this common side.

For example :

• In the opposite figure :

- $\angle ABD$ and $\angle DBC$ are two adjacent angles , for :
- They have a common vertex B and a common side \overrightarrow{BD}
 - The two other sides \overrightarrow{BA} and \overrightarrow{BC} are on two opposite sides of \overrightarrow{BD}



Complementary angles

Two angles are said to be complementary if the sum of their measures is 90°

For example :

The two angles whose measures are 55° and 35° are called two complementary angles because $55^\circ + 35^\circ = 90^\circ$

Remarks

- 1 The two complementary angles are either acute angles or one of them is zero angle and the other is a right angle.
- 2 The complements of the same angle (or the equal angles in measure) are equal in measure.
i.e. If $\angle A$ complements $\angle B$, $\angle C$ complements $\angle B$, then $m(\angle A) = m(\angle C)$

Supplementary angles

Two angles are said to be supplementary if the sum of their measures is 180°

For example :

The two angles whose measures are 143° and 37° are called two supplementary angles because $143^\circ + 37^\circ = 180^\circ$

Remarks

- 1 The two supplementary angles are either one of them is obtuse and the other is acute or each of them is a right angle or one of them is zero angle and the other is a straight angle.
- 2 The supplements of the same angle (or the equal angles in measure) are equal in measure.
i.e. If $\angle A$ supplements $\angle B$ and $\angle C$ supplements $\angle B$, then $m(\angle A) = m(\angle C)$

The two adjacent supplementary angles

Two adjacent angles formed by a straight line and a ray with a starting point on this straight line , are supplementary.

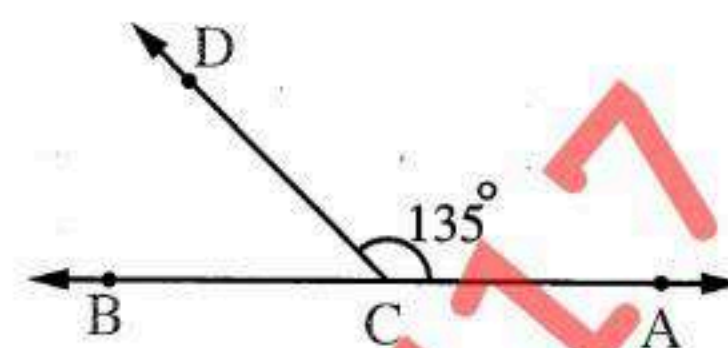
i.e. In the opposite figure :

$$\text{If } \overleftrightarrow{AB} \cap \overleftrightarrow{CD} = \{C\}$$

Therefore , $m(\angle ACD) + m(\angle DCB) = 180^\circ$ "Straight angle"

And if $m(\angle ACD) = 135^\circ$

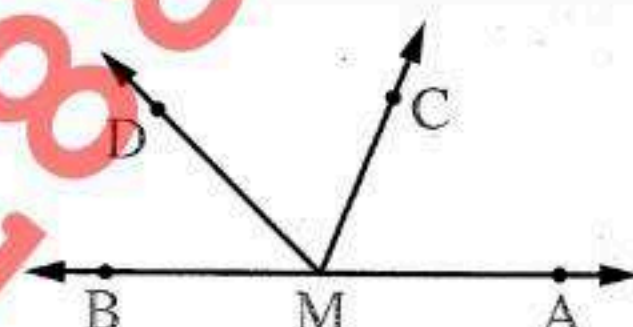
Then $m(\angle DCB) = 180^\circ - 135^\circ = 45^\circ$



Remark : -

If $M \in \overleftrightarrow{AB}$, and \overrightarrow{MC} and \overrightarrow{MD} are drawn on one side of \overleftrightarrow{AB} ,

then $m(\angle AMC) + m(\angle CMD) + m(\angle DMB) = 180^\circ$



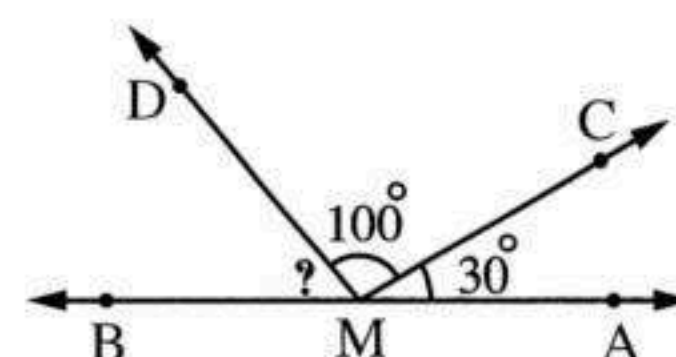
For example :

• In the opposite figure :

If $M \in \overleftrightarrow{AB}$, $m(\angle AMC) = 30^\circ$

, $m(\angle CMD) = 100^\circ$

, then : $m(\angle DMB) = 180^\circ - (30^\circ + 100^\circ) = 180^\circ - 130^\circ = 50^\circ$



Vertically opposite angles (V.O.A.)

If two straight lines intersect , then the measures of each two vertically opposite angles are equal.

• In the opposite figure :

If \overleftrightarrow{AB} and \overleftrightarrow{CD} intersect at M

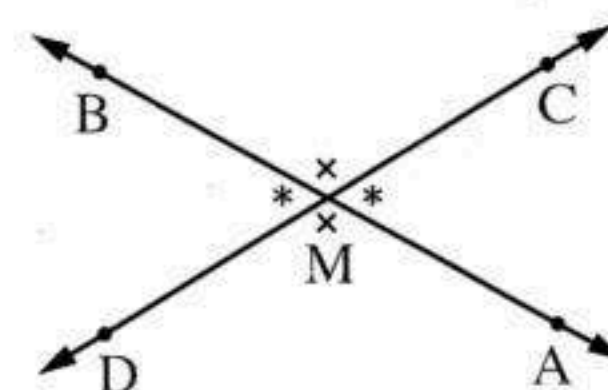
Then :

• $\angle AMC$ and $\angle BMD$ are vertically opposite angles ,

, then $m(\angle AMC) = m(\angle BMD)$

• Also , $\angle CMB$ and $\angle AMD$ are vertically opposite angles ,

, then $m(\angle CMB) = m(\angle AMD)$



Accumulative angles at a point

The sum of the measures of the accumulative angles at a point is 360°

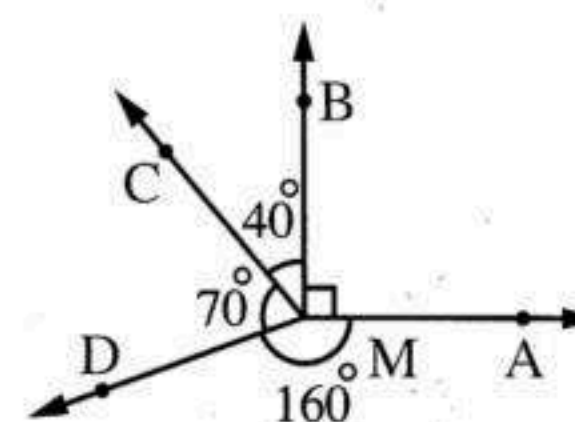
• In the opposite figure :

\overrightarrow{MA} , \overrightarrow{MB} , \overrightarrow{MC} and \overrightarrow{MD} are rays having the same starting point M

The angles $\angle AMB$, $\angle BMC$, $\angle CMD$ and $\angle DMA$

are called accumulative angles at the point M , hence we get :

$m(\angle AMB) + m(\angle BMC) + m(\angle CMD) + m(\angle DMA) = 90^\circ + 40^\circ + 70^\circ + 160^\circ = 360^\circ$



The angle bisector

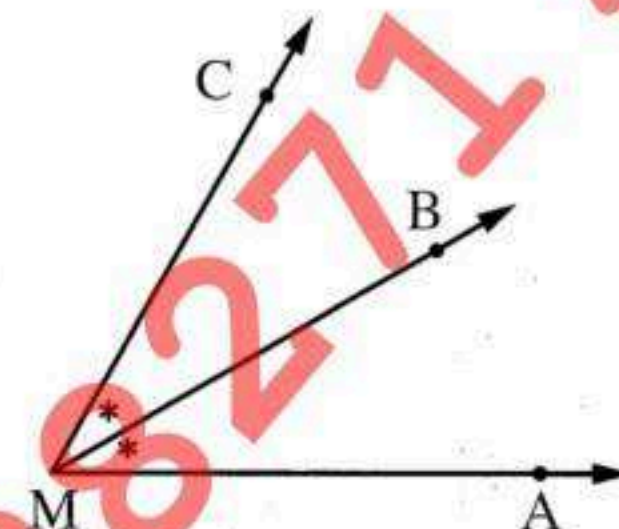
It is the ray that divides the angle into two halves (two equal angles in measure).

• In the opposite figure :

\overrightarrow{MB} bisects $\angle AMC$

i.e. $m(\angle AMB) = m(\angle BMC) = \frac{1}{2} m(\angle AMC)$

or $m(\angle AMC) = 2 m(\angle AMB) = 2 m(\angle BMC)$



Lesson [3] : Congruence - Congruent Triangles

First Congruence of two line segment

Generally

Two line segments are congruent if they are equal in length

If the length of \overline{XY} = the length of \overline{ZL} , then $\overline{XY} \equiv \overline{ZL}$

Second Congruence of two angles

Generally

Two angles are congruent if they are equal in measure.

If $m(\angle C) = m(\angle D)$, then $\angle C \equiv \angle D$

Third Congruence of two polygons

Remark

If the two polygons are congruent , then each side and each angle in one of them is congruent to its corresponding element in the other polygon.

For example :

If $\triangle ABC$ and $\triangle XYZ$ are two triangles in which :

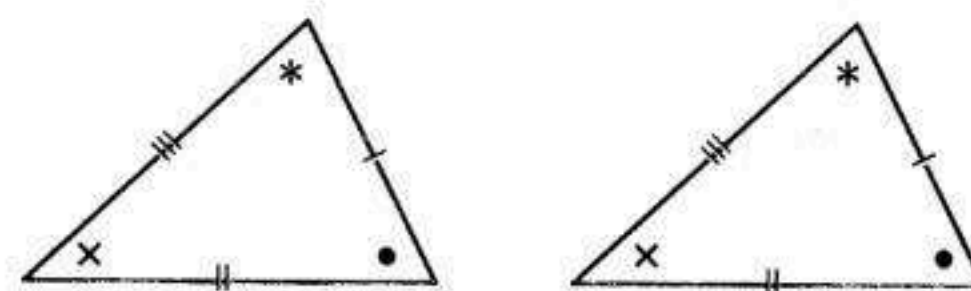
1 $AB = XY$, $AC = XZ$

and $BC = YZ$

2 $m(\angle A) = m(\angle X)$, $m(\angle B) = m(\angle Y)$

and $m(\angle C) = m(\angle Z)$

, then : $\triangle ABC \equiv \triangle XYZ$



Cases of congruence of two triangles

Two sides and the included angle

Two angles and one side

Three sides

Hypotenuse and one side in the right-angled triangle

The first case (Two sides and the included angle S.A.S.)

Two triangles are congruent if two sides and the included angle of one triangle are congruent to the corresponding parts of the other triangle.

Remark

In the case of congruence of two triangles by two sides and the included angle, the included angle should be between the two sides.

The second case (Two angles and one side A.S.A.)

Two triangles are congruent if two angles and the side drawn between their vertices of one triangle are congruent to the corresponding parts of the other triangle.

The third case (Three sides S.S.S.)

Two triangles are congruent if each side of one triangle is congruent to the corresponding side of the other triangle.

Remark

If each angle of one triangle is congruent to the corresponding angle of the other triangle, it is not necessary for the two triangles to be congruent.

The fourth case (Hypotenuse and one side in the right-angled triangle R.H.S.)

Two right-angled triangles are congruent if the hypotenuse and a side of one triangle are congruent to the corresponding parts of the other triangle.

Remark

The two right-angled triangles are congruent if the two sides of the right angle in one of them are congruent to the corresponding elements in the other triangle. (This case is an application of the first case of congruence of two triangles).

Lesson [4] : Parallelism

If a straight line intersects two parallel straight lines, then each two alternate angles are equal in measure.

If a straight line intersects two parallel straight lines, then each two corresponding angles are equal in measure.

If a straight line intersects two parallel straight lines, then each two interior angles in the same side of the transversal are supplementary.

How to prove that two straight lines are parallel ?

The two straight lines are parallel if a third straight line intersects them (as a transversal) and one of the following cases is satisfied :

- 1 Two alternate angles have the same measure.
- 2 Two corresponding angles have the same measure.
- 3 Two interior angles in the same side of the transversal are supplementary.

- 3 Using the geometric instruments or computer , draw the straight lines L_1 , L_2 , L_3 and L_4 , then draw the transversal M_1 to cut them at A , B , C and D respectively

Where : $AB = BC = CD$

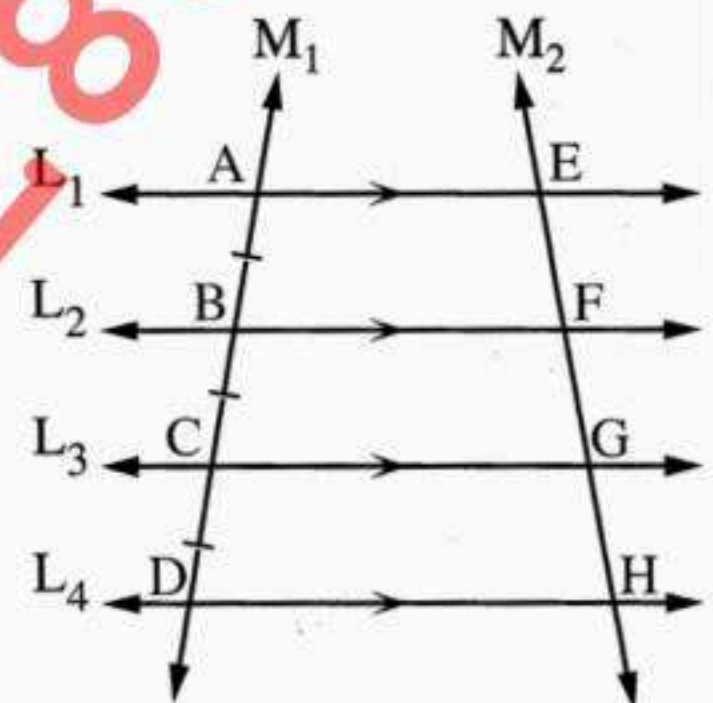
Then draw another transversal M_2 to cut them at E , F , G and H respectively.

, then find by measuring the lengths of \overline{EF} , \overline{FG} and \overline{GH}

We find that : $EF = FG = GH$

Generally : If : $L_1 \parallel L_2 \parallel L_3 \parallel L_4$, M_1 and M_2 are two transversal in which

$AB = BC = CD$, then $EF = FG = GH$



Generally

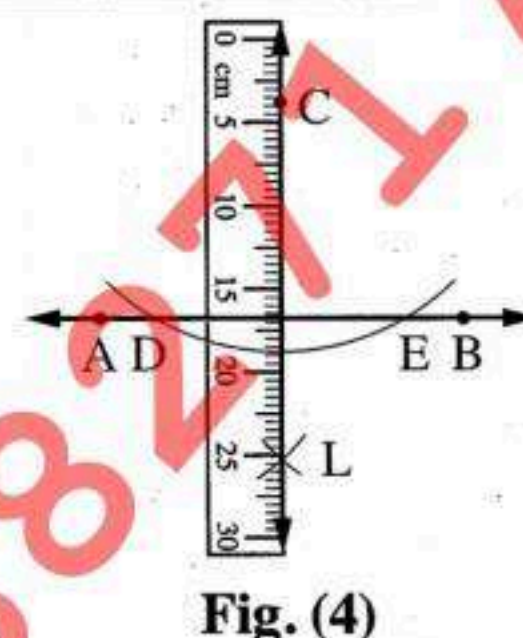
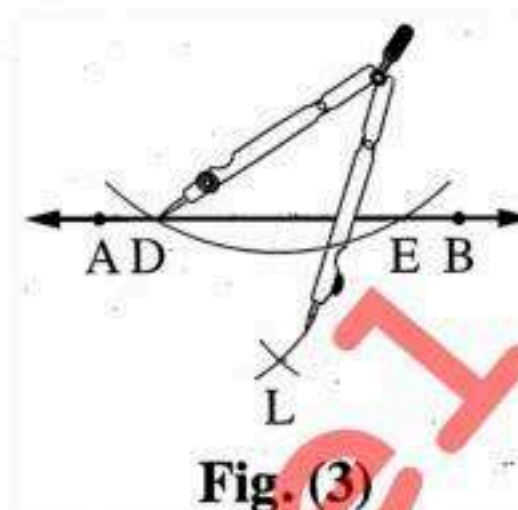
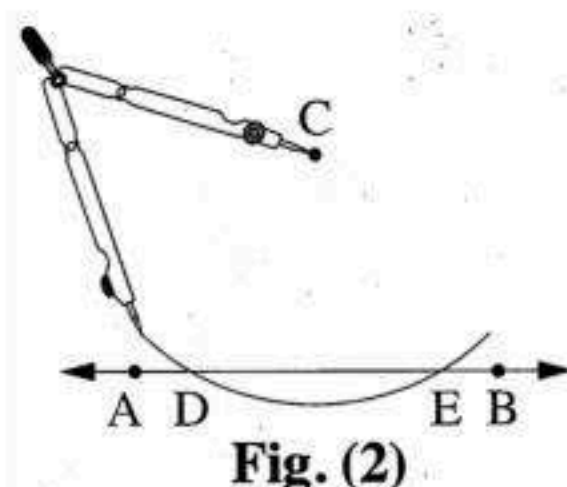
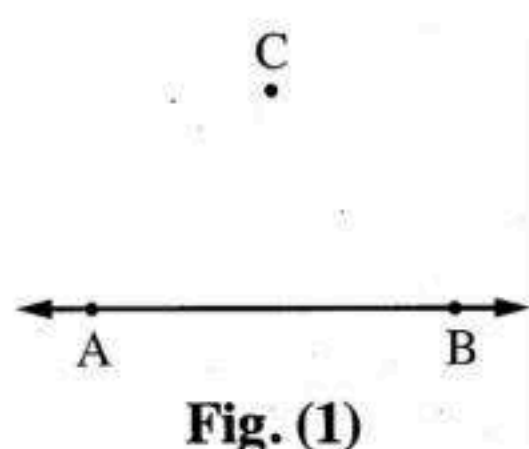
If parallel straight lines divide a straight line into segments of equal lengths , then they divide any other straight line into segments of equal lengths.

Generally : The perpendicular to one of two coplaner parallel straight lines is perpendicular to the other
And vice versa , if two coplaner straight lines are perpendicular to a third one , then the two straight lines are parallel.

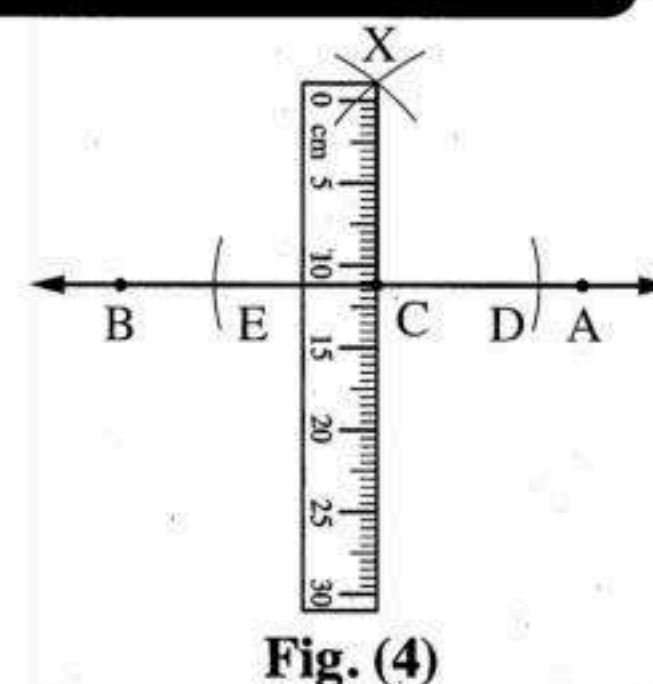
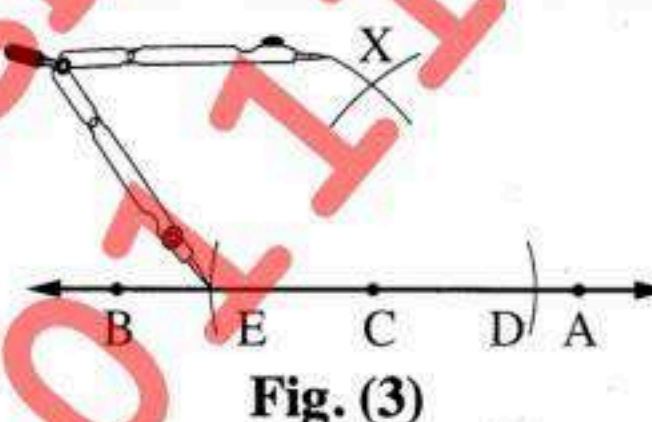
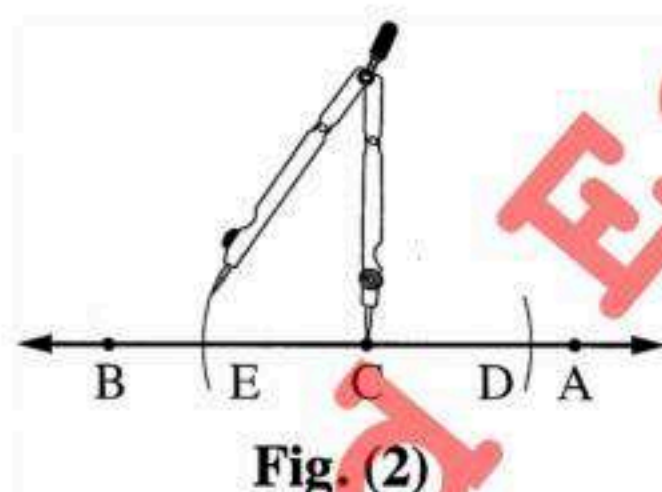
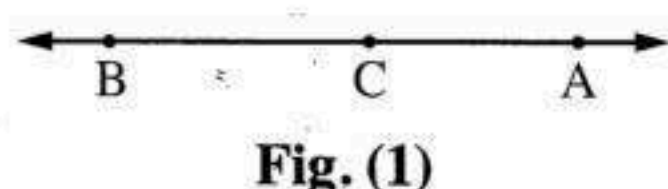
Generally : If two straight lines are parallel to a third straight line , then these two straight lines are parallel.

Lesson [5] : Geometric Constructions

First Constructing a perpendicular from a point outside a straight line :



Second Drawing a perpendicular to a straight line that passes through a point which belongs to that straight line.



The axis of symmetry of a line segment :

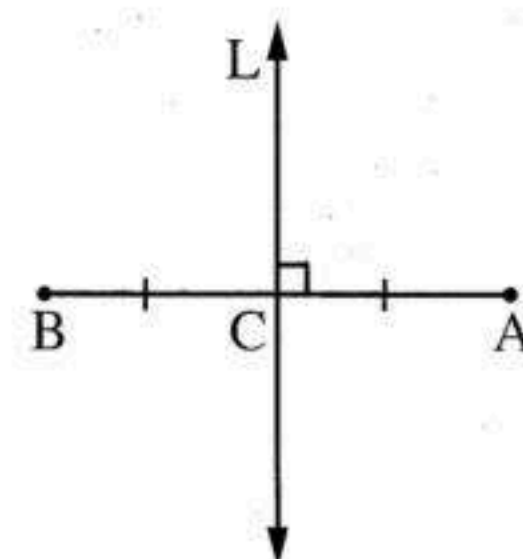
It is the straight line perpendicular to it from its midpoint.

• In the opposite figure :

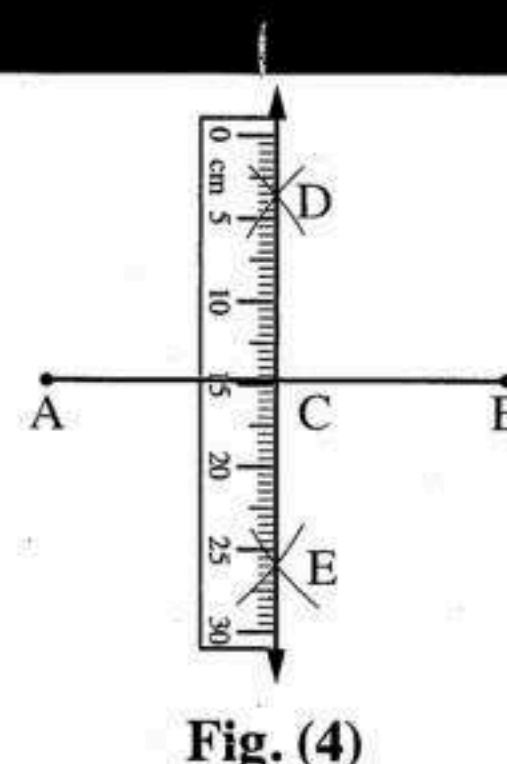
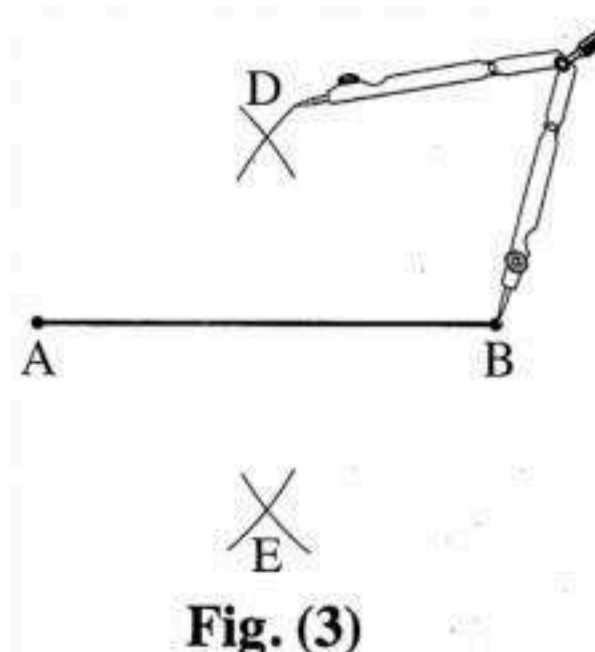
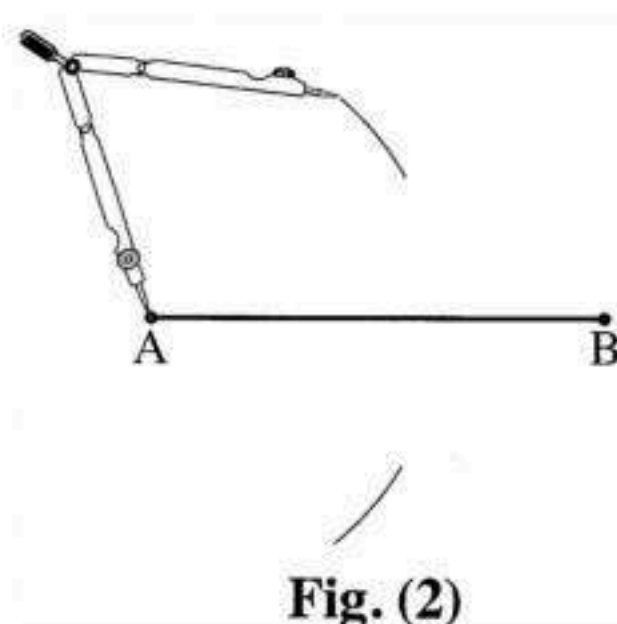
If C is the midpoint of \overline{AB} and the straight line

$L \perp \overline{AB}$ from the point C

Then the straight line L is the axis of symmetry of the line segment \overline{AB}



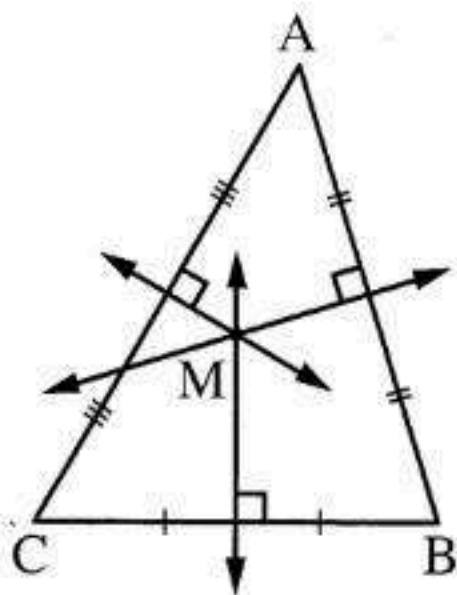
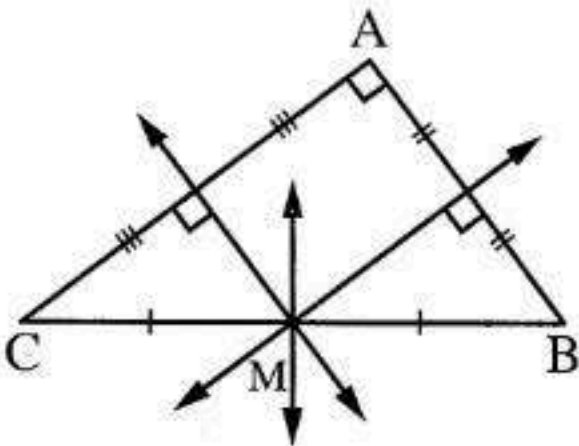
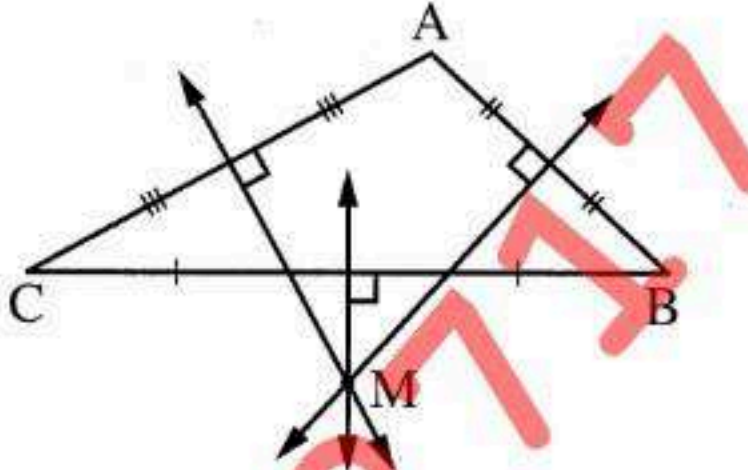
Third Bisecting a given line segment "Constructing the symmetry axis of a given line segment"



Remarks

The axes of symmetry of the sides of any triangle are intersecting at one point (say M).

The position of M differs according to the type of the triangle as follows :

Acute-angled triangle	Right-angled triangle	Obtuse-angled triangle
		
M is inside the triangle.	M is the midpoint of the hypotenuse.	M is outside the triangle.
<p>• The lengths of the line segments joining the point of intersection of the axes of symmetry and the vertices of the triangle are equal in all previous cases. i.e. $AM = BM = CM$</p>		

Fourth Constructing the bisector of a given angle :

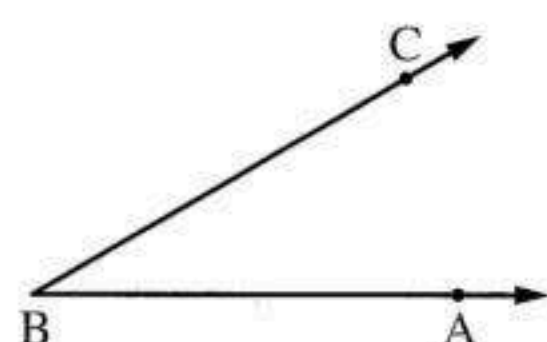


Fig. (1)

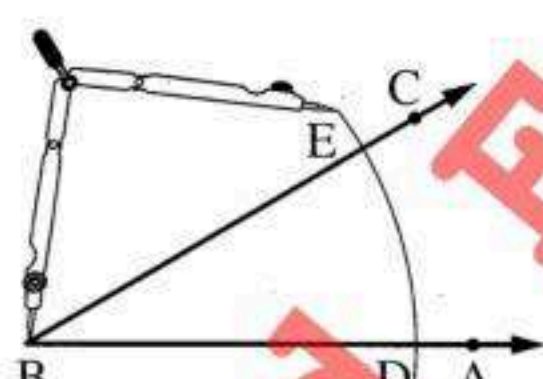


Fig. (2)

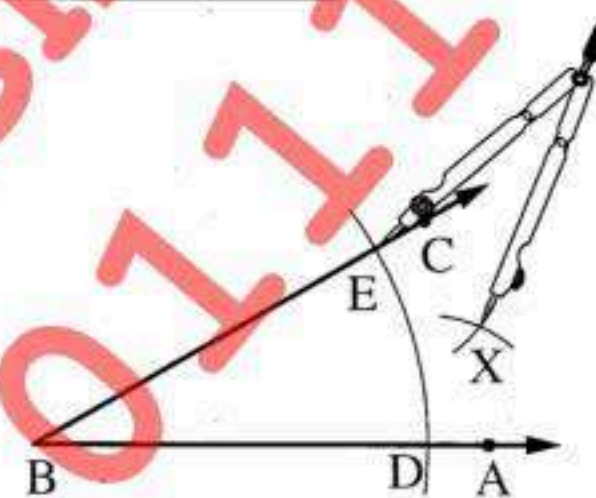


Fig. (3)

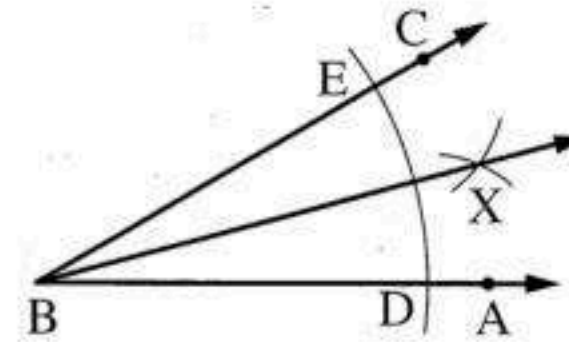


Fig. (4)

Fifth Constructing an angle to be congruent to a given angle (without using protractor) :

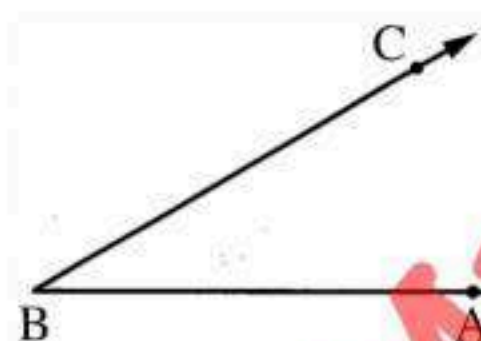


Fig. (1)



Fig. (2)

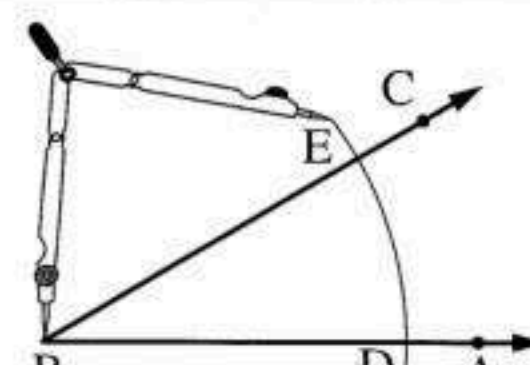


Fig. (3)

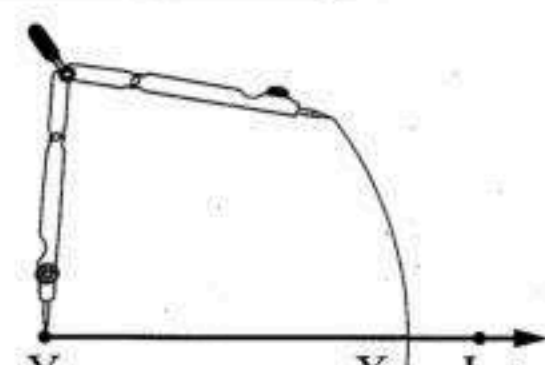


Fig. (4)

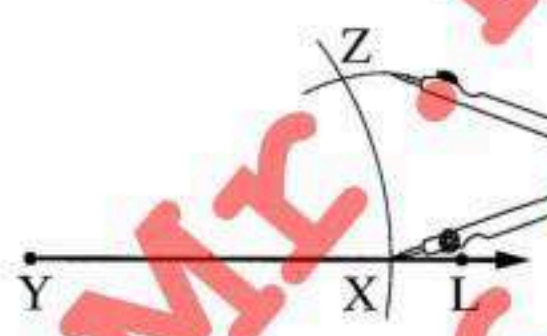


Fig. (5)

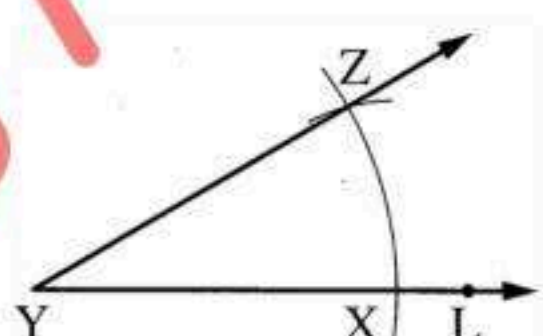


Fig. (6)

Sixth Drawing a straight line from a given point parallel to given straight line.

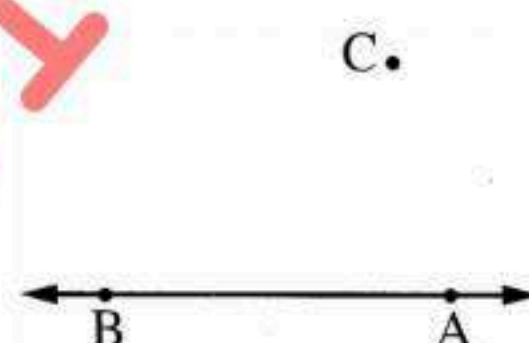


Fig. (1)

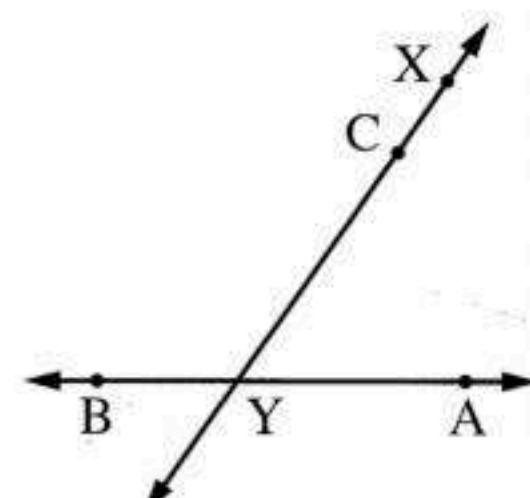


Fig. (2)

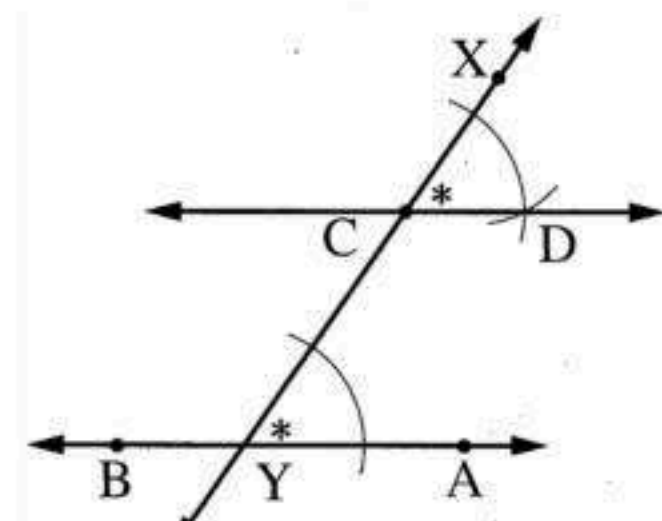


Fig. (3)

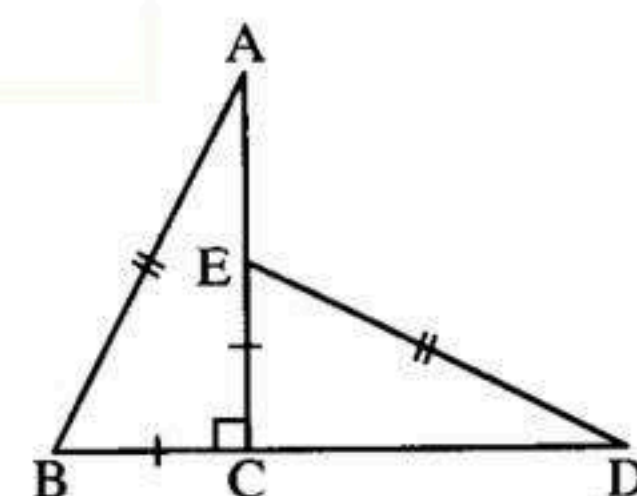
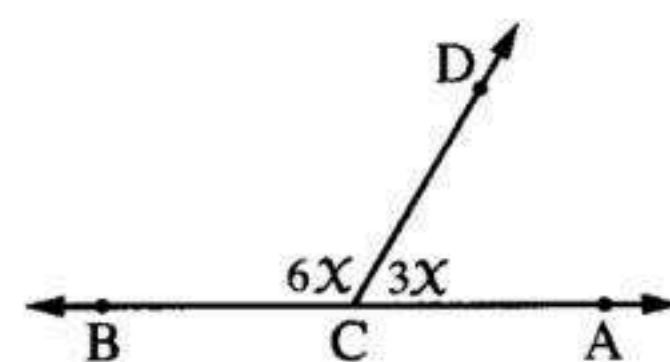
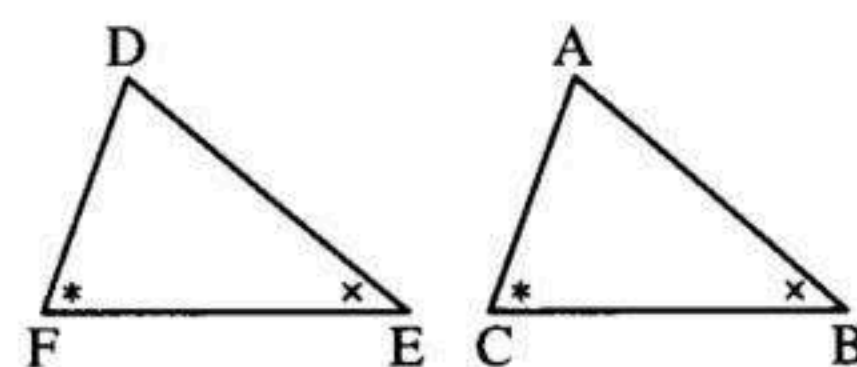
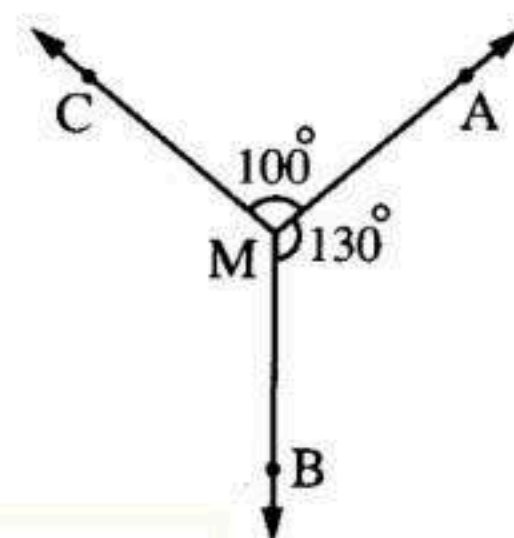
[A] : Choose The Correct Answer : -

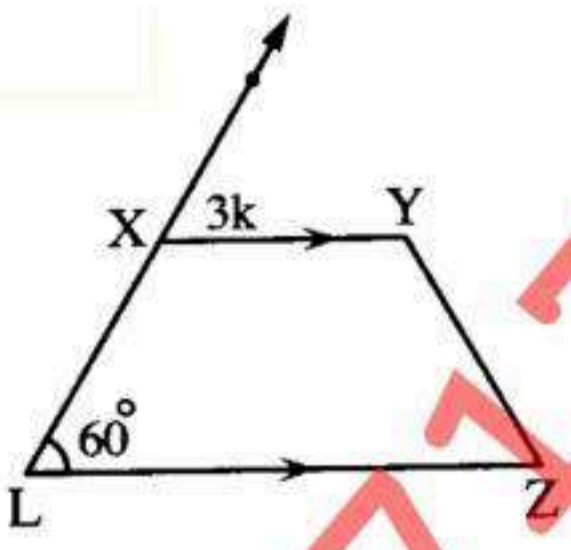
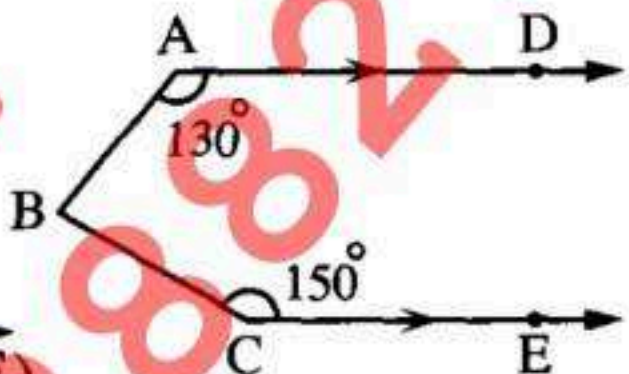
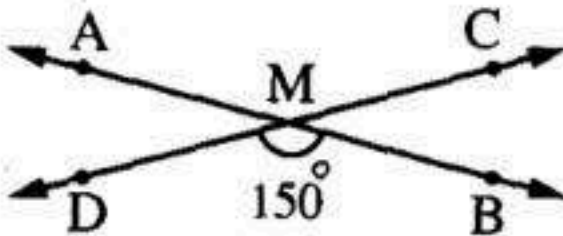
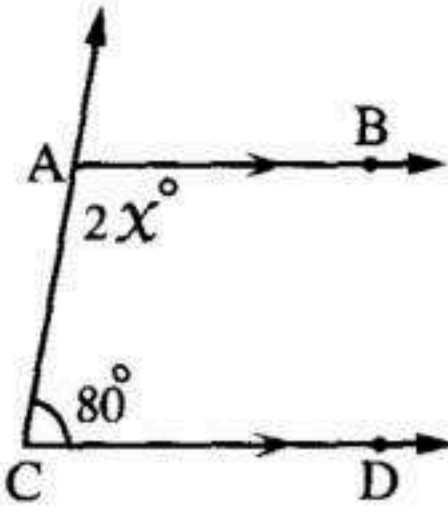
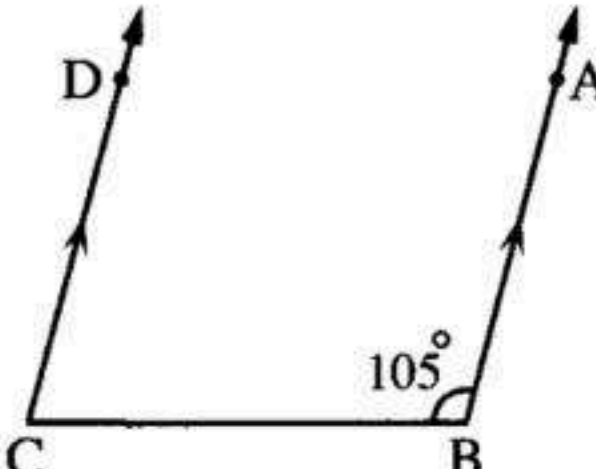
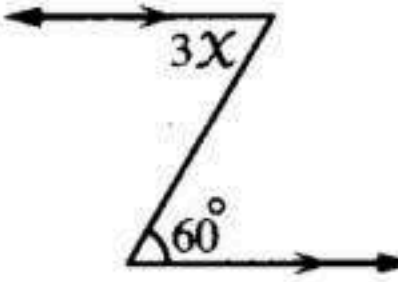
1	The measure of the right angle =° (a) 90 (b) 180 (c) 270 (d) 360	A
2	The measure of the straight angle =° (a) 90 (b) 180 (c) 360 (d) zero	B
3	The type of the angle of measure $179^{\circ} 60'$ is angle. (a) acute (b) obtuse (c) straight (d) right	C
4	The angle whose measure is 108° is angle. (a) an acute (b) a right (c) an obtuse (d) a straight	C
5	The angle whose measure is 210° is angle. (a) an acute (b) a right (c) an obtuse (d) a reflex	D
6	If $m(\angle B) = 120^{\circ}$, then $m(\text{reflex } \angle B) = \dots\dots\dots^{\circ}$ (a) 60 (b) 120 (c) 240 (d) 180	C
7	$\overline{AB} \dots\dots\dots \overrightarrow{AB}$. (a) \in (b) \notin (c) \subset (d) $\not\subset$	C
8	If $m(\angle A) + m(\angle B) = 90^{\circ}$, then $\angle A$, $\angle B$ are angles. (a) complementary (b) supplementary (c) equal (d) adjacent	A
9	The angle of measure 70° complements an angle of measure° (a) 90 (b) 20 (c) 180 (d) 110	B
10	If $\angle A$ complements $\angle B$, $m(\angle A) = m(\angle B)$, then $m(\angle A) = \dots\dots\dots^{\circ}$ (a) 90 (b) 180 (c) 45 (d) 60	C
11	The acute angle complements angle. (a) an acute (b) an obtuse (c) a right (d) a reflex	A
12	If the two adjacent angles are complementary, then their outer sides are (a) perpendicular. (b) coincident. (c) on the same straight line. (d) skew.	A

13	The two angles 35° , 55° are (a) complementary. (b) supplementary. (c) adjacent. (d) reflex.	A
14	If $m(\angle X) = 2 m(\angle Y)$, $\angle X$ and $\angle Y$ are two complementary angles , then $m(\angle Y) = \dots\dots\dots$ (a) 90° (b) 45° (c) 30° (d) 15°	C
15	The supplementary angle of the angle of measure 70° is (a) 30° (b) 110° (c) 20° (d) 290°	B
16	The acute angle supplements angle. (a) an acute (b) an obtuse (c) a right (d) a reflex	B
17	If one of two supplementary angles is right, then the other is angle. (a) an acute (b) a right (c) an obtuse (d) a straight	B
18	The obtuse angle supplements angle. (a) an acute (b) an obtuse (c) a right (d) a reflex	A
19	If $\angle A$ supplements $\angle B$ and $\angle A \equiv \angle B$, then $m(\angle A) = \dots\dots\dots^\circ$ (a) 180 (b) 90 (c) 360 (d) 45	B
20	The sum of the measures of two adjacent angles formed by a straight line and a ray with a starting point on this straight line is (a) 90° (b) 180° (c) 270° (d) 360°	B
21	If $\angle A$ and $\angle B$ are supplementary angles and $m(\angle A) = 2 m(\angle B)$, then $m(\angle A) = \dots\dots\dots^\circ$ (a) 90 (b) 60 (c) 180 (d) 120	D
22	If the ratio between two adjacent supplementary angles is $2 : 3$, then the measure of the smallest angle is (a) 108 (b) 36 (c) 72 (d) 125	C
23	If $\angle A \equiv \angle B$, $\angle A$ and $\angle B$ are two supplementary angles , then $\frac{1}{3} m(\angle A) = \dots\dots\dots$ (a) 15° (b) 30° (c) 40° (d) 60°	B

24	The sum of measures of the accumulative angles at a point equals (a) 90° (b) 180° (c) 630° (d) 360°	D
25	If $AB = XY$, then $\overline{AB} \dots\dots\dots \overline{XY}$ (a) $>$ (b) \equiv (c) $<$ (d) \neq	B
26	In $\triangle ABC$, if $m(\angle A) = 30^\circ$, $m(\angle B) = 90^\circ$, then $m(\angle C) = \dots\dots\dots$ (a) 60° (b) 30° (c) 45° (d) 90°	A
27	If $\triangle XYZ \equiv \triangle LMN$, then $m(\angle Y) = m(\angle \dots\dots\dots)$ (a) L (b) M (c) N (d) X	B
28	If $\triangle ABC \equiv \triangle XYZ$ and $m(\angle C) = 50^\circ$, then $m(\angle \dots\dots\dots) = 50^\circ$ (a) X (b) Y (c) Z (d) M	C
29	If $\overline{AB} \equiv \overline{XY}$, then $AB - XY = \dots\dots\dots$ (a) AB (b) XY (c) 1 (d) zero	D
30	If $\triangle ABC \equiv \triangle XYZ$, then $BC = \dots\dots\dots$ (a) YZ (b) XZ (c) XY (d) AC	A
31	If $\triangle ABC \equiv \triangle MNO$, $m(\angle M) = 40^\circ$ and $m(\angle C) = 60^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$ (a) 40 (b) 80 (c) 60 (d) 100	B
32	If $\triangle ABC \equiv \triangle XYZ$ and $m(\angle A) + m(\angle X) = 100^\circ$, then $m(\angle A) = \dots\dots\dots^\circ$ (a) 100 (b) 80 (c) 40 (d) 50	D
33	If $\triangle ABC \equiv \triangle XYZ$, $m(\angle A) + m(\angle C) = 110^\circ$, then $m(\angle Y) = \dots\dots\dots^\circ$ (a) 50 (b) 70 (c) 80 (d) 100	B
34	If two straight lines are parallel to a third straight line , then they are (a) perpendicular. (b) intersecting. (c) parallel. (d) congruent.	C
35	If parallel straight lines divide a straight line into segments of equal lengths , then they divide any other straight line into segments of lengths. (a) parallel (b) not equal (c) equal (d) perpendicular	C

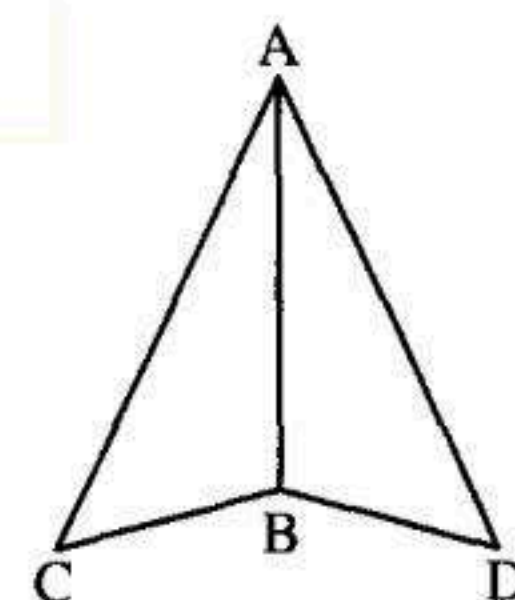
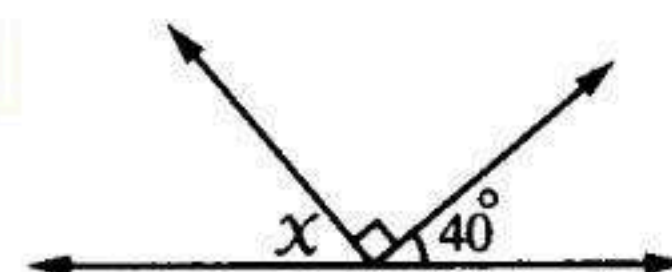
36	The straight line that is perpendicular to one of two parallel lines is to the other. (a) parallel (b) congruent (c) perpendicular (d) equal	C
37	If $\overleftrightarrow{AB} \parallel \overleftrightarrow{XY}$, then $\overleftrightarrow{AB} \cap \overleftrightarrow{XY} = \dots\dots\dots$ (a) $\{B\}$ (b) \overline{AX} (c) \emptyset (d) $\{Y\}$	C
38	If $L_1 \parallel L_2$ and $L_1 \perp L_3$, then (a) $L_1 \perp L_2$ (b) $L_1 \parallel L_3$ (c) $L_2 \parallel L_3$ (d) $L_2 \perp L_3$	D
39	In the opposite figure : $m(\angle CMB) = \dots\dots\dots^\circ$ (a) 230 (b) 100 (c) 130 (d) 30	C
40	In the opposite figure : The necessary condition to make $\triangle ABC \equiv \triangle DEF$ is (a) $AB = DE$ (b) $AC = DF$ (c) $BC = EF$ (d) $m(\angle A) = m(\angle D)$	C
41	In the opposite figure : $\overleftrightarrow{AB} \cap \overleftrightarrow{CD} = \{C\}$, then $x = \dots\dots\dots^\circ$ (a) 180 (b) 30 (c) 20 (d) 120	C
42	In the opposite figure : If $AB = DE$, $BC = EC$, $\overline{AC} \perp \overline{BD}$, then $m(\angle A) = \dots\dots\dots$ (a) $m(\angle B)$ (b) $m(\angle D)$ (c) $m(\angle DEC)$ (d) $m(\angle ACD)$	B



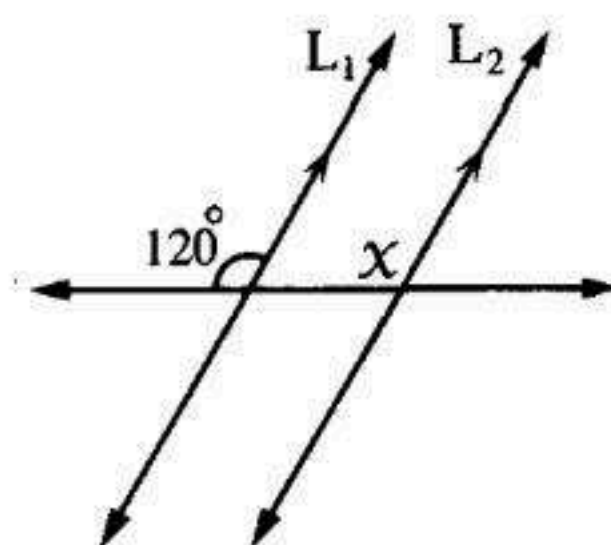
43	<p>In the opposite figure : If $\overline{XY} \parallel \overline{LZ}$, then $k = \dots\dots\dots^\circ$</p> <p>(a) 90 (b) 60 (c) 30 (d) 20</p>		D
44	<p>In the opposite figure : $\overline{AD} \parallel \overline{CE}$ $m(\angle B) = \dots\dots\dots^\circ$ (Hint : Draw a line passing through B and parallel to \overline{AD} and \overline{CE})</p> <p>(a) 70 (b) 80 (c) 90 (d) 100</p>		B
45	<p>In the opposite figure : $\overline{AB} \cap \overline{DC} = \{M\}$, $m(\angle AMC) = \dots\dots\dots^\circ$</p> <p>(a) 30 (b) 210 (c) 150 (d) 60</p>		C
46	<p>In the opposite figure : $x = \dots\dots\dots^\circ$</p> <p>(a) 40 (b) 80 (c) 50 (d) 100</p>		C
47	<p>In the opposite figure : $m(\angle C) = \dots\dots\dots$</p> <p>(a) 105° (b) 75° (c) 45° (d) 90°</p>		B
48	<p>In the opposite figure : $x = \dots\dots\dots^\circ$</p> <p>(a) 20 (b) 30 (c) 40 (d) 120</p>		A

[A] : Complete the Following : -

- 1 The acute angle , whose measure is less than and more than
- 2 $\overrightarrow{AB} \cup \overrightarrow{AC} = \dots\dots\dots$
- 3 The type of the angle of measure $89^\circ 60'$ is
- 4 If the two adjacent angles are supplementary angles , then their outer sides are
- 5 The two bisectors of two adjacent supplementary angles are
- 6 The two adjacent angles formed by a straight line and a ray with a starting point on this straight line are
- 7 In the opposite figure :
 $x = \dots\dots\dots^\circ$
- 8 If two straight lines intersect , then the measures of each two vertically opposite angles are
- 9 The two vertically opposite angles are in measure.
- 10 If $\triangle ABC \cong \triangle XYZ$, then $\angle CAB \cong \angle \dots\dots\dots$
- 11 If the polygon ABCDE \cong the polygon XYZEF , then BC =
- 12 If polygon AXDY \cong polygon BXYC , then AD =
- 13 In the opposite figure :
 If $\triangle ABC \cong \triangle ABD$, the perimeter of the figure ACBD = 20 cm. ,
 AB = 6 cm. , then the perimeter of $\triangle ABC = \dots\dots\dots$ cm.



14	The two triangles are congruent if two sides and of one triangle are congruent with their corresponding parts in the other triangle.
15	The two right-angled triangles are congruent if
16	The two right-angled triangles are congruent if the and a side of one triangle are congruent with their corresponding parts in the other triangle.
17	Two triangles are congruent if each of one triangle is congruent to its corresponding part of the other triangle.
18	If \overleftrightarrow{AB} and \overleftrightarrow{CD} lie in the same plane and $\overleftrightarrow{AB} \cap \overleftrightarrow{CD} = \emptyset$, then \overleftrightarrow{AB} and \overleftrightarrow{CD} are
19	If two straight lines are parallel to a third line, then the two straight lines are
20	If a straight line intersects two parallel straight lines, then every two corresponding angles are
21	If a straight line intersects two parallel lines, then each two alternate angles are
22	If a straight line intersects two parallel straight lines, then each two interior angles in the same side of the transversal are
23	The straight line that is perpendicular to one of two parallel lines is also
24	If two straight lines are perpendicular to a third line, then the two straight lines are
25	Two straight lines are parallel if they are cut by a transversal such that the two interior angles on one side of the transversal are
26	<p>In the opposite figure :</p> <p>L_1, L_2 are two parallel straight lines</p> <p>, then $x = \dots\dots\dots^\circ$</p>



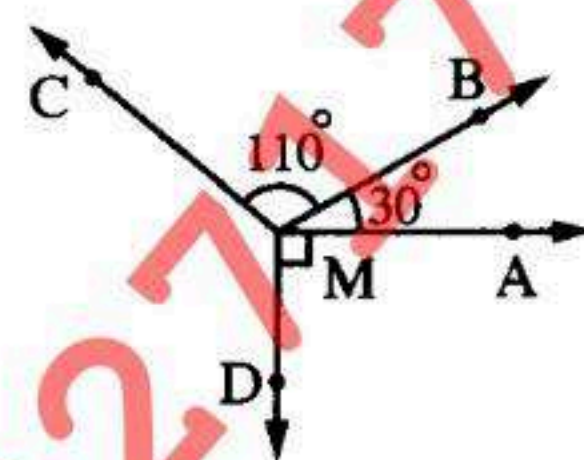
[B] : Essay Problems : -

1

In the opposite figure :

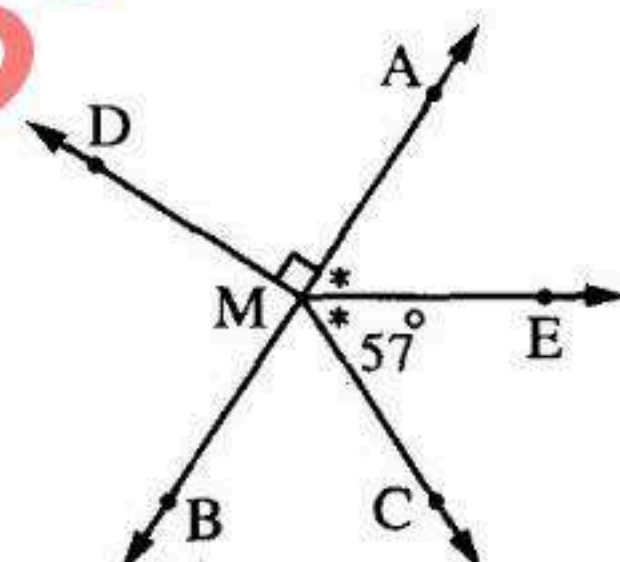
$m(\angle AMB) = 30^\circ, m(\angle BMC) = 110^\circ$

$m(\angle AMD) = 90^\circ$

Find : $m(\angle CMD)$ 

2016 Exam (15) Question (3) (b)

2

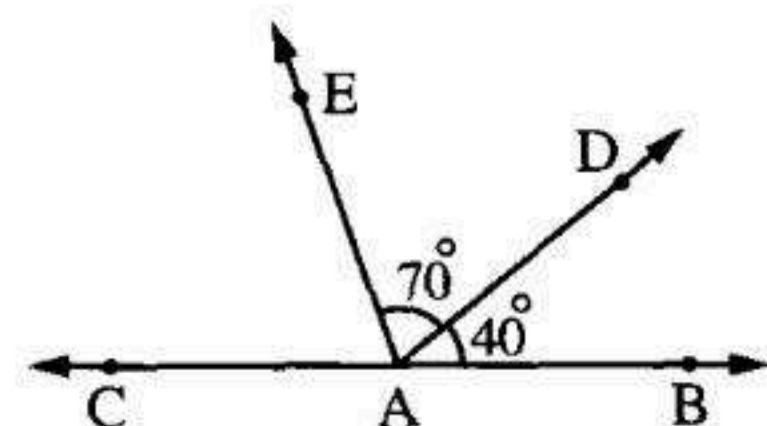
In the opposite figure :**Calculate :** $m(\angle DMC)$ (give reason)

2016 Exam (2) Question (3) (b)

3

In the opposite figure :

$m(\angle BAD) = 40^\circ, m(\angle DAE) = 70^\circ, A \in \overleftrightarrow{BC}$

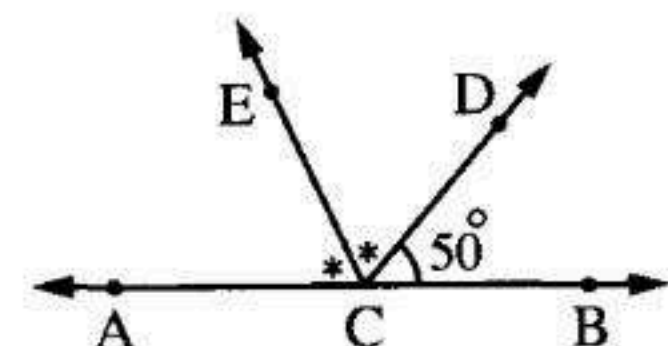
Prove that : \overrightarrow{AE} bisects $\angle DAC$ 

2016 Exam (4) Question (3) (a)

4

In the opposite figure :

$C \in \overleftrightarrow{AB}, m(\angle BCD) = 50^\circ,$

 \overrightarrow{CE} bisects $\angle DCA$ **Find :** $m(\angle ACE)$ 

2016 Exam (3) Question (5) (b)

5

In the opposite figure :

$\overleftrightarrow{AC} \cap \overleftrightarrow{DE} = \{B\}, m(\angle ABD) = 50^\circ$

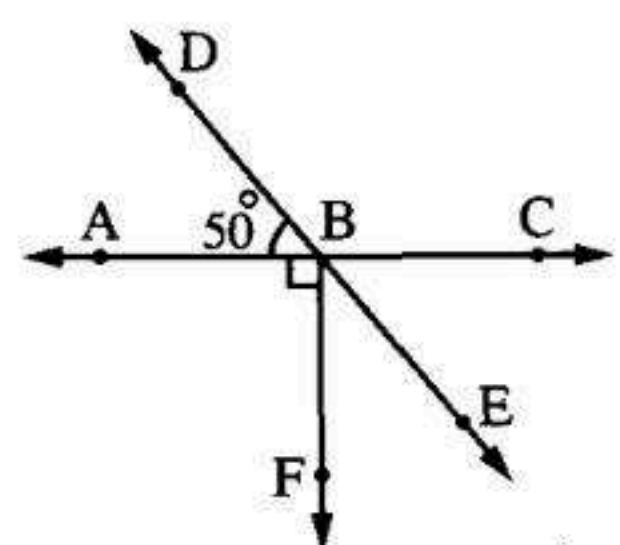
and $m(\angle ABF) = 90^\circ$

Find showing steps :

(1) $m(\angle DBC)$

(2) $m(\angle CBE)$

(3) $m(\angle FBE)$



2016 Exam (12) Question (3) (a)

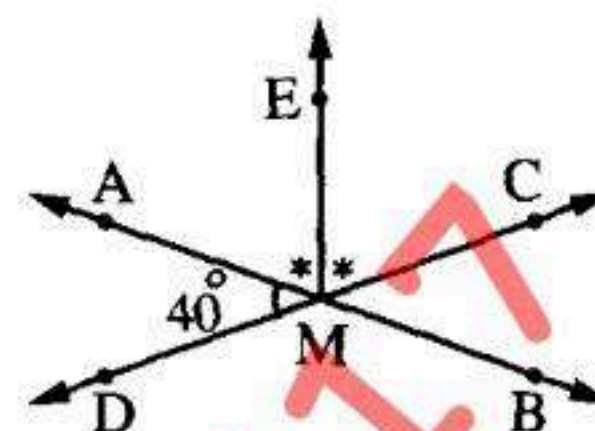
6

In the opposite figure :

$$\overleftrightarrow{AB} \cap \overleftrightarrow{DC} = \{M\}$$

, \overleftrightarrow{ME} bisects $\angle AMC$ and $m(\angle AMD) = 40^\circ$

Find : $m(\angle AME)$, $m(\angle BME)$



2016 Exam (8) Question (3) (a)

7

In the opposite figure :

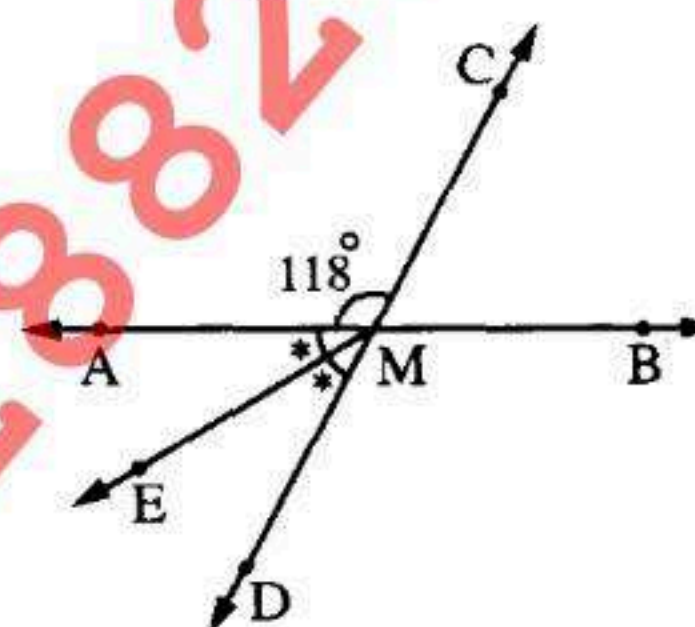
$$\overleftrightarrow{AB} \cap \overleftrightarrow{CD} = \{M\} , \overleftrightarrow{ME} \text{ bisects } \angle AMD$$

, $m(\angle AMC) = 118^\circ$ Find :

① $m(\angle BMD)$

② $m(\angle BMC)$

③ $m(\angle AME)$



2016 Exam (6) Question (3) (a)

8

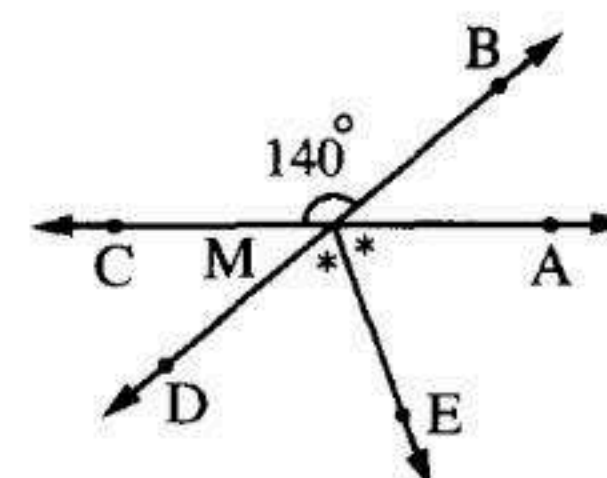
In the opposite figure :

$$\overleftrightarrow{AC} \cap \overleftrightarrow{BD} = \{M\} ,$$

$m(\angle CMB) = 140^\circ$,

\overleftrightarrow{ME} bisects $\angle AMD$

Find : ① $m(\angle AMB)$ ② $m(\angle AME)$



2016 Exam (1) Question (3) (b)

9

Mention two cases of congruency of two triangles.

2016 Exam (1) Question (4) (a)

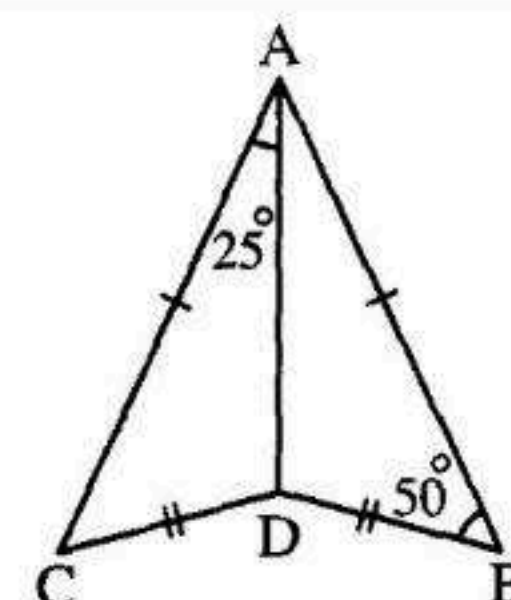
10

Complete from the opposite figure :

① The common side between the two triangles is

② $\triangle ABD \cong \triangle \dots\dots\dots$

③ $m(\angle ADB) = \dots\dots\dots^\circ$



2016 Exam (5) Question (4) (a)

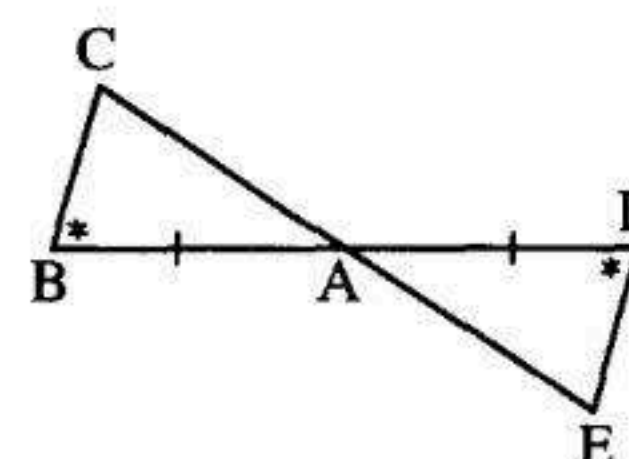
11

In the opposite figure :

$$\overleftrightarrow{EC} \cap \overleftrightarrow{BD} = \{A\} , AB = AD \text{ and}$$

$m(\angle ABC) = m(\angle ADE)$

Does $\triangle ADE \cong \triangle ABC$? Why ?



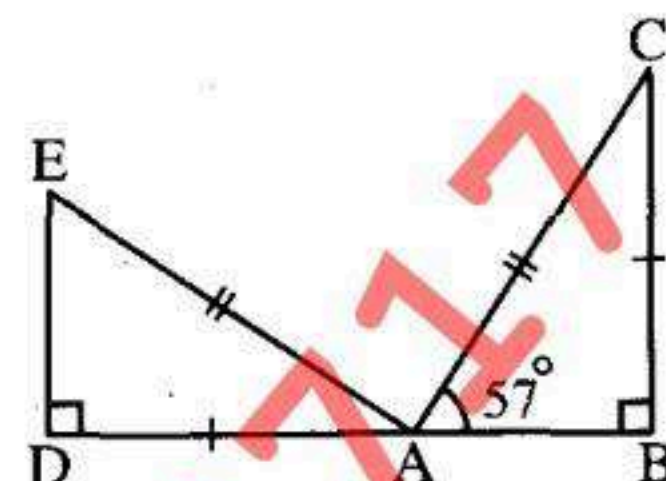
2016 Exam (13) Question (4) (b)

12

In the opposite figure :

Prove that : $\triangle ABC \equiv \triangle EDA$

, then find the measures of angles of $\triangle ADE$



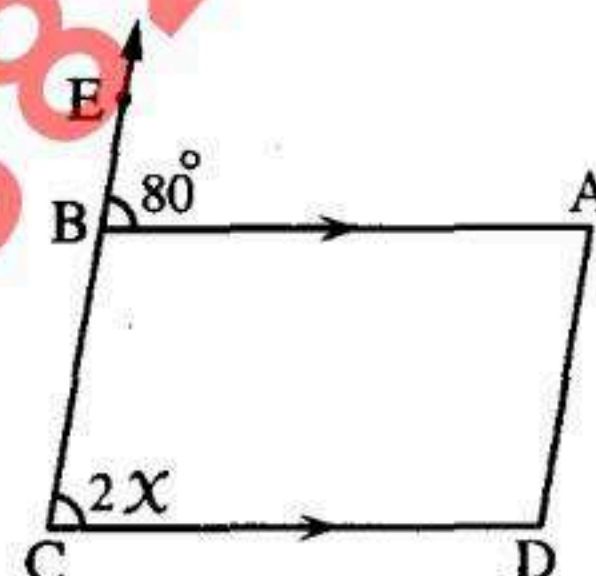
2016 Exam (3) Question (4) (a)

13

In the opposite figure :

$\overline{AB} \parallel \overline{DC}$

Find the value of : x



2016 Exam (14) Question (3) (b)

14

In the opposite figure :

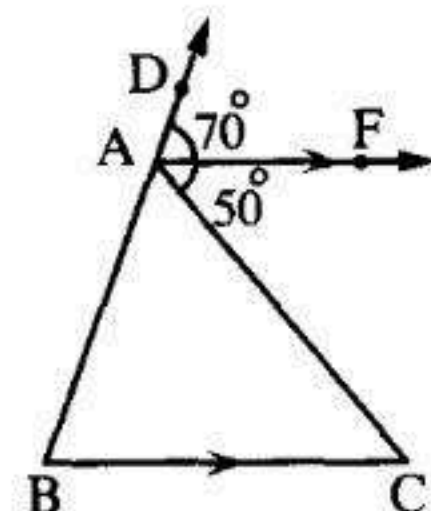
$\overline{AF} \parallel \overline{BC}$, $m(\angle DAF) = 70^\circ$, $m(\angle FAC) = 50^\circ$

Find :

(1) $m(\angle B)$

(2) $m(\angle C)$

(3) $m(\angle BAC)$



2016 Exam (6) Question (5) (a)

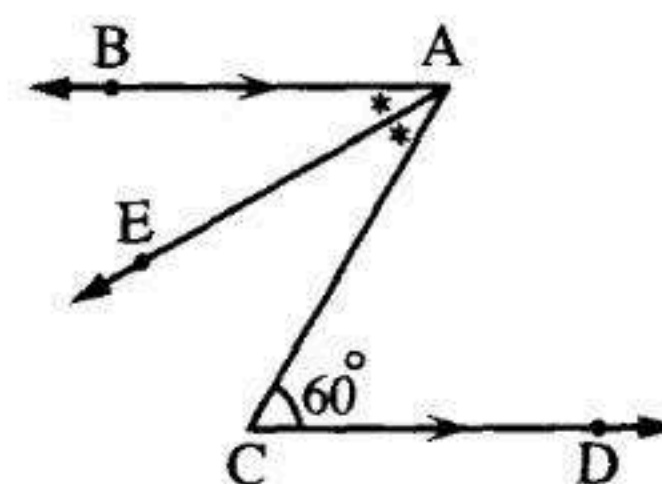
15

In the opposite figure :

$\overline{AB} \parallel \overline{CD}$, \overline{AE} bisects $\angle BAC$

, $m(\angle C) = 60^\circ$

Find : $m(\angle BAE)$



2016 Exam (8) Question (5) (a)

16

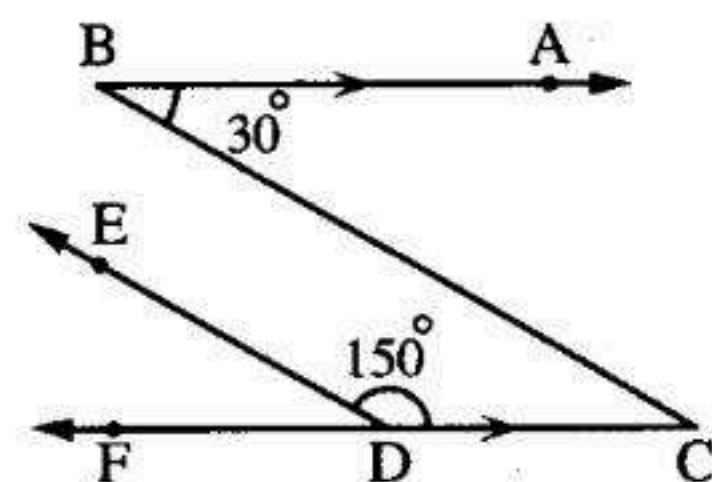
In the opposite figure :

$\overline{BA} \parallel \overline{CD}$, $m(\angle ABC) = 30^\circ$

, $m(\angle EDC) = 150^\circ$

Is $\overline{DE} \parallel \overline{CB}$? Why ?

(Write the steps of your answer)



2016 Exam (9) Question (5) (b)

17

Draw $\angle ABC$ whose measure is 60° and bisect it. (Don't remove the arcs)

2016 Exam (12) Question (4) (a)

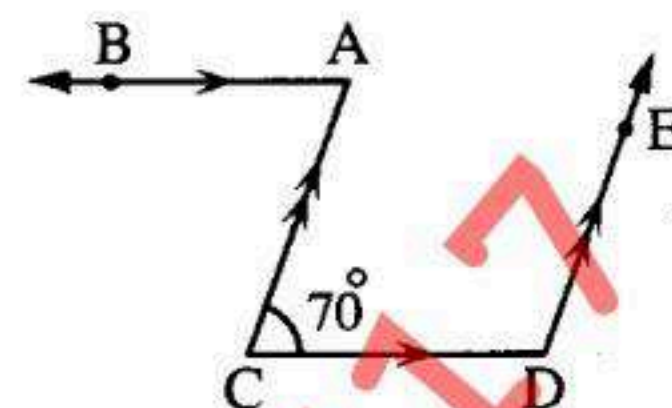
18

In the opposite figure :

$\overrightarrow{AB} \parallel \overrightarrow{DC}$, $\overrightarrow{CA} \parallel \overrightarrow{DE}$, $m(\angle C) = 70^\circ$

Find : (1) $m(\angle A)$ (give reason)

(2) $m(\angle D)$ (give reason)



2016 Exam (1) Question (5) (b)

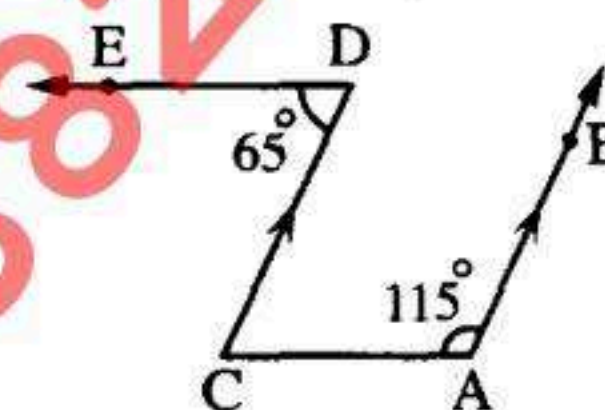
19

In the opposite figure :

$\overrightarrow{AB} \parallel \overrightarrow{CD}$, $m(\angle BAC) = 115^\circ$,

$m(\angle EDC) = 65^\circ$

Does $\overrightarrow{AC} \parallel \overrightarrow{DE}$? Why ?



2016 Exam (13) Question (5) (a)

20

In the opposite figure :

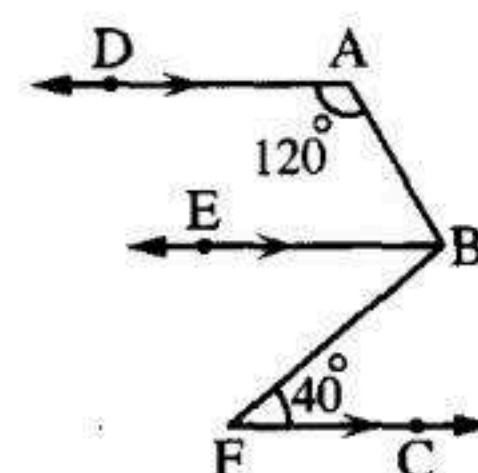
$\overrightarrow{AD} \parallel \overrightarrow{BE} \parallel \overrightarrow{FC}$, $m(\angle A) = 120^\circ$

, $m(\angle BFC) = 40^\circ$

Find : (1) $m(\angle ABE)$

(2) $m(\angle FBE)$

(3) $m(\angle ABF)$



2016 Exam (6) Question (4) (b)

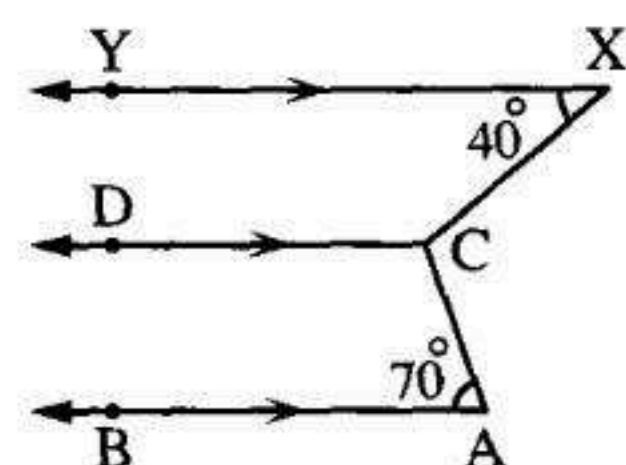
21

In the opposite figure :

$\overrightarrow{AB} \parallel \overrightarrow{CD} \parallel \overrightarrow{XY}$,

$m(\angle A) = 70^\circ$, $m(\angle X) = 40^\circ$

Find : $m(\angle ACX)$ and $m(\angle DCX)$



2016 Exam (7) Question (3) (b)

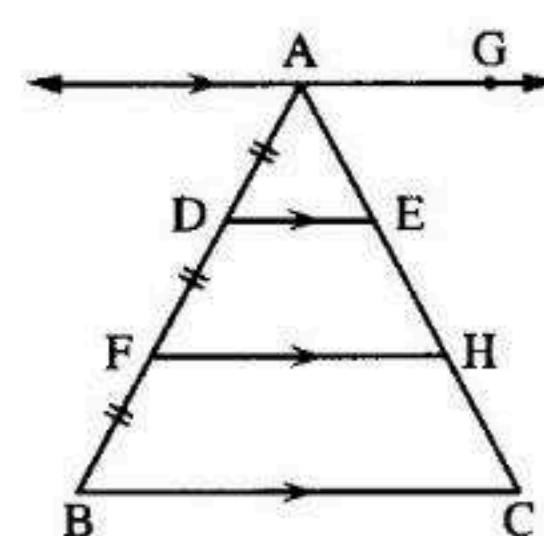
22

In the opposite figure :

$\overrightarrow{AG} \parallel \overrightarrow{DE} \parallel \overrightarrow{FH} \parallel \overrightarrow{BC}$ and $AC = 12$ cm.

If $AD = DF = FB$

, find the length of : \overline{AH}



2016 Exam (11) Question (5) (b)

23

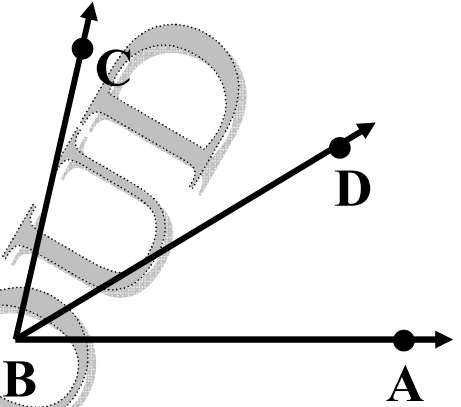
Draw \overline{AB} where $AB = 5$ cm. , using ruler and compasses draw the axis of symmetry of \overline{AB} (Do not remove the arcs).

2016 Exam (11) Question (3) (b)

Adjacent angles:

Two angles are said to be adjacent if they have a common vertex, a common side and the other two sides on opposite sides of this common side.

$\angle ABD$, $\angle DBC$ are adjacent angles



Complementary angles:

Two angles are said to be complementary if their sum is 90°

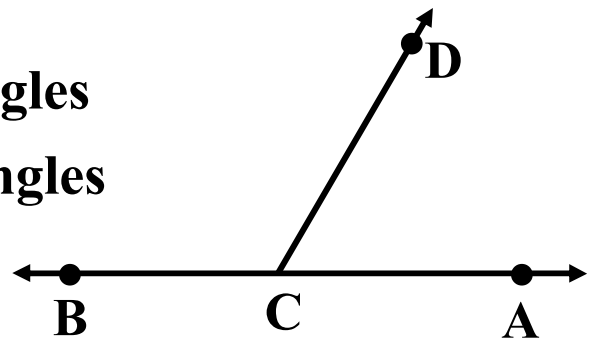
Supplementary angles:

Two angles are said to be supplementary if their sum is 180°

Remark: Two adjacent angles formed by a straight line and a ray with a starting point on this straight line are supplementary

$\angle ACD$, $\angle DCB$ are adjacent angles

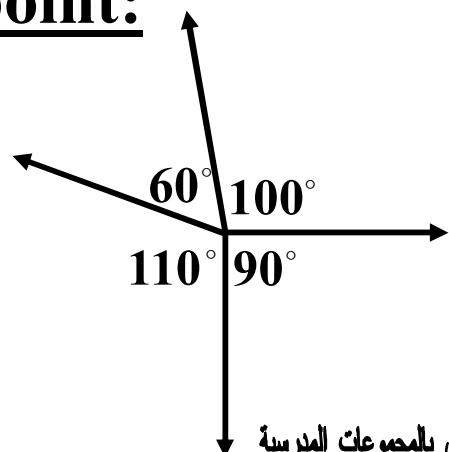
And they are supplementary angles



Accumulative angles at a point:

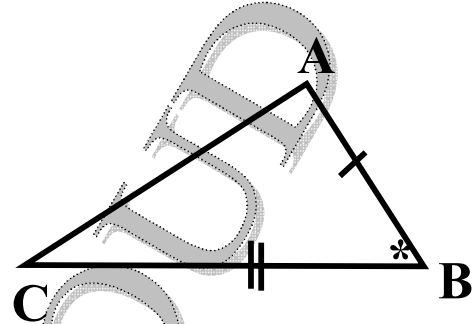
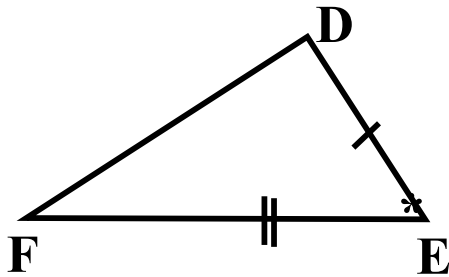
The sum of measures of the Accumulative angles

At a point is 360°



The first case for congruency (S.A.S)

Two triangles are congruent if two sides and the included angle of one are congruent with the corresponding parts of the other



If in the two triangles , ABC and DEF

$$\left\{ \begin{array}{l} \overline{AB} \equiv \overline{DE} \\ \overline{BC} \equiv \overline{EF} \\ \angle B \equiv \angle E \end{array} \right.$$

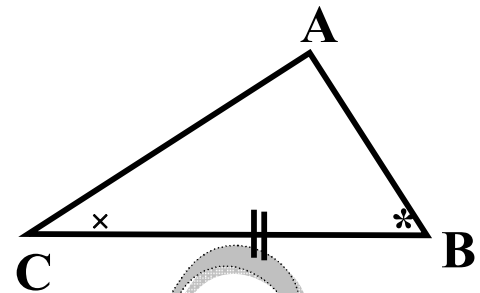
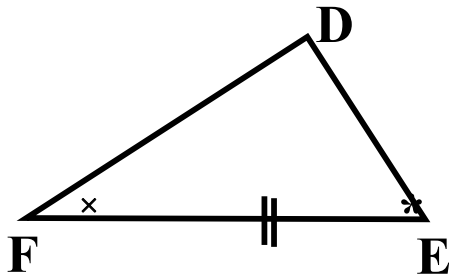
Then $\triangle ABC \equiv \triangle DEF$ and from congruency, we get
 $\overline{AC} \equiv \overline{DF}$, $\angle A \equiv \angle D$ and $\angle C \equiv \angle F$

The second case for congruency (S.A.A)

If the two angles and the side drawn between their vertices of one of the two triangles are congruent to the corresponding parts of the other triangle, then the two triangles are congruent.

If in the two triangles , ABC and DEF

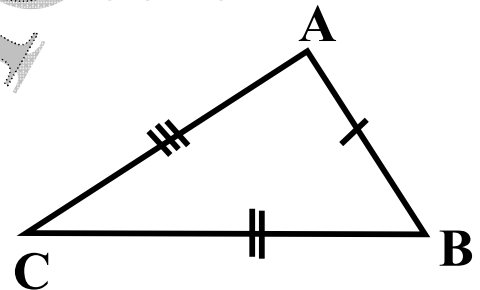
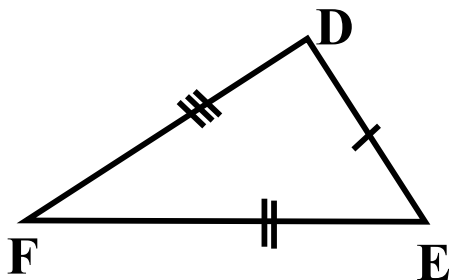
$$\left\{ \begin{array}{l} \overline{BC} \equiv \overline{EF} \\ \angle B \equiv \angle E \\ \angle C \equiv \angle F \end{array} \right.$$



Then $\triangle ABC \equiv \triangle DEF$ and from congruency, we get
 $\overline{AB} \equiv \overline{DE}$, $\overline{AC} \equiv \overline{DF}$ and $\angle A \equiv \angle D$

The third case for congruency (S.S.S)

Two triangles are congruent if each side of one triangle is congruent to its corresponding side of the other triangle.



If in the two triangles, $\triangle ABC$ and $\triangle DEF$

$$\left\{ \begin{array}{l} \overline{AB} \equiv \overline{DE} \\ \overline{AC} \equiv \overline{DF} \\ \overline{BC} \equiv \overline{EF} \end{array} \right.$$

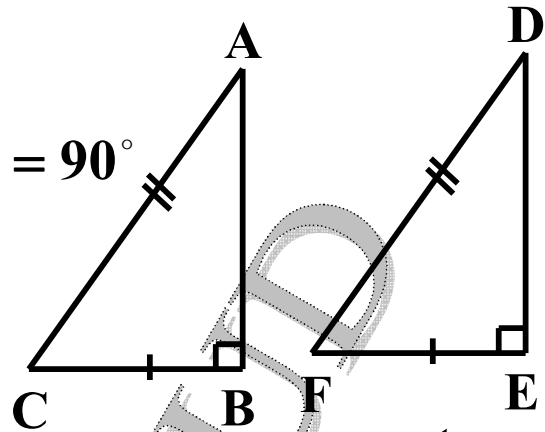
Then $\triangle ABC \equiv \triangle DEF$ and from congruency, we get
 $\angle A \equiv \angle D$, $\angle B \equiv \angle E$ and $\angle C \equiv \angle F$

The fourth case for congruency.

Two right-angled triangles are congruent, if the hypotenuse and one side of one triangle are congruent to their corresponding parts of the other triangle.

If in the two triangles, $\triangle ABC$ and $\triangle DEF$

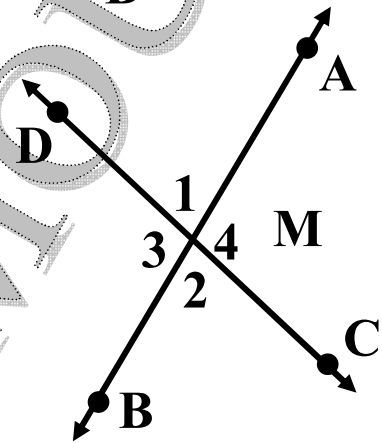
$$\left\{ \begin{array}{l} \overline{AC} \equiv \overline{DF} \\ \overline{BC} \equiv \overline{EF} \\ m(\angle B) = m(\angle E) = 90^\circ \end{array} \right.$$



V.O.A.

$$m(\angle 1) = m(\angle 2)$$

$$m(\angle 3) = m(\angle 4)$$



Then $\triangle ABC \equiv \triangle DEF$ and from congruency, we get $\overline{AB} \equiv \overline{DE}$, $\angle A \equiv \angle D$ and $\angle C \equiv \angle F$

Parallel straight lines:

Corresponding angles:

$$m(\angle 1) = m(\angle 2), m(\angle 3) = m(\angle 4)$$

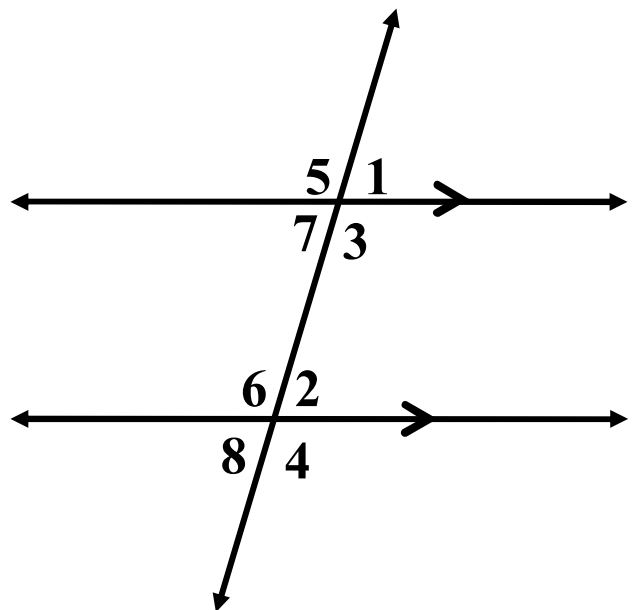
$$m(\angle 5) = m(\angle 6), m(\angle 7) = m(\angle 8)$$

Alternate angles:

$$m(\angle 3) = m(\angle 6), m(\angle 2) = m(\angle 7)$$

Interior supplementary

Angles:



$$m(\angle 3) + m(\angle 2) = 180^\circ, m(\angle 7) + m(\angle 6) = 180^\circ$$

[1] Complete:

- 1) The sum of measures of the accumulative angles at a point =
- 2) The angle whose measure is 72° complements the angle whose measure is
- 3) If $\triangle ABC \equiv \triangle XYZ$ and $m(\angle X) = 50^\circ$, $m(\angle B) = 60^\circ$ then $m(\angle Z) = \dots\dots\dots$
- 4) The diagonal of the rectangle divides its surface into two triangles.
- 5) The angle of measure is $\left(52\frac{2}{5}\right)^\circ$ is supplemented by the angle of measure
- 6) If $\triangle ABC \equiv \triangle XYZ$ and $m(\angle A) + m(\angle B) = 130^\circ$, then $m(\angle Z) = \dots\dots\dots$
- 7) If $m(\angle A) = 150^\circ$, then $m(\text{reflex } \angle A) = \dots\dots\dots$

8) The two adjacent complementary angles , their terminal sides are

9) If a line segment is extended from one side without limit, the produced figure is

10) If $\angle A$ supplements $\angle B$, $\angle A \equiv \angle B$, then $m(\angle B) = \dots\dots\dots$

.....

11) The measure of the straight angle =

12) In the right-angled triangle , the area of the square set up the hypotenuse equals

.....

13) If one of the two supplement angles is acute then the other is angle.

14) The two triangles are congruent if two sides and in one of them are

congruent to their corresponding elements in the other.

15) If $m(\angle A) = 170^\circ$, then $m(\text{reflex } \angle A) = \dots\dots\dots$

16) $\dots\dots\dots < \text{the measure of the obtuse angle} < \dots\dots\dots$

17) If $\triangle XYZ$ is right-angled at X , $XY = 12 \text{ cm}$, $XZ = 9 \text{ cm}$.
then $(YZ)^2 = \dots\dots\dots \text{cm}^2$.

18) The required condition for the two straight lines are parallel is $\dots\dots\dots$

19) If $\triangle ABC \equiv \triangle XYZ$ then $BC = \dots\dots\dots$

20) If $\angle A$ supplements $\angle B$, and $m(\angle A) = 2 m(\angle B)$,
then $m(\angle B) = \dots\dots\dots$

21) The angle of measure is $89^\circ 60'$ is $\dots\dots\dots$ angle.

22) The number of edges which are parallel to one edge of a cube is $\dots\dots\dots$

23) If $\overline{AB} \equiv \overline{XY}$, then $AB - XY = \dots\dots\dots$

24) The sum of measures of the two complementary angles =

25) The angle of measure is x° complements the angle of measure is

26) If ABC is a triangle in which $AB = 5\text{ cm}$, $BC = 12\text{ cm}$ and $AC = 13\text{ cm}$ then $m(\angle \dots) = 90^\circ$

27) The two right-angled triangles are congruent if in one of them are congruent with their corresponding elements in the other triangle.

28) The angle whose measure $47^\circ 30'$ is complemented the angle whose measure

29) The sum of measures of the two supplementary angles equals

30) If $m(\angle X) = \frac{1}{2}m(\angle Y)$ and $m(\angle X) = 30^\circ$, then the two angles X and Y are

31) In the right-angled triangle , the area of the square set up the hypotenuse equals

32) The two straight lines which are parallel to a third straight line are

33) If $m(\angle X) = 2m(\angle Y)$ and Y is obtuse angle, then $\angle X$ is

34) If $\triangle ABC \cong \triangle XYZ$ and $m(\angle X) + m(\angle Z) = 140^\circ$, then $m(\angle B) = \dots$

35) The two adjacent angles formed by intersecting a straight line and a ray whose start point lies on the straight line are

36) In $\triangle ABC$: if $(AB)^2 - (BC)^2 = (AC)^2$, then $m(\angle \dots) = 90^\circ$

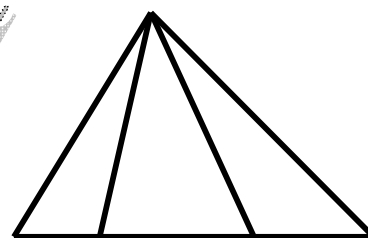
37) If $m(\angle A) = 50^\circ$, $\angle A$ complements $\angle B$, $\angle B$ supplements $\angle C$, then $m(\angle C) = \dots$

38) A rectangle of length 4 cm. and width 3 cm , then the area of the square set its diagonal equals cm^2

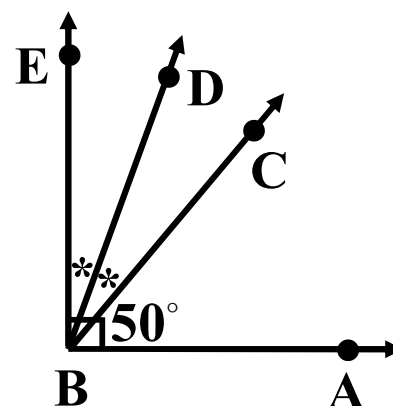
39) If the lengths of the two sides of the right angle in the right-angled triangle are 5 cm. and 6 cm. then the area of the square set up the hypotenuse =cm²

40) If $m(\angle X) = \frac{1}{2} m(\angle Y)$ and $m(\angle X) = 60^\circ$, then the two angles X and Y are

41) The number of triangles in the opposite figure is



42) In the opposite figure:

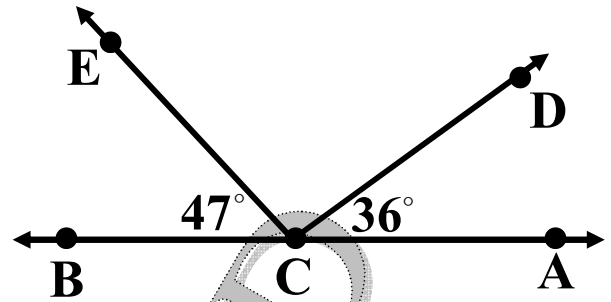


If $m(\angle ABC) = 50^\circ$, BD bisects $\angle CBE$

$\overrightarrow{BD} \perp \overrightarrow{BE}$, then $m(\angle CBD) = \dots\dots\dots$

43) In the opposite figure:

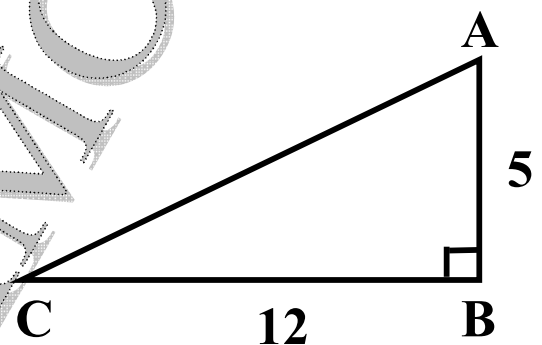
$m(\angle DCE) = \dots\dots\dots$



44) In the opposite figure:

ABC is a right-angled triangle

at B then $(AC)^2 = \dots\dots \text{cm}^2$.



45) In the opposite figure:

If $\triangle ABC$ is

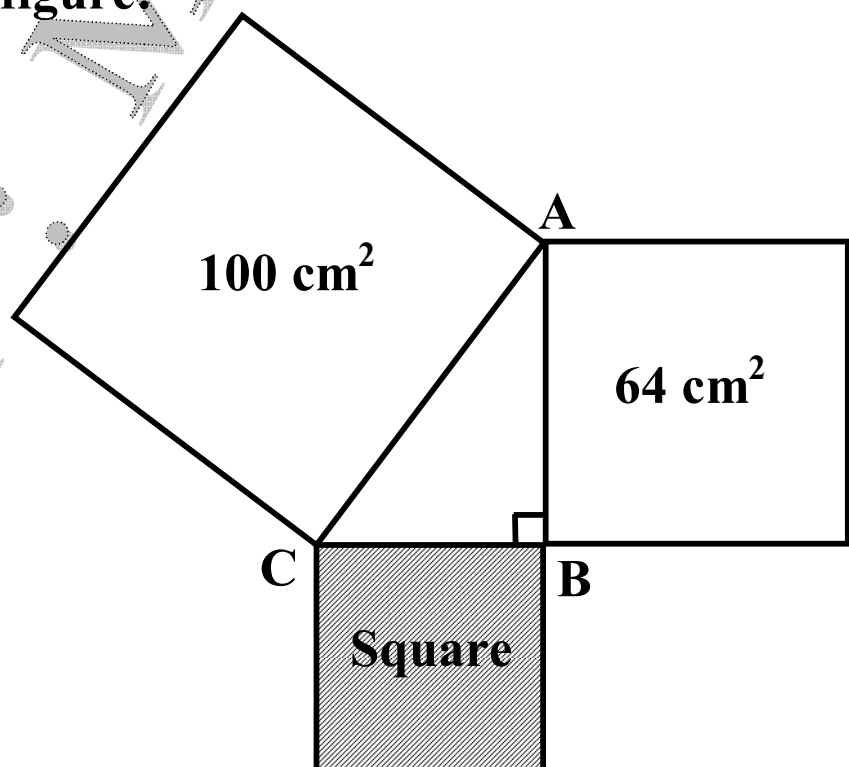
right-angled

at B then the

area of the

shaded square

equals $\dots\dots \text{cm}^2$.



46) In the opposite figure:

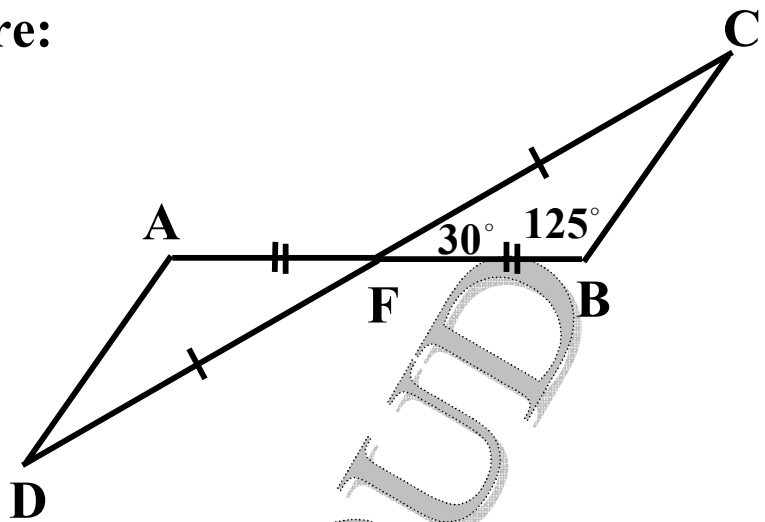
If $\overline{AB} \cap \overline{CD} = \{F\}$

$FC = FD, FA = FB$

$m(\angle CFB) = 30^\circ$

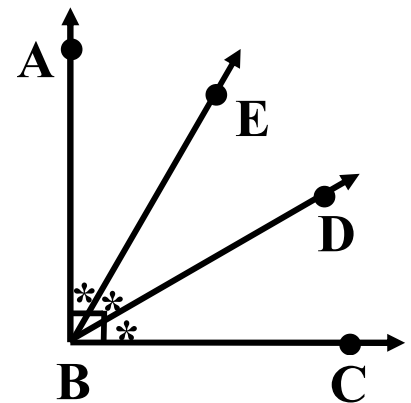
and $m(\angle B) = 125^\circ$

then $m(\angle D) = \dots$



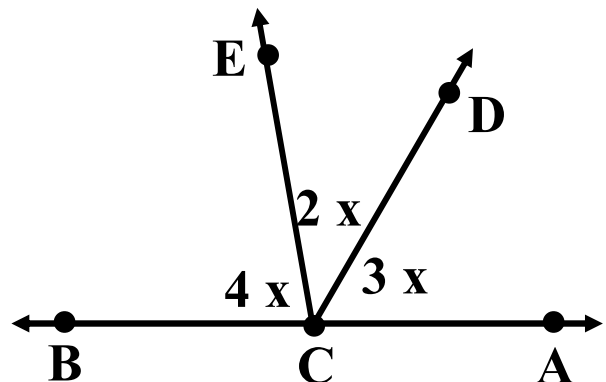
47) In the opposite figure:

If $\overrightarrow{BA} \perp \overrightarrow{BC}$, then $m(\angle CBE) = \dots\dots$



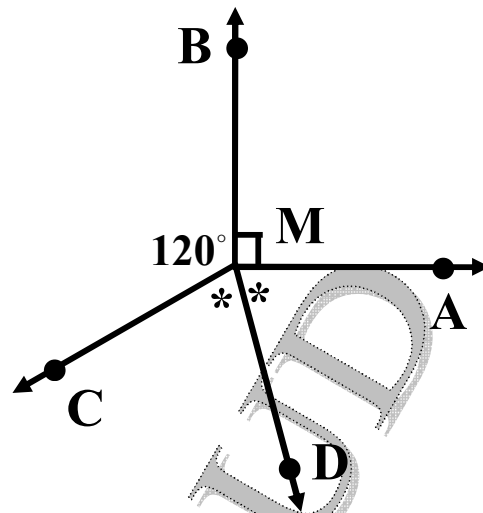
48) In the opposite figure:

If $A \in \overline{BC}$, then $x = \dots\dots$



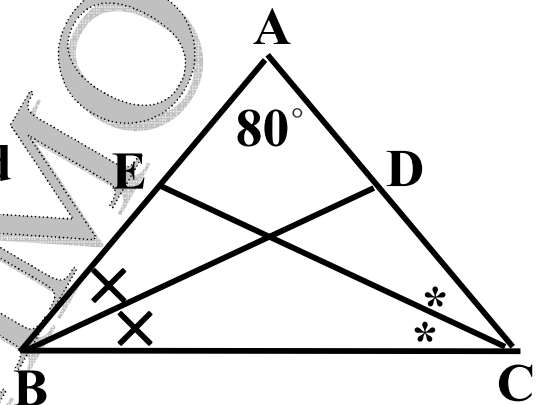
49) In the opposite figure:

\overrightarrow{MD} bisects $\angle AMC$,
then $m(\angle AMD) = \dots$

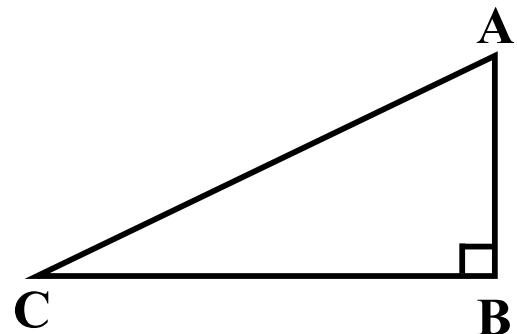


50) In the opposite figure:

$m(\angle A) = 80^\circ$, \overrightarrow{BD} bisects $\angle B$ and
 \overrightarrow{CE} bisects $\angle C$,
then $m(\angle CFB) = \dots\dots\dots$

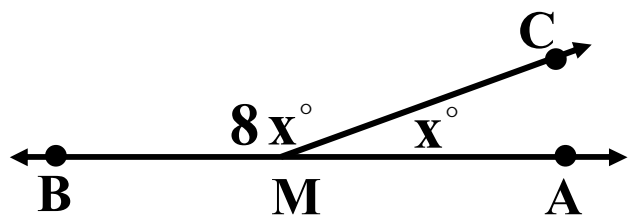


51) The hypotenuse in the
opposite triangle is



52) In the opposite figure:

If $M \in \overline{AB}$, then $x = \dots\dots\dots$



53) If $\triangle XYZ$ is

right-angled

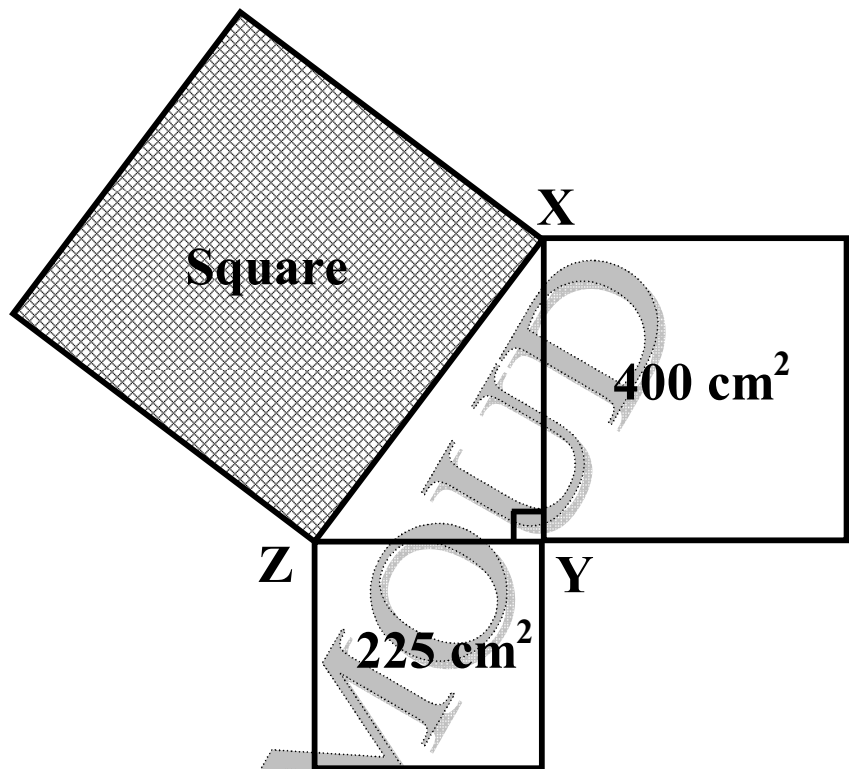
triangle at

Y , then

the area of

shaded square

$= \dots \text{cm}^2$



54) In the opposite figure:

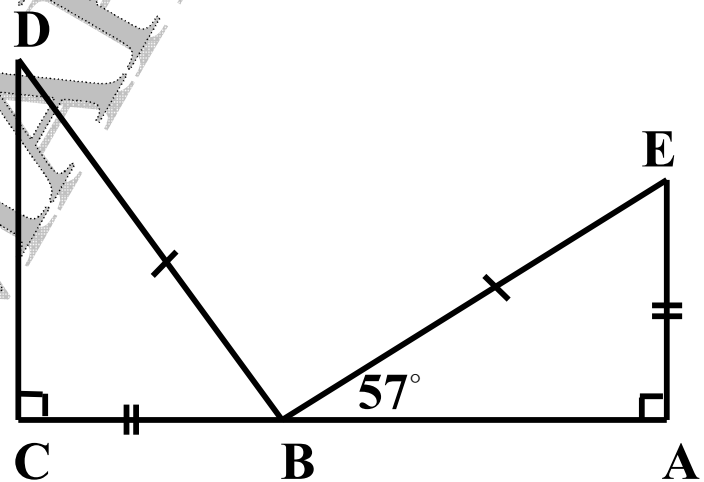
$B \in \overleftrightarrow{AC}, AE = BC$

$BE = BD, m(\angle A)$

$= m(\angle C) = 90^\circ,$

$m(\angle EBA) = 57^\circ$

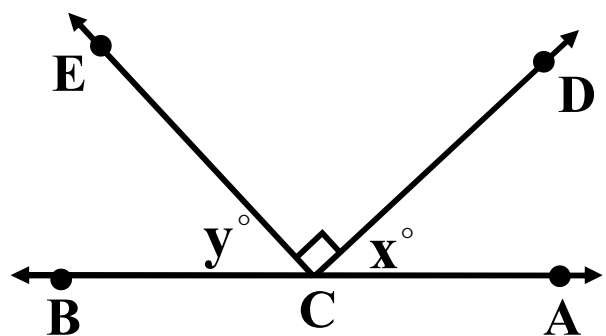
then $m(\angle EBD) = \dots$



55) In the opposite figure:

If $C \in \overleftrightarrow{AB}$

then $x^\circ + y^\circ = \dots$

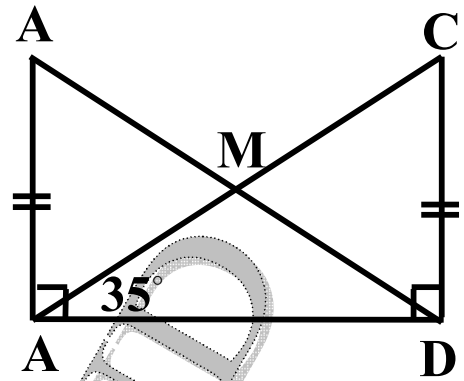


56) In the opposite figure:

If $AB = CD$, $m(\angle CBD) = 35^\circ$

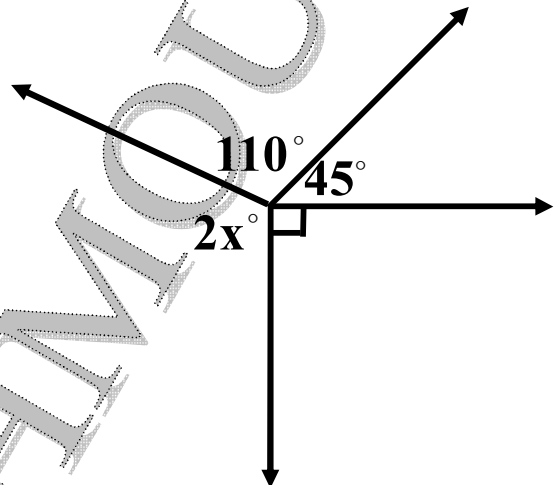
$\overline{AB} \perp \overline{DB}$ and $\overline{CD} \perp \overline{DB}$

then $m(\angle DMB) = \dots\dots$



57) In the opposite figure:

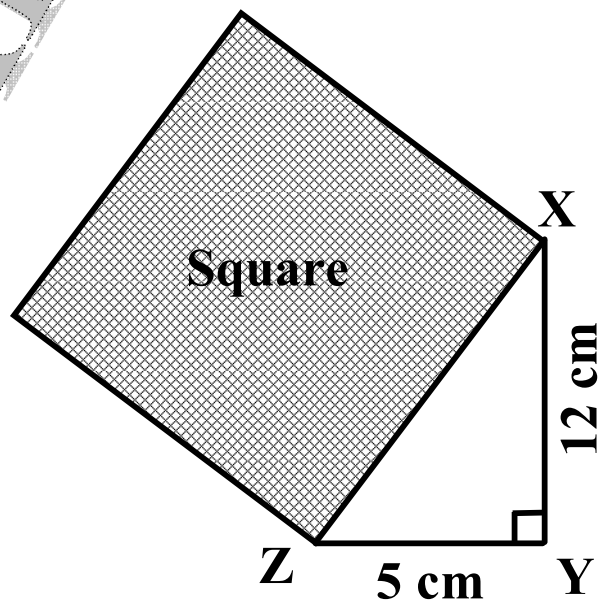
$x = \dots$



58) In the opposite figure:

The area of the shaded

square = $\dots\dots\text{cm}^2$.

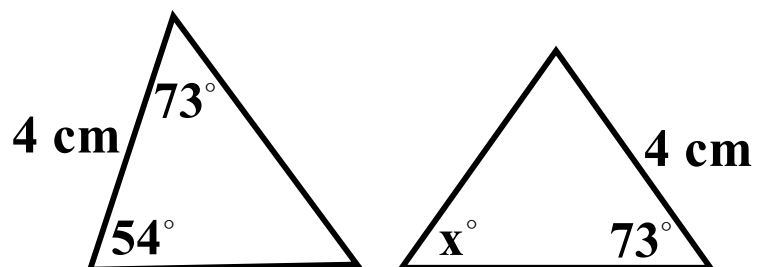


59) In the opposite figure:

If the two triangles

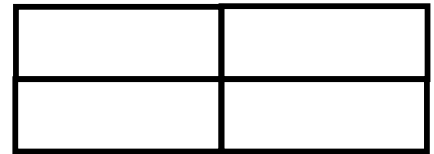
are congruent

then $x = \dots$



60) The number of rectangles

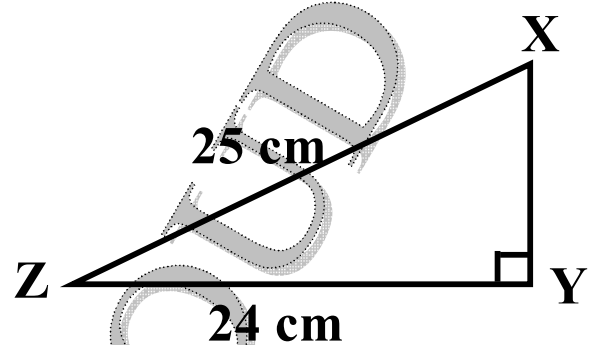
in the opposite figure =



61) In the opposite figure:

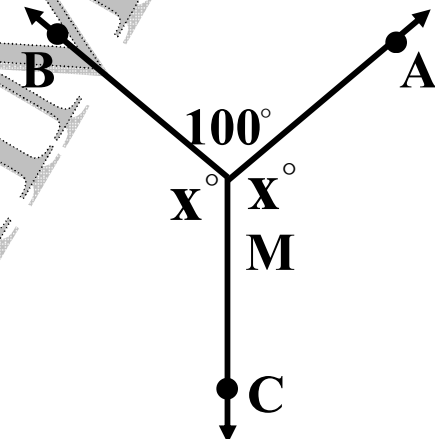
If XYZ is a right-angled triangle at Y

then $(XY)^2 = \dots\dots\dots \text{cm}^2$.



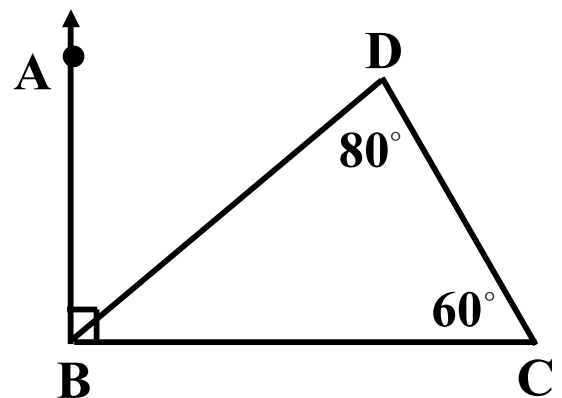
62) In the opposite figure:

If $m(\angle AMB) = 100^\circ$, then $x = \dots\dots$

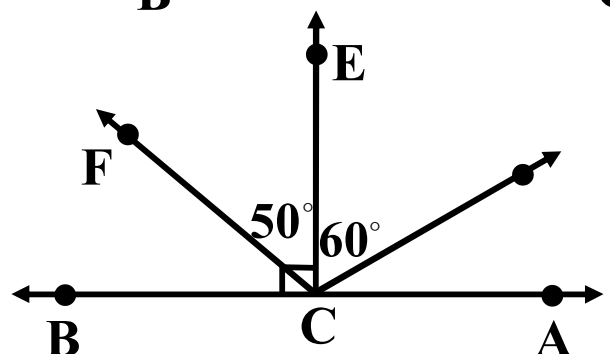


63) In the opposite figure:

If $\overrightarrow{BA} \perp \overrightarrow{BC}$, then $m(\angle ABD) = \dots\dots\dots$

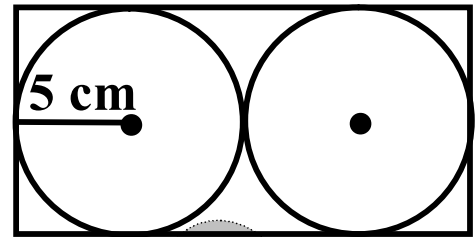


64) The number of obtuse angle in the opposite figure is



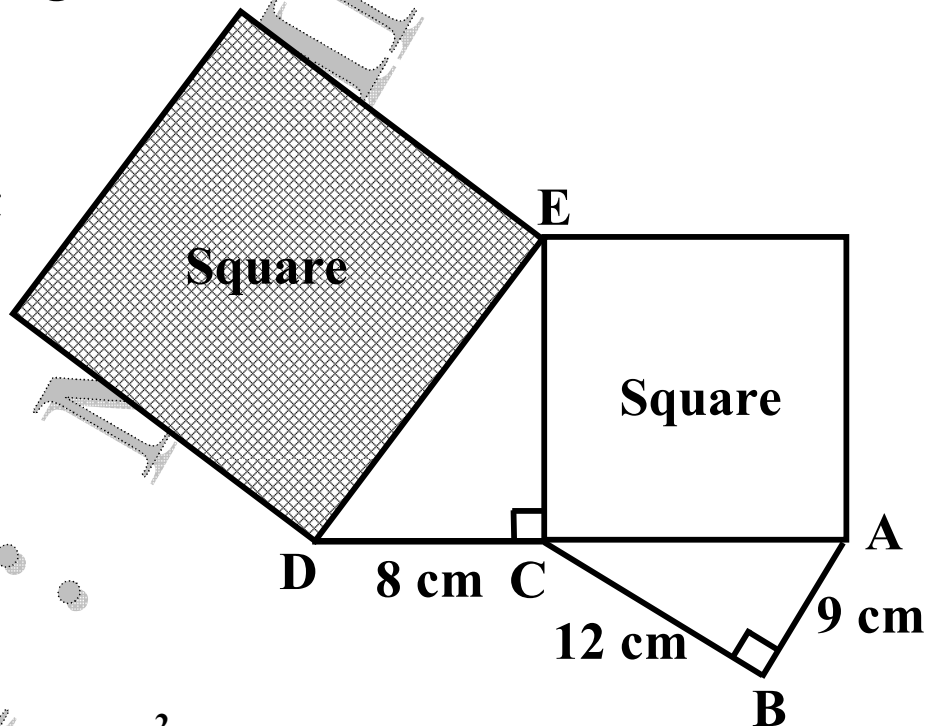
65) In the opposite figure:

Two circles are drawn inside a rectangle M and N each of them is of radius 5 cm long , then the area of rectangle = cm^2 .



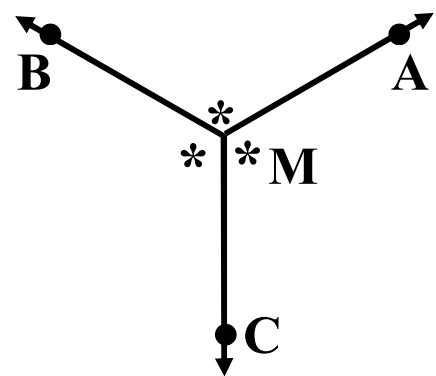
66) In the opposite figure:

If $\triangle ABC$ is right-angled at B and $\triangle ECD$ is Right-angled at C, then the area of the shaded square = cm^2 .



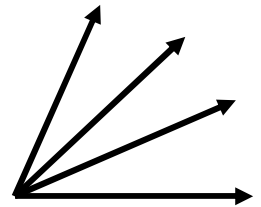
67) In the opposite figure:

$m(\angle AMC) = \dots\dots^\circ$



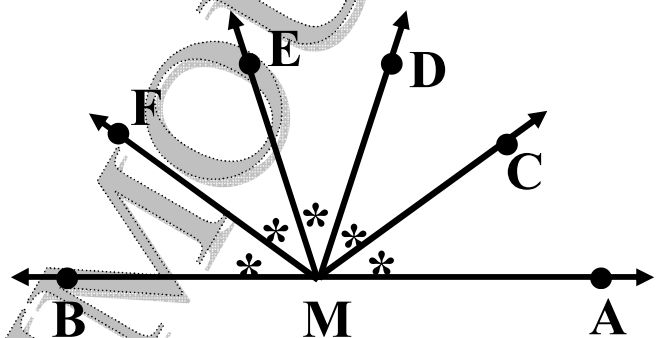
68) In the opposite figure:

The number of the acute angles
in the opposite figure is



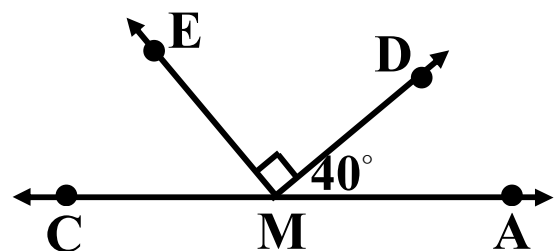
69) In the opposite figure:

If $M \in \overleftrightarrow{AB}$, then
 $m(\angle AMC) = \dots\dots$



70) In the opposite figure:

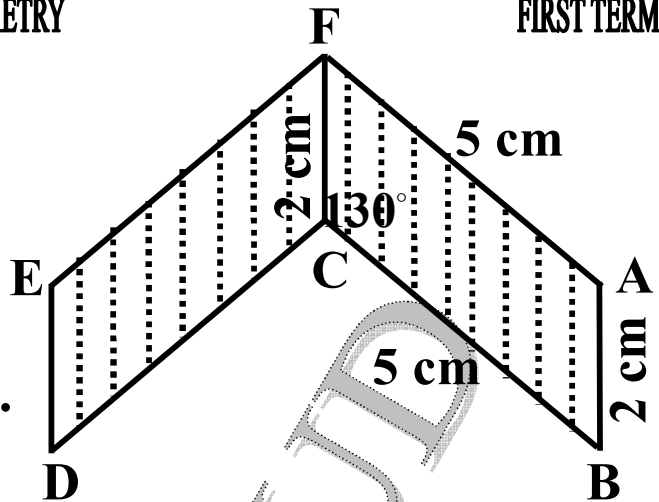
If $M \in \overleftrightarrow{AC}$, then
 $m(\angle EMC) = \dots\dots$



71) In the opposite figure:

If the figure $ABCF \equiv$
the figure $EDCF$, then

- a) The perimeter of the
shaded figure = cm.
b) $m(\angle BCD) = \dots\dots\dots$



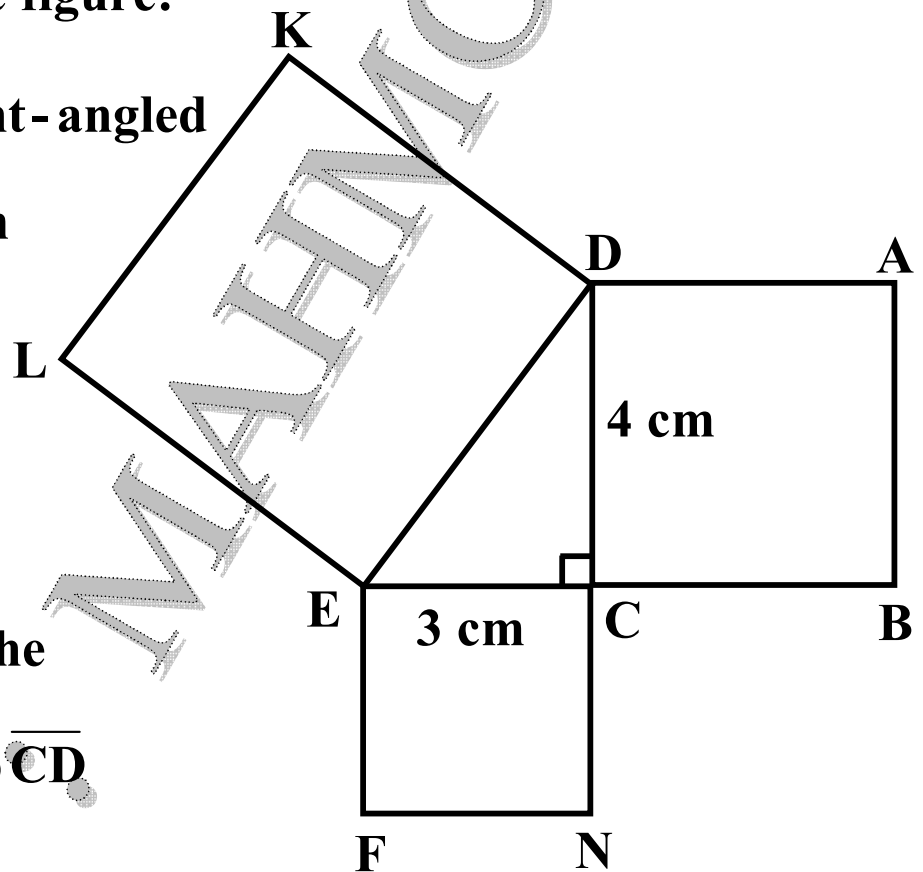
72) In the opposite figure:

If $\triangle CDE$ is right-angled
at C, $CD = 4$ cm

$CE = 3$ cm.

Complete
the following

- a) The area of the
square set up \overline{CD}
= cm^2 .
b) The area of the square
set up $\overline{DE} = \dots\dots\text{cm}^2$.
c) The area of all figure = cm^2 .



73) In the opposite figure:

If $AB = AD$, $BC = 6$ cm.

$m(\angle BAC) = m(\angle DAC) = 35^\circ$

$m(\angle B) = 25^\circ$ Complete

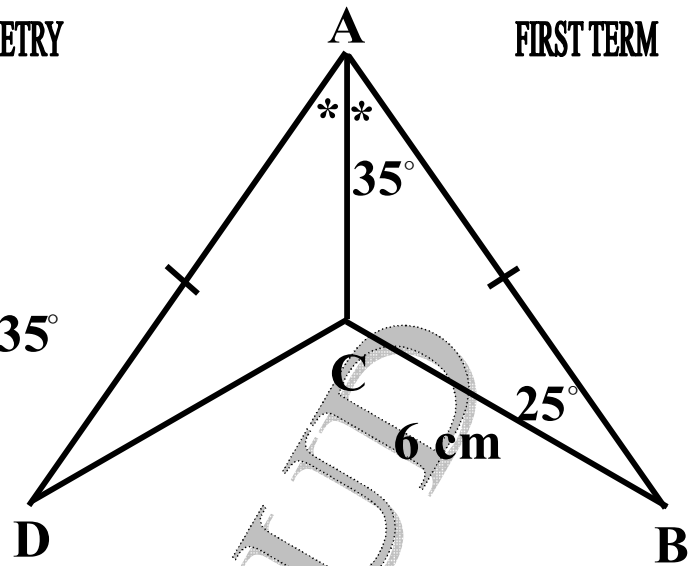
the following:

a) $\triangle ACB \equiv \dots\dots$

b) $m(\angle D) = \dots\dots$

c) $CD = \dots\dots$ cm

d) $m(\angle ACD) = \dots\dots$



74) In the opposite figure:

If $D \in \overleftrightarrow{CE}$, $\overline{BC} \perp \overline{CD}$

the figure $ABCD \equiv$ the

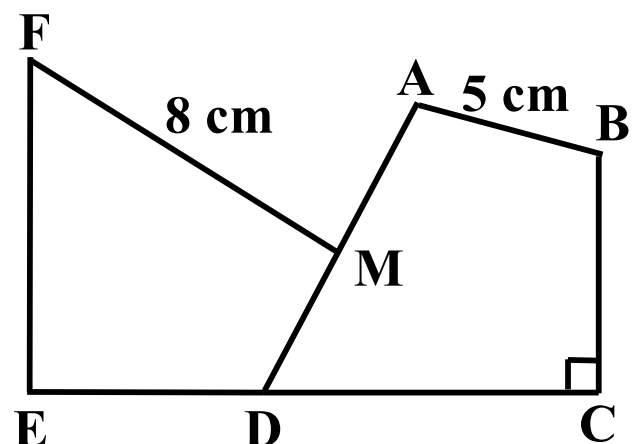
figure $MDEF$ complete

the following:

a) $m(\angle B) = m(\angle \dots\dots)$

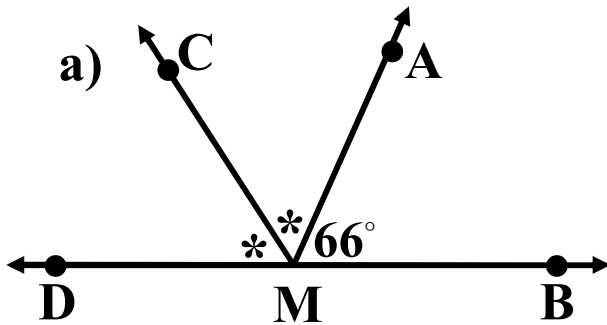
b) $m(\angle B) + m(\angle F) = \dots\dots$

c) $AM = \dots\dots$ cm.



75) Find the measure of the required angle under each

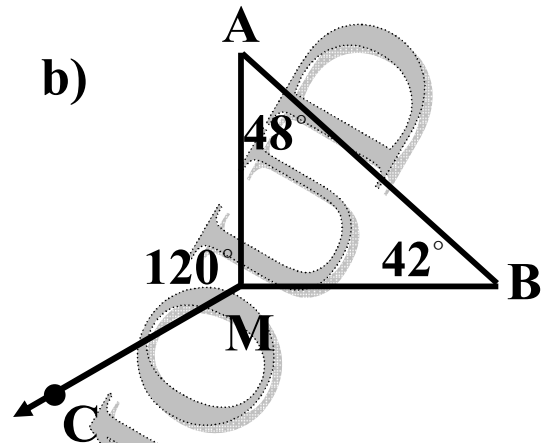
figure:



If $M \in \overleftrightarrow{BD}$, \overrightarrow{MC} bisects

$\angle AMD$, then

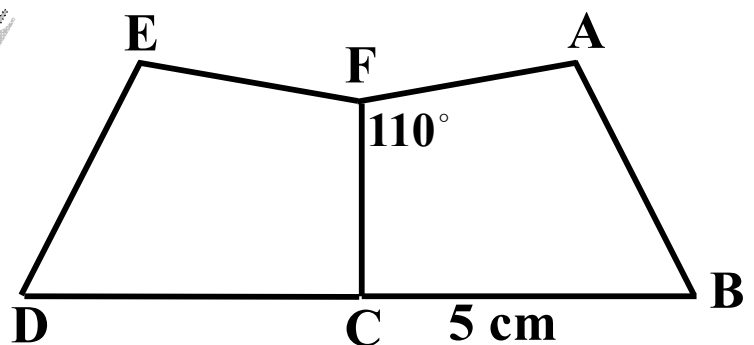
$m(\angle AMC) = \dots\dots$



$m(\angle BMC) = \dots\dots$

76) In the opposite figure:

If $C \in \overleftrightarrow{BD}$,
 $m(\angle AFC) = 110^\circ$



$BC = 5 \text{ cm}$. and the polygon $ABCF \cong$ the polygon $EDCF$

Complete the following :

a) \overline{CF} is side.

b) $BD = \dots\dots\dots$ cm.

c) $m(\angle FCD) = \dots\dots\dots$

d) $m(\angle AFE) = \dots\dots\dots$

77) In the opposite figure:

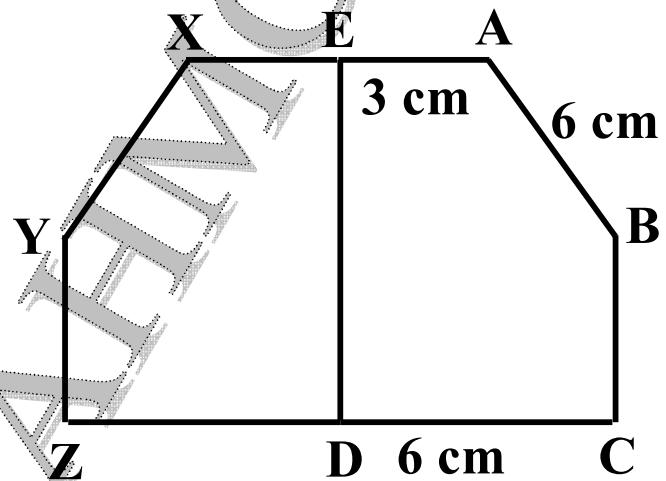
If $D \in \overleftrightarrow{CZ}$, the figure

$ABCDE \equiv$ the figure

$XYZDE$, $AE = 3$ cm

$BC = 4$ cm and

$AB = CD = 6$ cm.



Complete the following:

a) $XY = \dots\dots\dots$ cm.

b) $YZ = \dots\dots\dots$ cm.

c) $m(\angle EDC) = \dots\dots\dots$

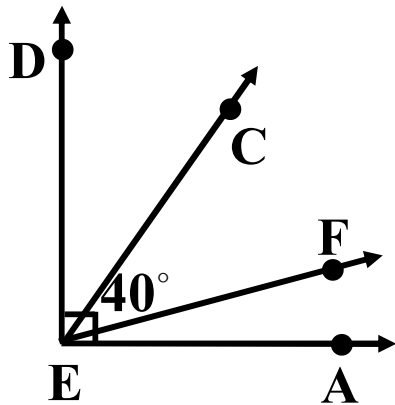
d) $CZ = \dots\dots\dots$ cm.

e) The perimeter of the figure $ABCZYX = \dots\dots\dots$ cm.

78) Find the measure of the required angle under each

figure:

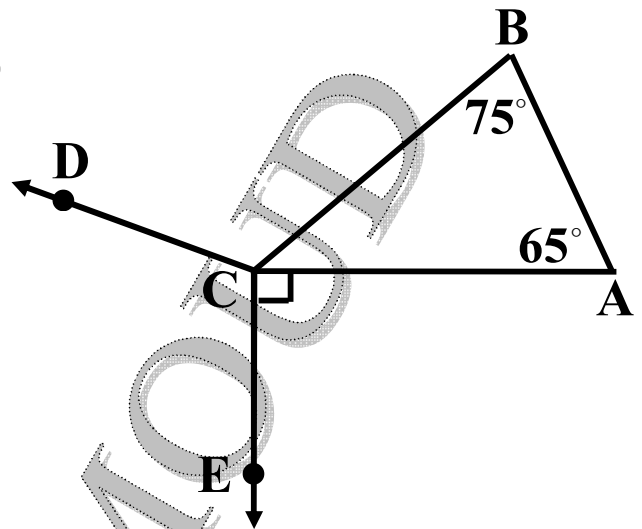
a)



If $\overrightarrow{EA} \perp \overrightarrow{ED}$

then $m(\angle AEF) = \dots\dots$

b)



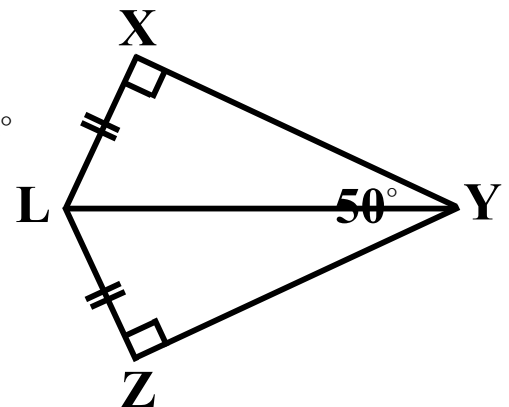
$m(\angle ECD) = \dots\dots$

79) In the opposite figure:

If $LZ = LX$, $m(\angle Z) = m(\angle X) = 90^\circ$

and $m(\angle XYZ) = 50^\circ$

Complete the following:



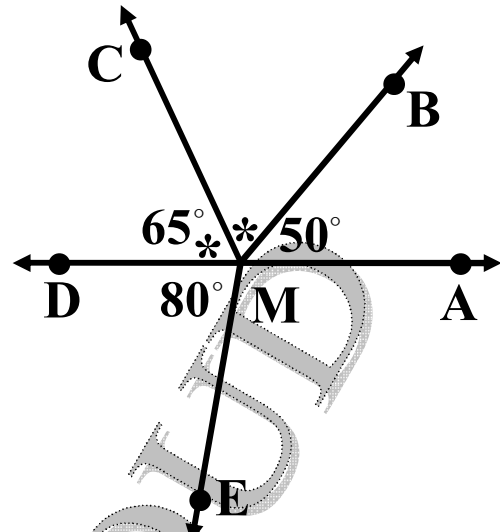
a) $\triangle XYL \equiv \triangle \dots\dots$

b) $YZ = \dots\dots$

c) $m(\angle XLY) = m(\angle \dots\dots\dots) = \dots\dots$

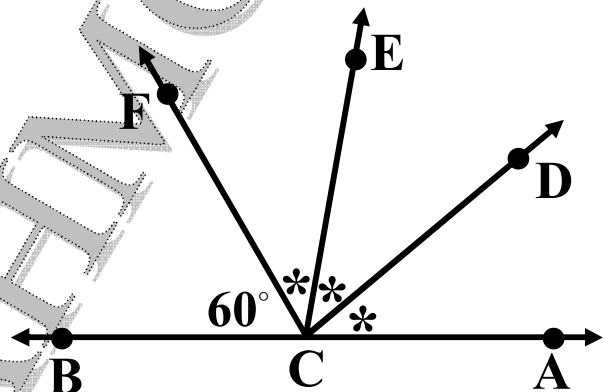
80) Find the measure of the
required angle:

If \overrightarrow{MC} bisects $\angle BMD$
then $m(\angle AME) = \dots\dots\dots$



81) Find the measure of the
required angle:

If $C \in \overleftrightarrow{AB}$ then
 $m(\angle DCB) = \dots\dots\dots$



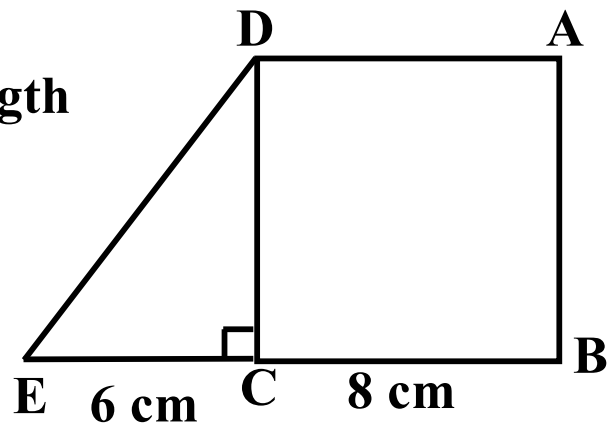
82) In the opposite figure:

ABCD is a square of side length

8 cm. and $E \in \overrightarrow{BC}$ such that
 $CE = 6 \text{ cm.}$

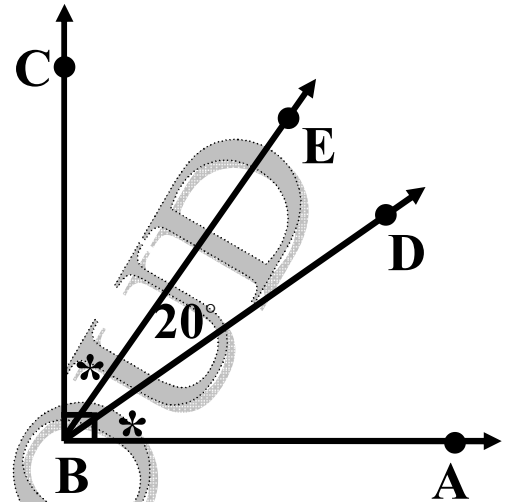
a) The area of $\triangle DCE$
 $= \dots\dots\dots \text{cm}^2.$

b) The area of the square set up $\overline{DE} = \dots\dots\dots \text{cm}^2.$



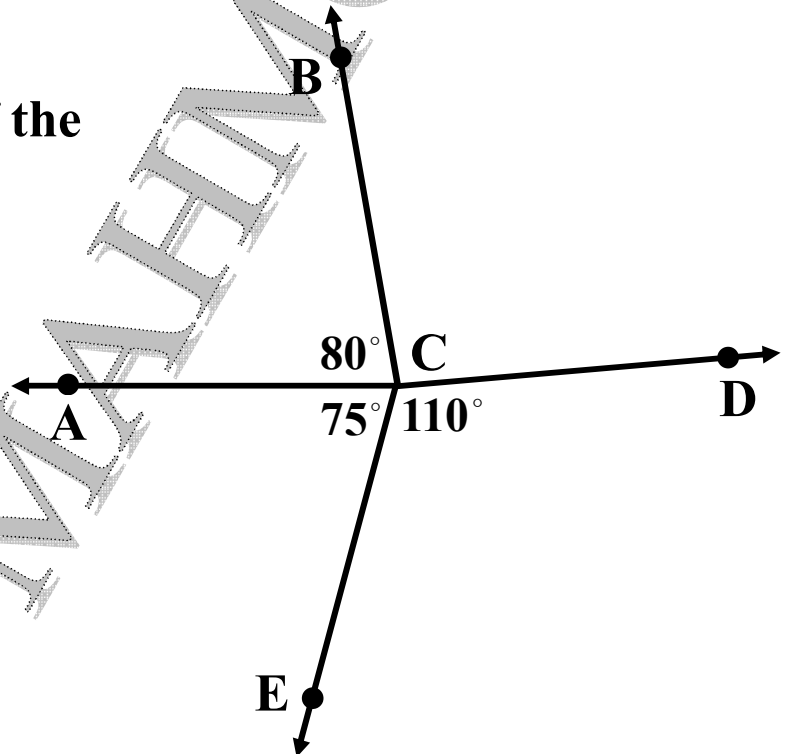
83) Find the measure of the required angle:

If $\overrightarrow{BA} \perp \overrightarrow{BC}$
then $m(\angle ABD) = \dots$



84) Find the measure of the
required angle

$m(\angle BCD) = \dots$



[2]

1) In the opposite figure:

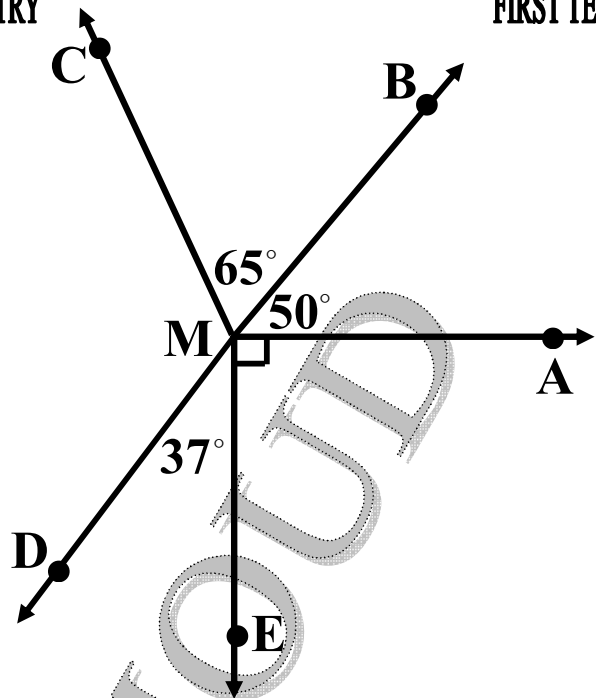
If $m(\angle AMB) = 50^\circ$

$m(\angle BMC) = 65^\circ$

$m(\angle EMD) = 37^\circ$

and $\overrightarrow{MA} \perp \overrightarrow{ME}$

Find: $m(\angle CMD)$



.....

.....

.....

2) In each of the following figures show if the two

triangles are congruent or not. If they are congruent

name the case of congruency and state the results

obtained. If they are not give reasons given that the

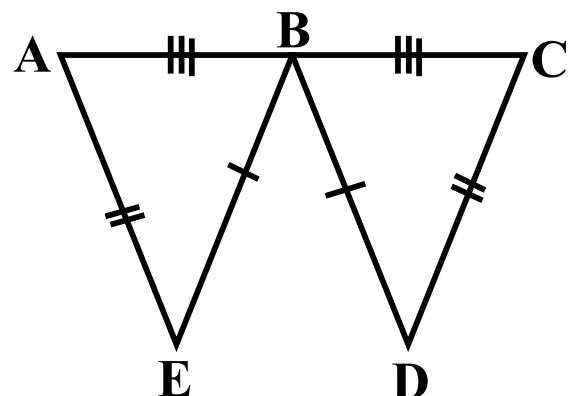
similar signs denote to congruence of the labeled

elements by them.

.....

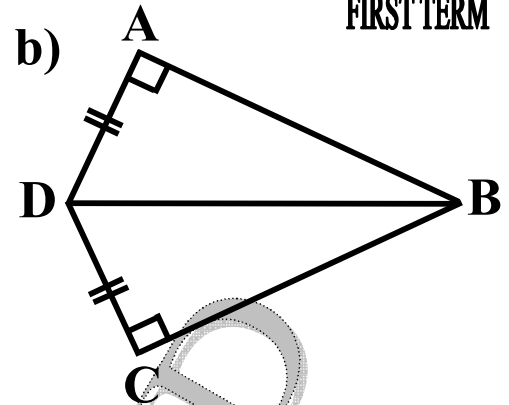
.....

a)



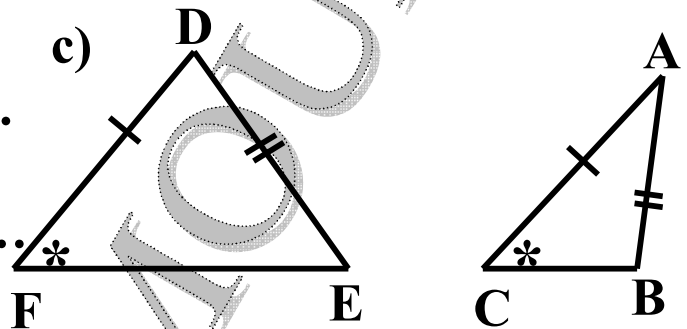
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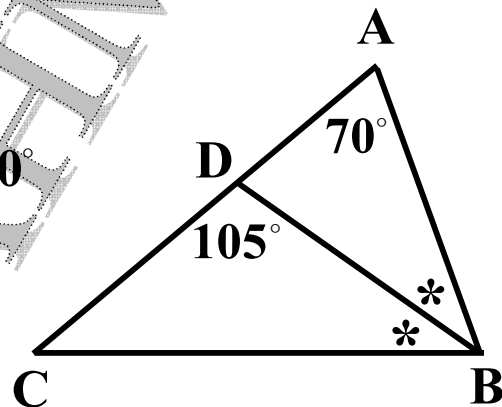
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3) In the opposite figure:

\overrightarrow{BD} bisects $\angle ABC$, $m(\angle A) = 70^\circ$
and $m(\angle CBD) = 105^\circ$
Find: $m(\angle C)$



.....

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4) In the opposite figure:

If $m(\angle AMB) = m(\angle BMC) = m(\angle DME)$, $\overrightarrow{MA} \perp \overrightarrow{MF}$

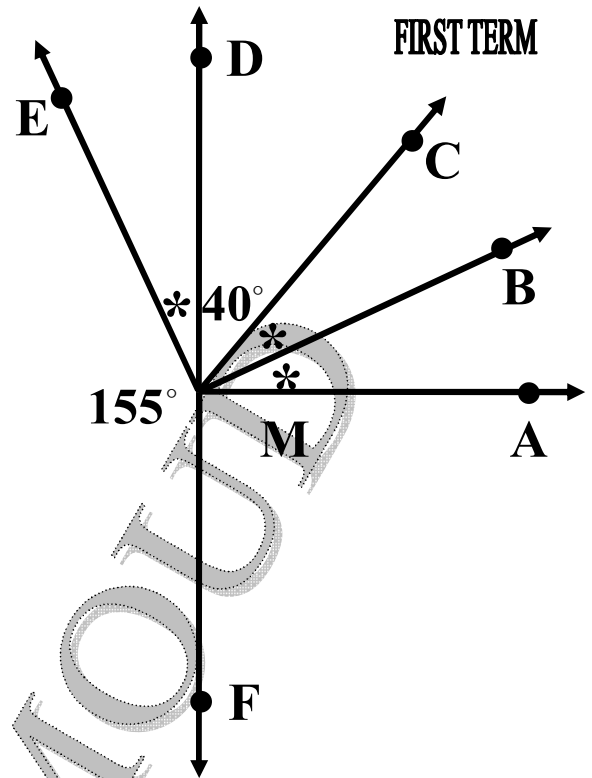
$m(\angle EMF) = 155^\circ$ and $m(\angle CMD) = 40^\circ$. find: $m(\angle AMB)$

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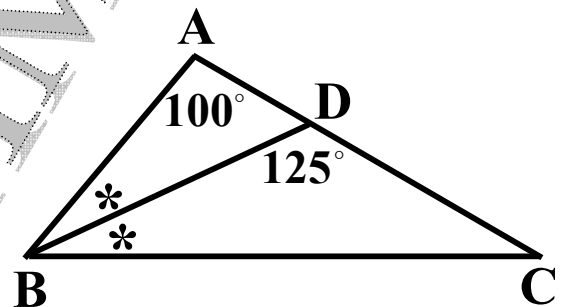
5) In the opposite figure:

\overrightarrow{BD} bisects $\angle CBA$

$m(\angle CDB) = 125^\circ$

$m(\angle A) = 100^\circ$

Find: $m(\angle C)$



.....

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6) In the opposite figure:

$AB = BC$, $DA = DC$, $m(\angle ABD) = 40^\circ$,

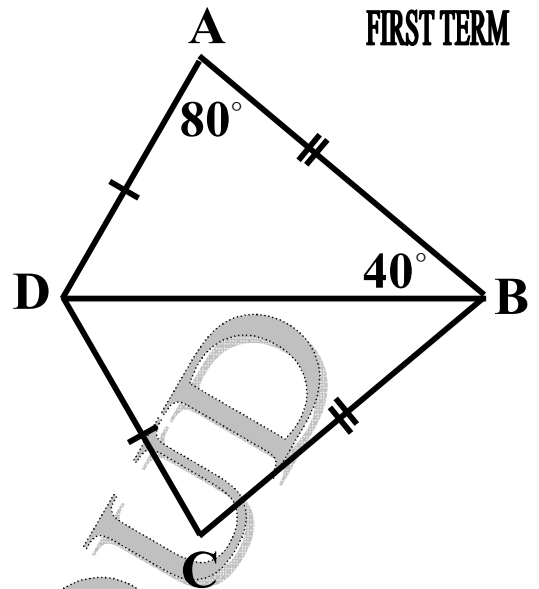
$m(\angle BAD) = 80^\circ$ find: $m(\angle ADC)$

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7) In the opposite figure:

If \overrightarrow{FE} bisects $\angle AFD$, find $m(\angle AFE)$

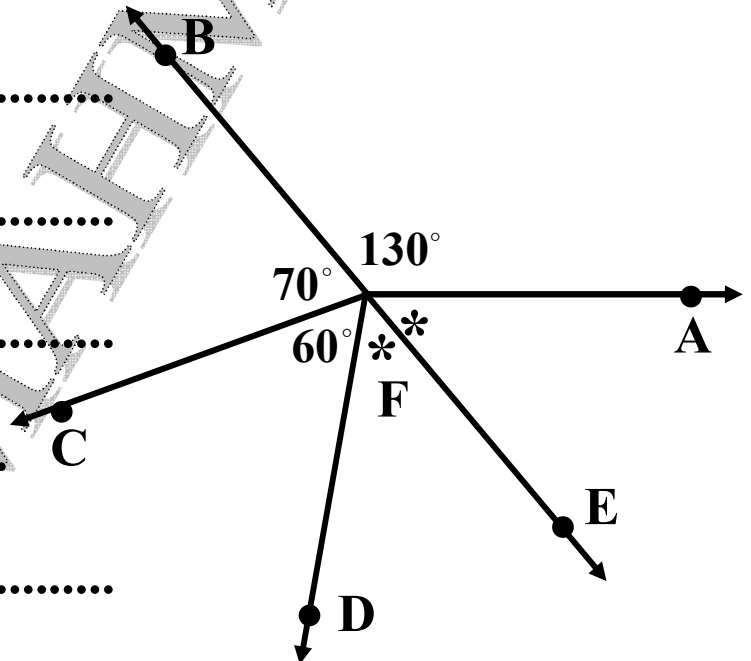
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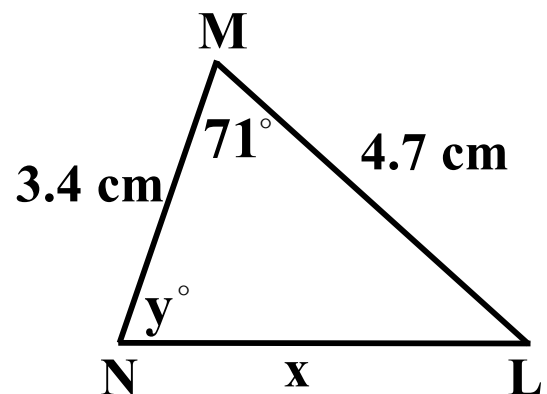
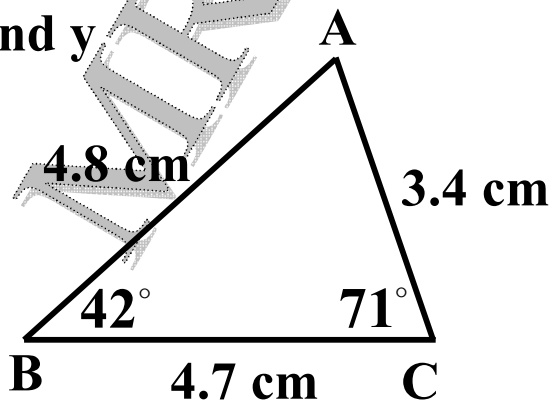
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8) Study the following two figures, then find the value of

x and y



9) In the opposite figure:

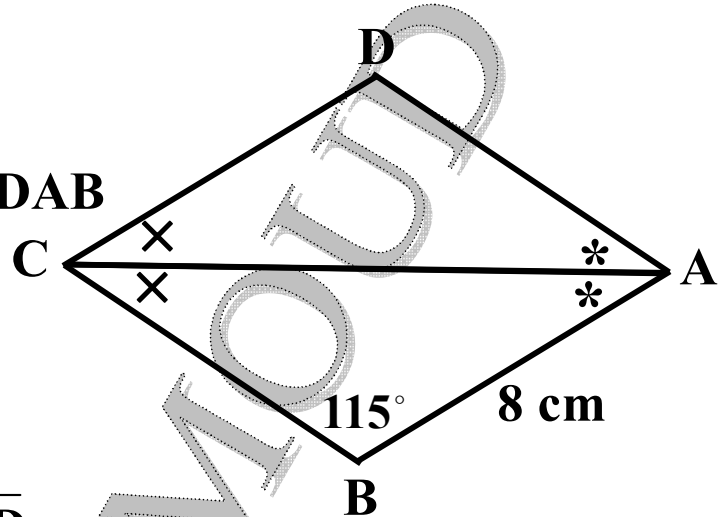
\overleftrightarrow{AC} bisects $\angle DCB$ and $\angle DAB$

$m(\angle B) = 115^\circ$ and

$AB = 8 \text{ cm}$.

Find : a) $m(\angle D)$

b) The length of \overline{AD}



10) In each of the following figures show if the two

triangles are congruent or not. If they are

congruent name the case of congruency and the

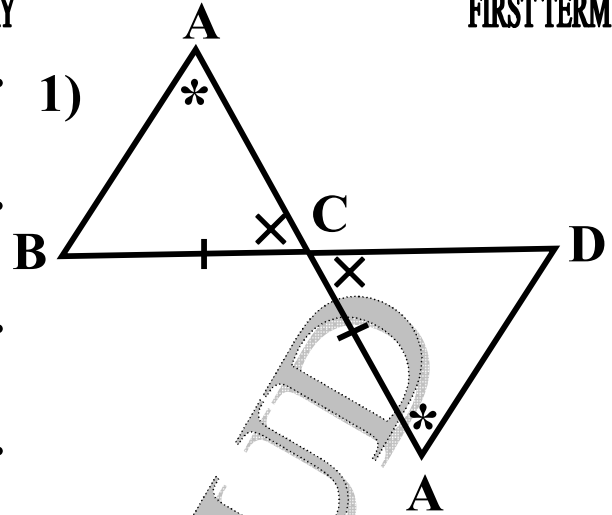
results of the congruency and if they are not

congruent give the reason. (given that : the similar

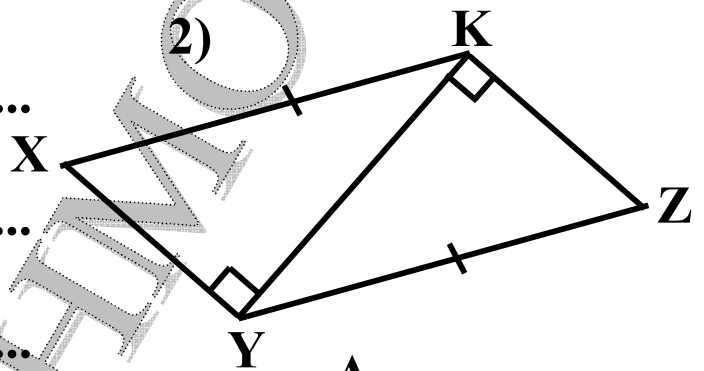
signs denote to congruency of labeled elements by

these signs)

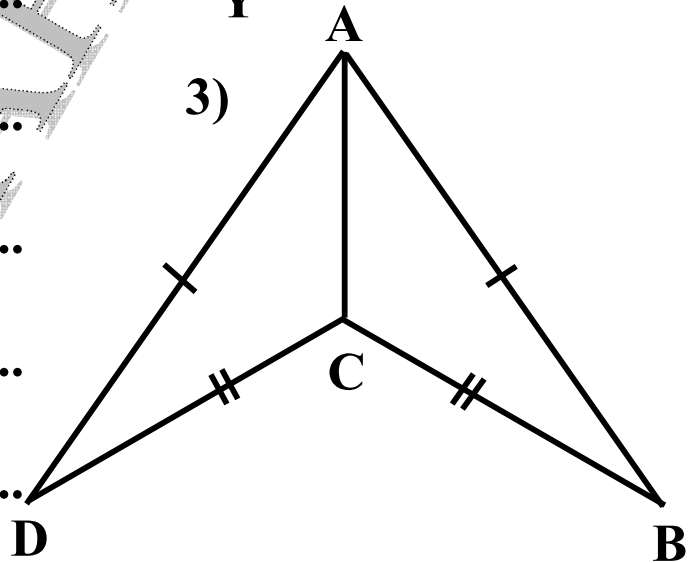
1)



2)



3)



11) In the opposite figure:

If $m(\angle AMB) = m(\angle BMC) = m(\angle CMD) = m(\angle DME)$

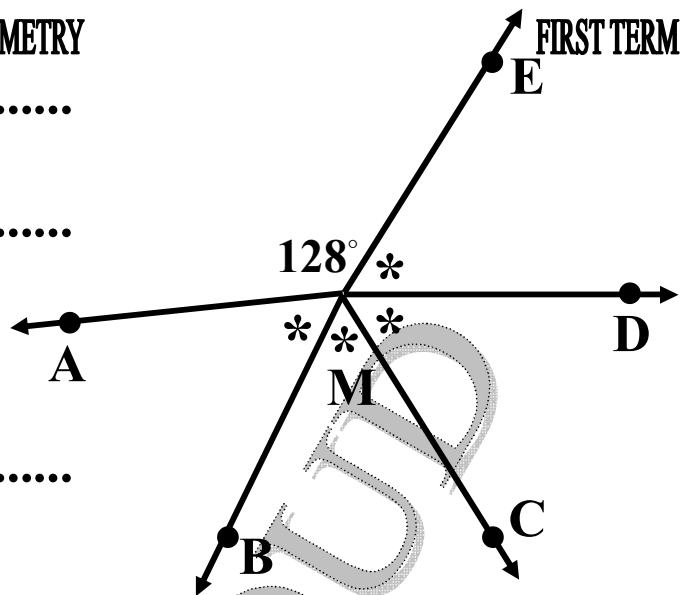
and $m(\angle EMA) = 128^\circ$. find: $m(\angle BMC)$

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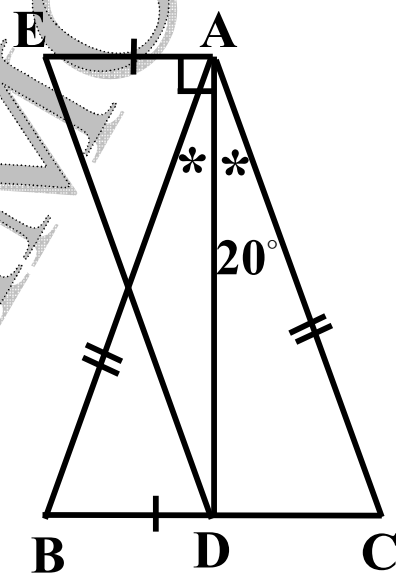
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12) In the opposite figure:

$AC = AB$, $AE = DB$, \overrightarrow{AD}
is the bisector of $\angle CAB$ and
 $\overline{DA} \perp \overline{AE}$
Find: $m(\angle AED)$



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13) In the opposite figure:

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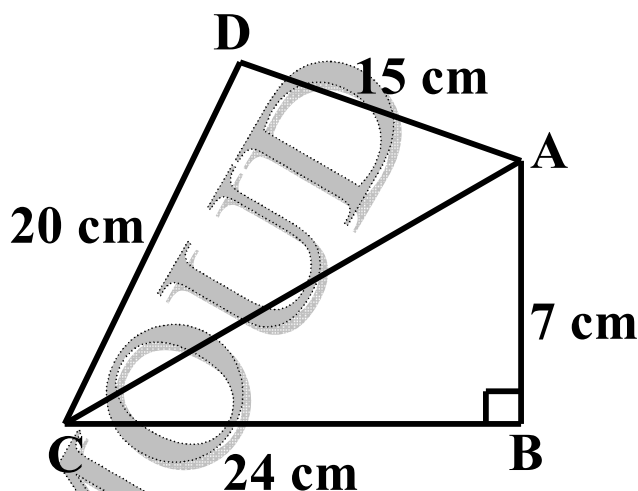
If $m(\angle ABC) = 90^\circ$, $AB = 7 \text{ cm}$, $BC = 24 \text{ cm}$

$CD = 20 \text{ cm}$. and $DA = 15 \text{ cm}$.

a) Is $m(\angle ADC) = 90^\circ$?

Why?

b) Find the area of the whole figure.



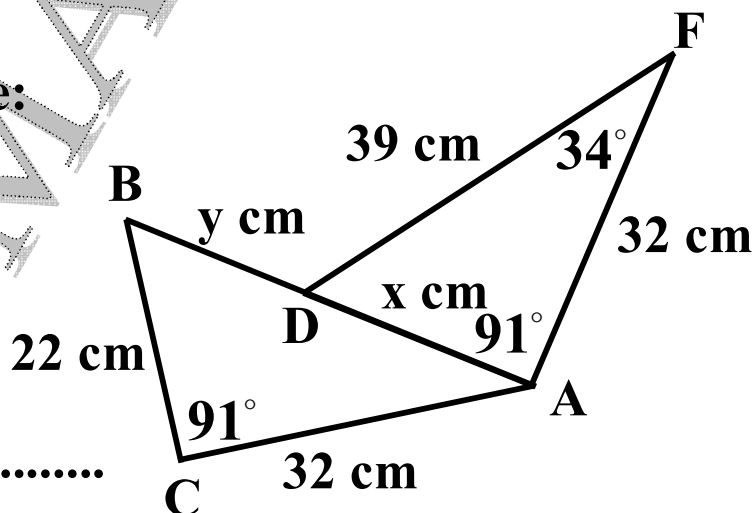
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14) In the opposite figure:

Find the value of

x and y



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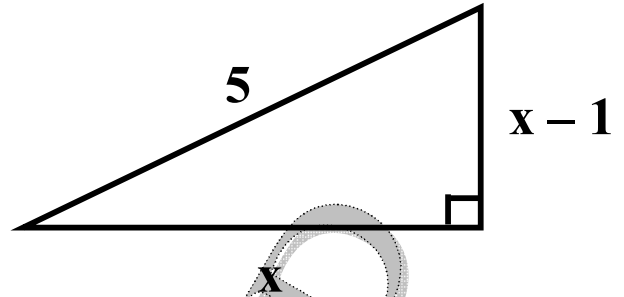
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[3] Choose:

1) In the opposite figure:



Which of the following
represents a true statement?

a) $x^2 + (x - 1)^2 = 25$

b) $x + (x - 1) = 25$

c) $x^2 - x = 12$

d) $(x - 1)^2 - x^2 = 25$

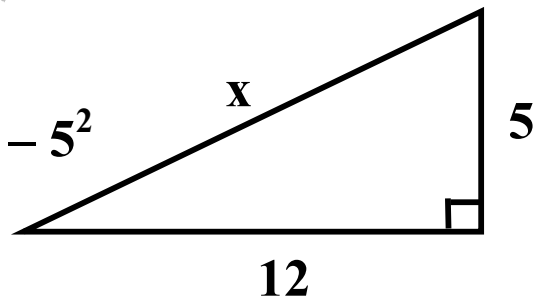
2) Which of the following represents a correct
statement?

a) $x = 5^2 + 12$

b) $x^2 = 12^2 - 5^2$

c) $x + 25 = 144$

d) $x^2 = 169$



[4]

1) Using the ruler and compasses. Draw ΔABC in which
 $AB = AC = 7$ cm. and $BC = 6$ cm. then bisect each of
 $\angle B$ and $\angle C$ by two bisectors intersecting at M

Is $MB = MC$? (Don't remove arcs)

2) State three cases of congruency of two triangles.

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3) If ΔABC in which $AB = 60 \text{ cm}$, $AC = 61$, $BC = 11 \text{ cm}$
is ΔABC right - angled or not ? then if it is
right - angled determine the right - angle.

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4) In ΔABC : $AB = 7 \text{ cm.}$, $AC = 25 \text{ cm}$ and $BC = 24 \text{ cm.}$
is ΔABC is right - angled or not ?
then determine the right angle if exist.

.....
.....

5) Using the geometric instruments draw an angle
of measure 130° then divide it into 4 equal angles
in measure

6) Put (\checkmark) or (\times):-

a) Each two equal triangles in perimeter are
congruent.

b) The two right-angled triangles are congruent if
two sides in one of them are equal to their
corresponding sides in the other

7) Draw $\triangle ABC$ in which $AB = AC = 5 \text{ cm.}$ and $BC = 6 \text{ cm.}$
then draw $\overline{AD} \perp \overline{BC}$ where $\overline{AD} \cap \overline{BC} = \{D\}$, then
find by measure the length of \overline{AD}

8) A ladder of length 10 metre leans on a horizontal
ground and a vertical wall if its upper end is over the
ground by 8 metre find the square of the distance
between its lower end and the wall. Show your work.

9) LMN is a triangle in which $LM = 20 \text{ cm}$, $MN = 21 \text{ cm}$ and $LN = 29 \text{ cm}$ show if ΔLMN is a right - angled or not. determine the right angle if it exists.

10) Using the geometric tools to draw the equilateral triangle ABC whose side length = 4 cm. then draw $\overline{AD} \perp \overline{BC}$ where $\overrightarrow{AD} \cap \overline{BC} = \{ D \}$

11) Using the geometric tools to draw ΔABC in which $AB = 3 \text{ cm}$, $BC = 4 \text{ cm}$, $AC = 5 \text{ cm}$, then bisect $\angle B$ by \overrightarrow{BD} which cuts \overline{AC} at D and find by measure the length of \overline{BD}

12) Put (\checkmark) or (\times):-

a) Each two congruent triangles are equal in area.

b) The two triangles are congruent if the measures of the angles of one of them are equal to its corresponding measures of the angles in the other two sides.

c) The area of the square set up a side of the

right angle in the right-angled triangle equals the sum of the areas of the two squares set up the other two sides.

13) Draw ΔABC which is an equilateral and its side length = 5 cm. long then bisect $\angle A$, $\angle B$ and $\angle C$ by three bisectors intersecting at M is $MA = MB = MC$?

14) Draw ΔABC in which $AB = 7$ cm, $m(\angle A) = 50^\circ$ and $m(\angle B) = 70^\circ$, then draw $\overline{CD} \perp \overline{AB}$ and cut it at D, then find by measure the length of \overline{CD} then calculate the area of ΔABC .

15) If ABC is a triangle in which $AB = 3 \text{ cm}$, $BC = 4 \text{ cm}$ and $AC = 5 \text{ cm}$ show if the triangle ABC is right - angled or not ? then determine the right angle if it exist.

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16) Using the geometric tools , draw an angle of measure 65° then bisect it.

17) Draw ΔABC in which $AB = AC = 6$ cm. and

$m(\angle A) = 70^\circ$ using the compasses and the ruler to bisect $\angle B$ and $\angle C$ by two bisectors meeting at M

18) Mention two cases of congruency of two triangles.

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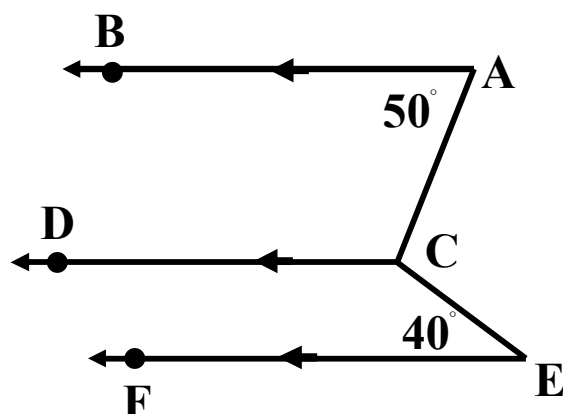
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[5] Complete:

1) In the opposite figure :

$m(\angle ACE) = \dots\dots\dots$



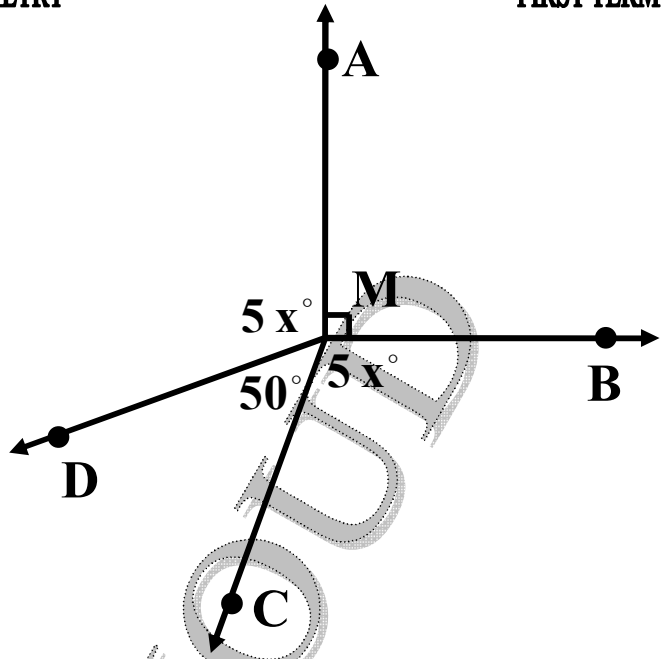
2) In the opposite figure :

the value of $x = \dots\dots\dots$

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3) If a straight line cuts two parallel straight lines ,

then each two corresponding angles are

..... in measure.

4) The sum of the measures of the accumulative angles

at a point equals°

5) If two straight lines intersect, then each two vertical

opposite angles are in measure.

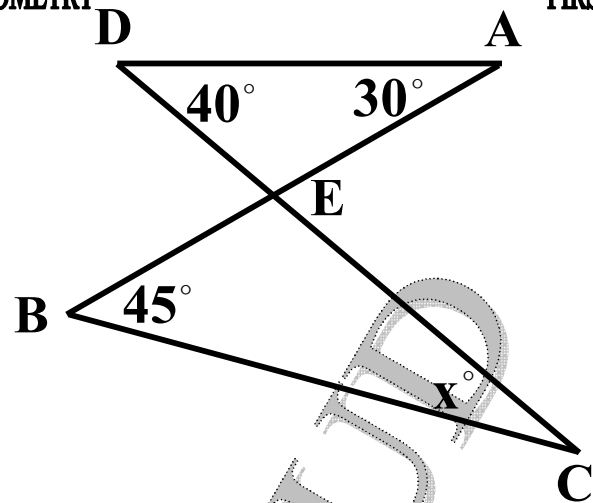
6) The perpendicular to one of two parallel

straight lines is the other.

7) In the opposite figure :

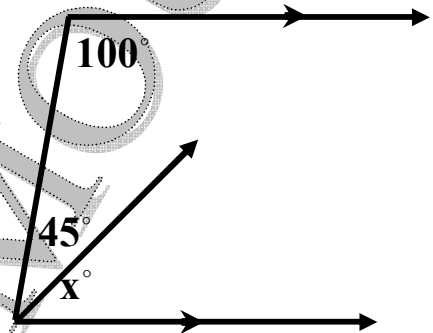
$$\text{If } \overline{AB} \cap \overline{CD} = \{E\}$$

then $x = \dots\dots\dots$



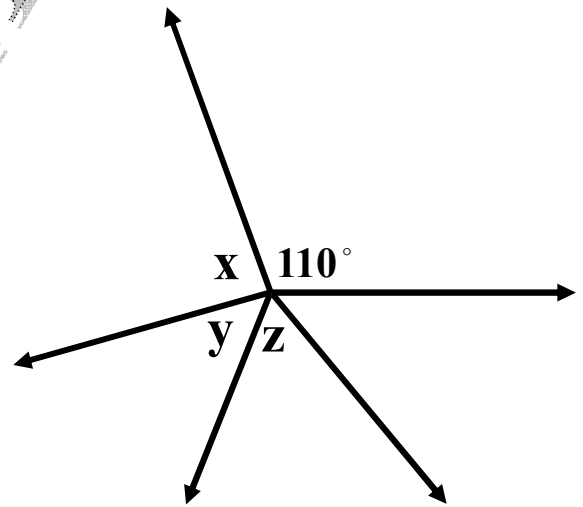
8) In the opposite figure :

The value of $x = \dots\dots\dots^\circ$



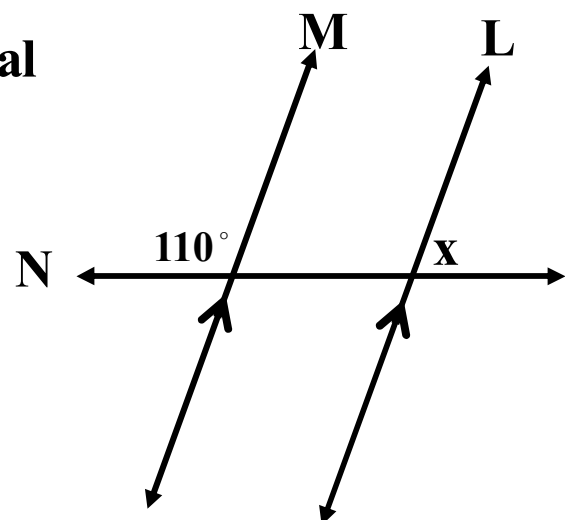
9) In the opposite figure :

$$x + y + z = \dots\dots\dots^\circ$$



10) In the opposite figure :

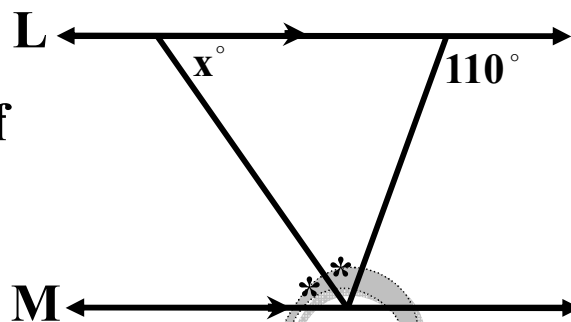
$L \parallel M$ and N is a transversal to them then $x = \dots\dots\dots$



11) In the opposite figure :

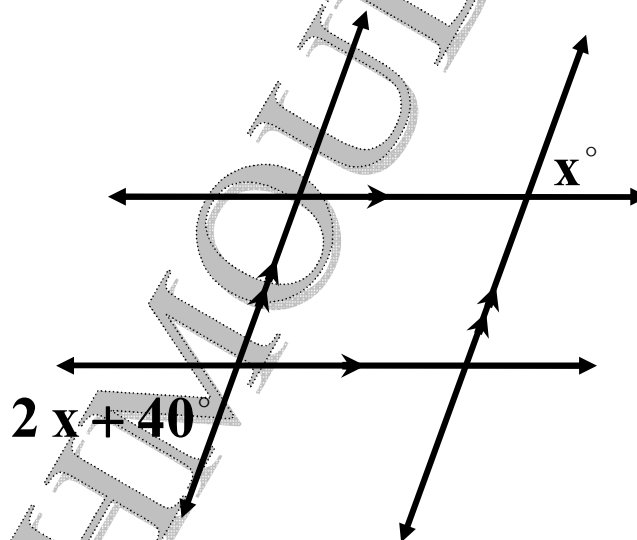
If $L \parallel M$, then the value of

$x = \dots\dots\dots$



12) In the opposite figure :

The value of $x = \dots\dots\dots$

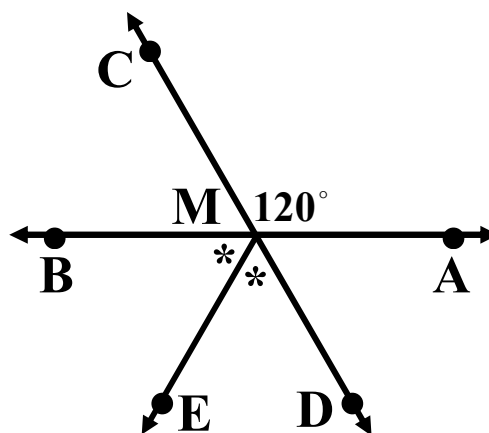


13) In the opposite figure :

$\overleftrightarrow{AB} \cap \overleftrightarrow{CD} = \{M\}$ and \overrightarrow{ME}

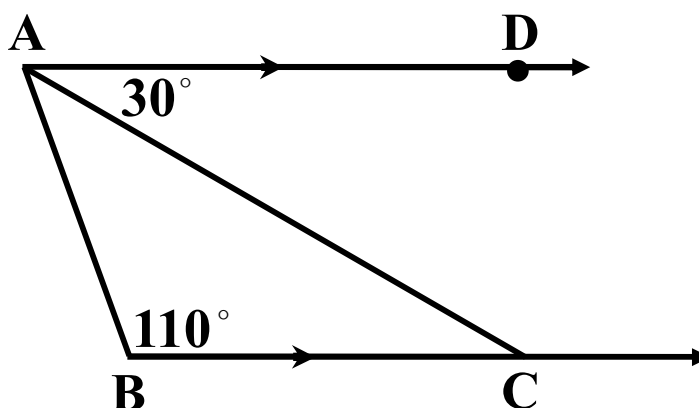
bisects $\angle BMD$

then $m(\angle AME) = \dots\dots\dots$



14) In the opposite figure :

$m(\angle BAC) = \dots\dots\dots^\circ$

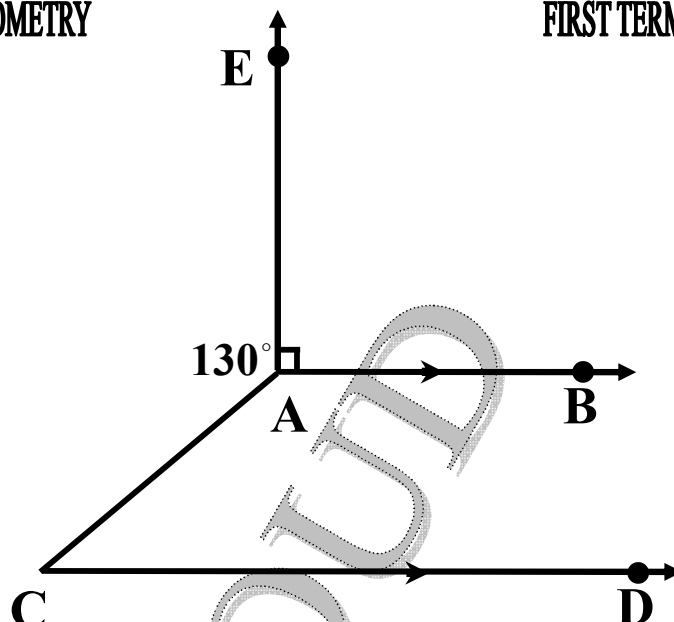


15) In the opposite figure :

If $\overrightarrow{AB} \parallel \overrightarrow{CD}$, $\overline{AE} \perp \overline{AB}$

and $m(\angle EAC) = 130^\circ$

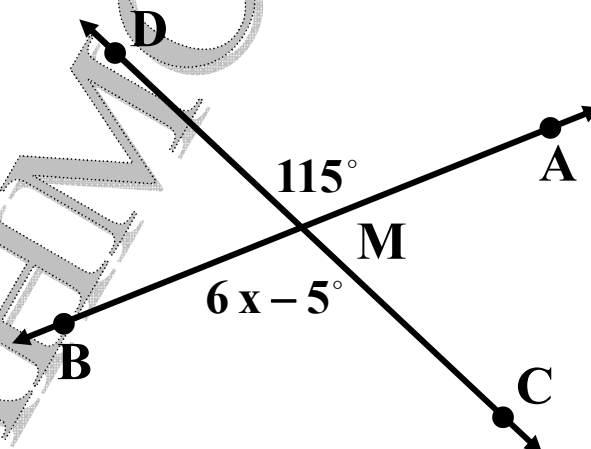
then $m(\angle C) = \dots\dots\dots^\circ$



16) In the opposite figure :

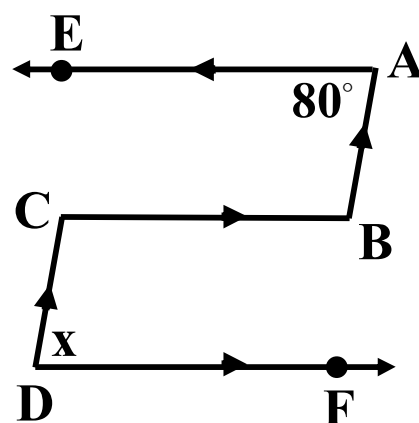
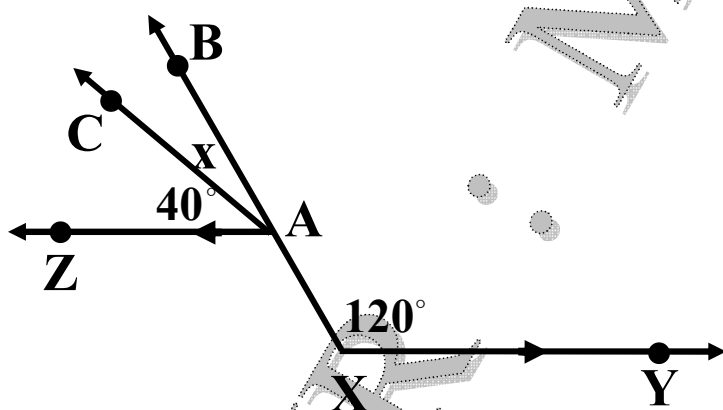
$\overleftrightarrow{AB} \cap \overleftrightarrow{CD} = \{M\}$

The value of $x = \dots\dots^\circ$



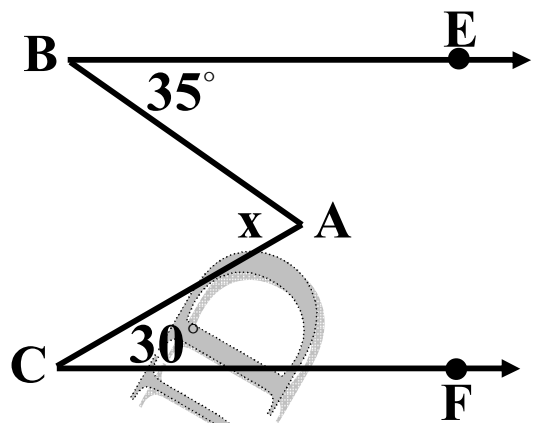
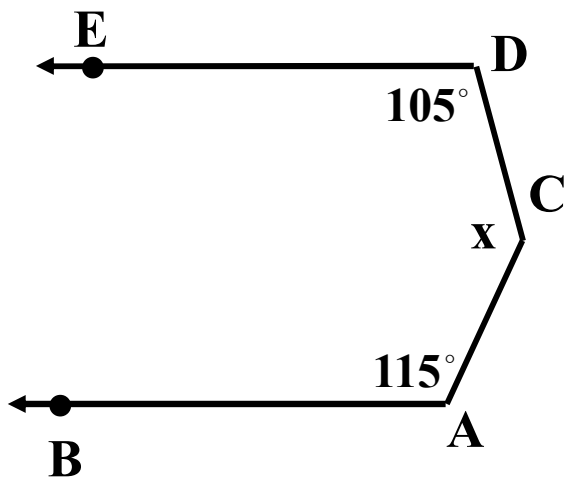
[6] In The opposite figure:

Find the value of x



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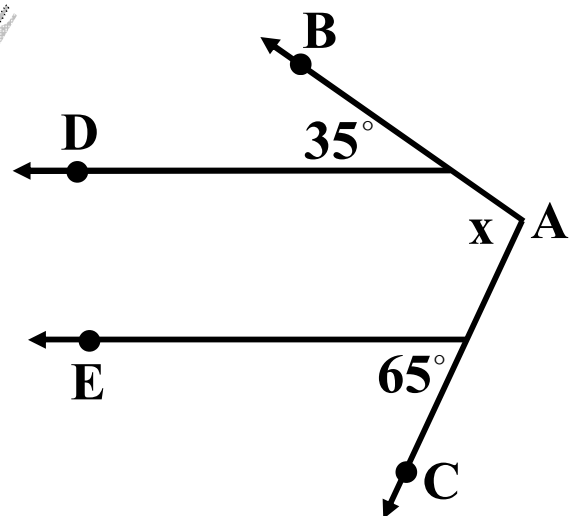
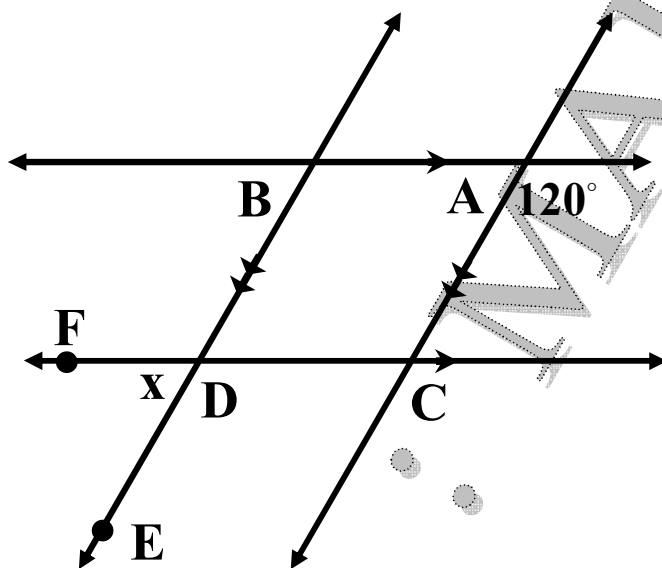
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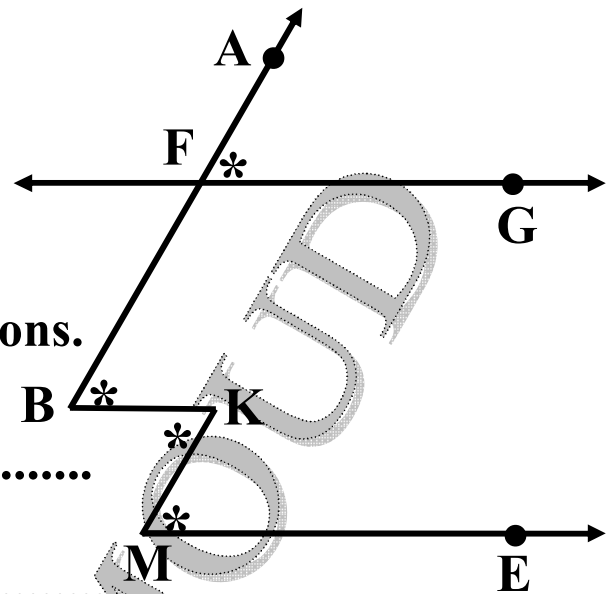
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[7] In The opposite figure:

$$m(\angle AFG) = m(\angle B)$$

$$= m(\angle K) = m(\angle M)$$

write the four pairs of parallel lines. give yor reasons.



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[8] In each of the following figures , show if the two

triangles are congruent or not if they are congruent

name the case of congruence.

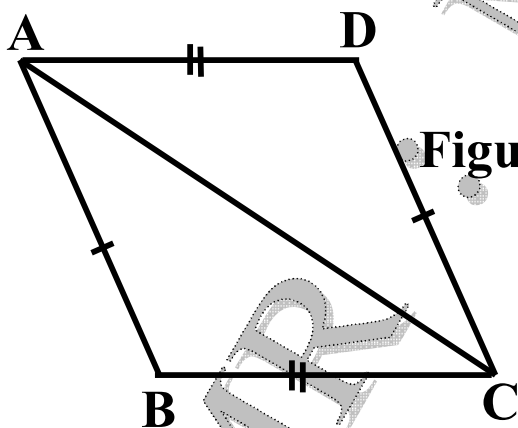


Figure (1)

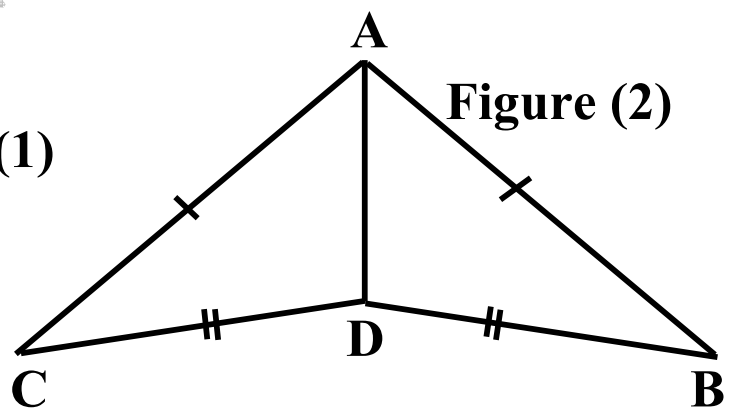


Figure (2)

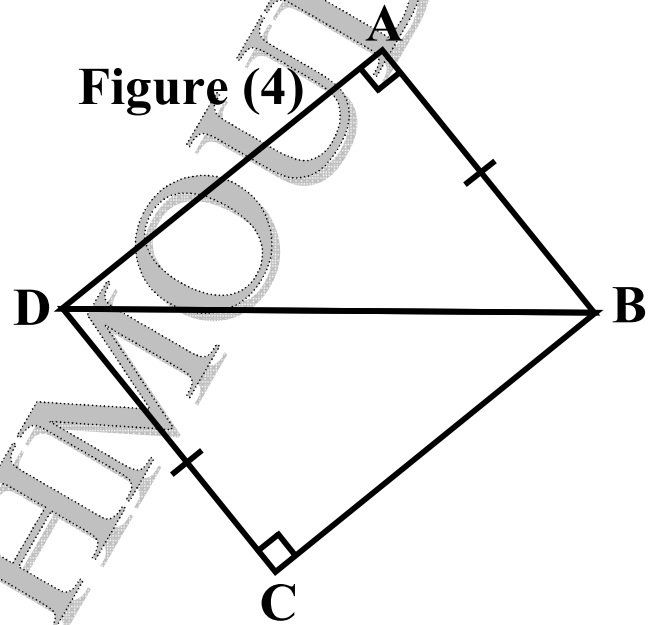
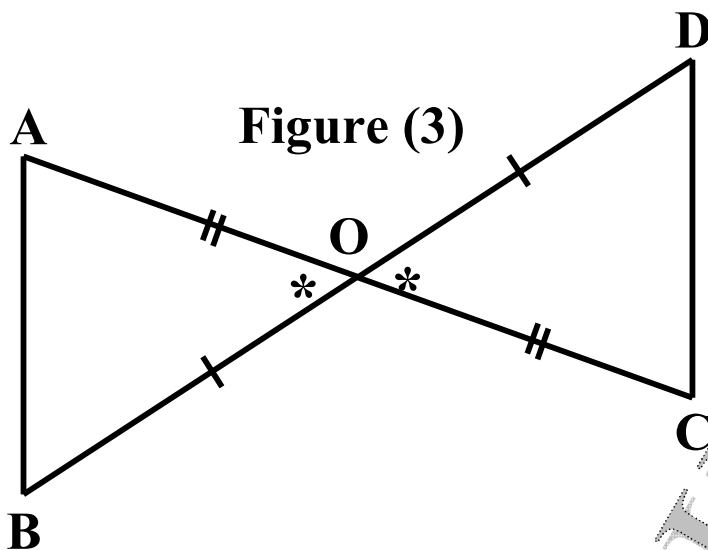
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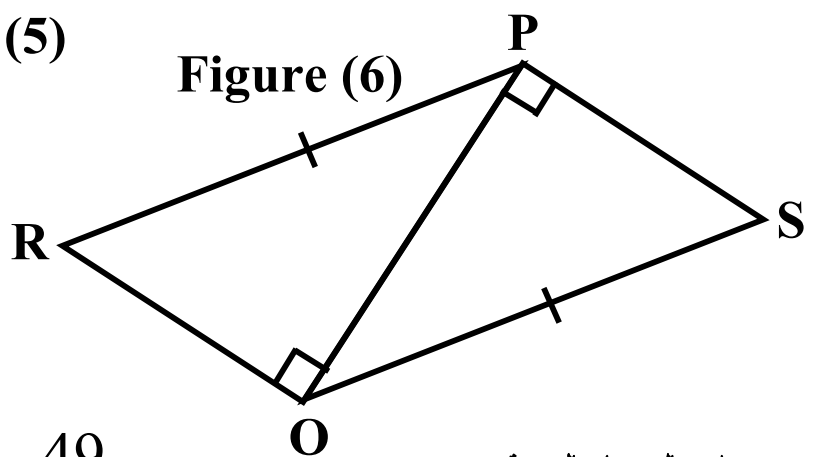
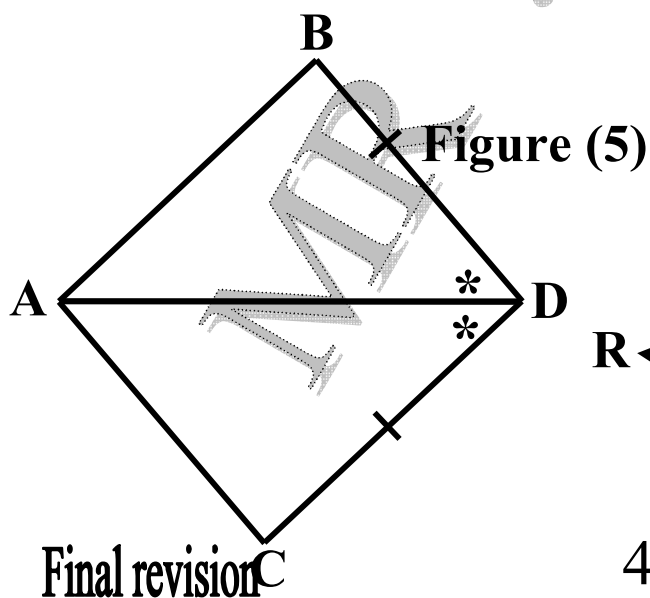


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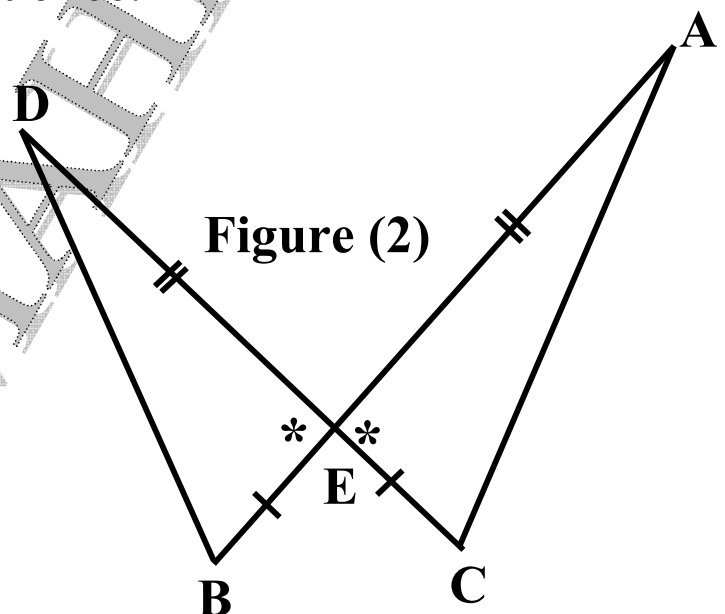
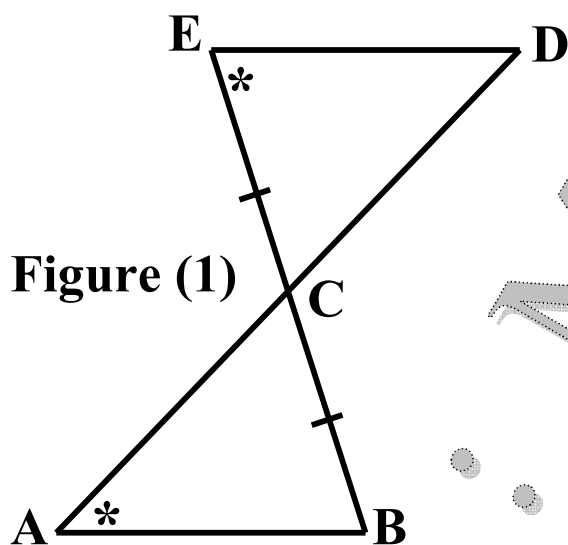
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[9] In each of the following figures , show if the two triangles are congruent or not if they are congruent name the case of congruence.



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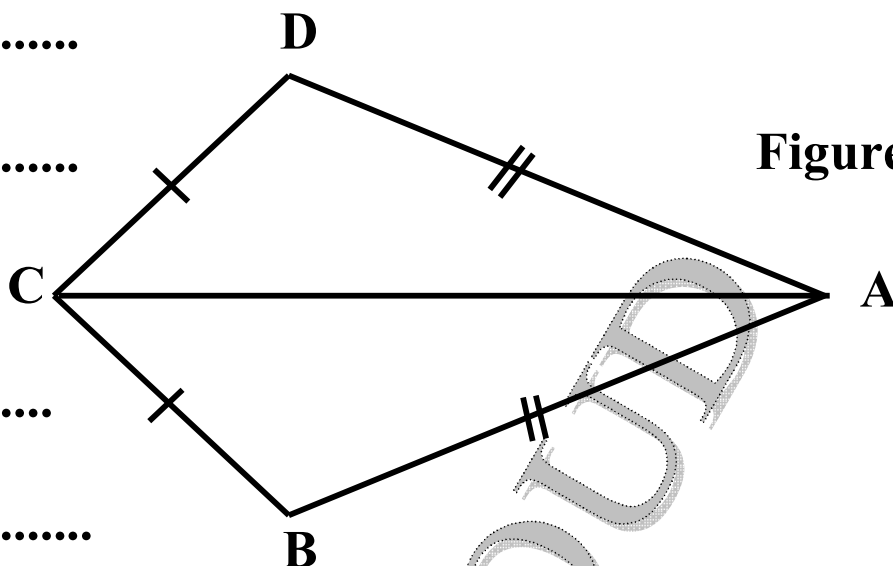


Figure (3)

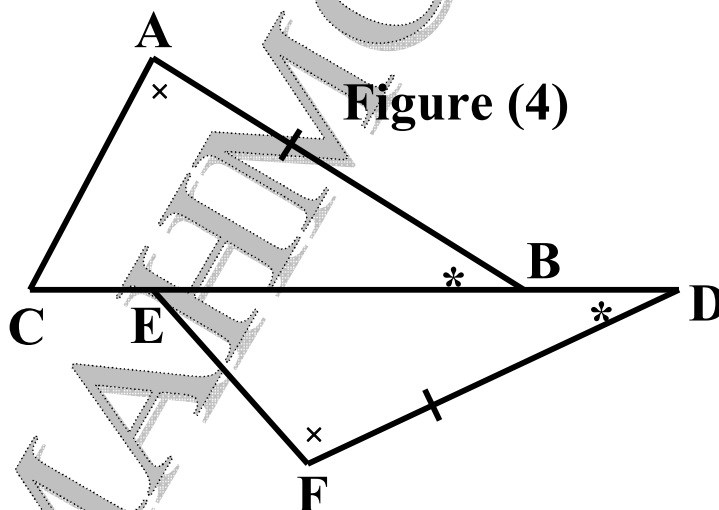


Figure (4)

[1] Mention the type of the angle whose measure is as the following:

1) 57° 2) 117° 3) 90°

4) 200° 5) 180° 6) $90\frac{2}{5}^\circ$

7) $181\frac{3}{4}^\circ$ 8) $43\frac{1}{2}^\circ$

[2] Write the measure of the angle which complements each of the angles whose measure are as follow:

- 1) 20° 2) 90° 3) 152°
 4) 0° 5) $92\frac{1}{2}^\circ$ 6) 180°
 7) 10° 8) $141\frac{2}{5}^\circ$

[3] Write the measure of the angle which supplements each of the angles whose measure are as follow:

- 1) 30° 2) 60° 3) 48°
 4) 0° 6) 90°
 5) $32\frac{1}{2}^\circ$ 7) $25\frac{3}{4}^\circ$ 8) $53\frac{1}{4}^\circ$

[4] Complete:

- 1) The angle is
 2) Measure of the right angle =
 3) The acute angle is the angle whose measure is less
 Than and greater than

4) The sum of the complementary angles =

5) The sum of the supplementary angles =

6) Measure of the straight angle =

And the measure of zero angle =

7) The two adjacent angles formed from the

Intersection of a ray and a straight line are.....

[5] Complete the following

1) The acute angle complements an.....angle and

Supplements.....angle.

2) The zero angle complements a.....and

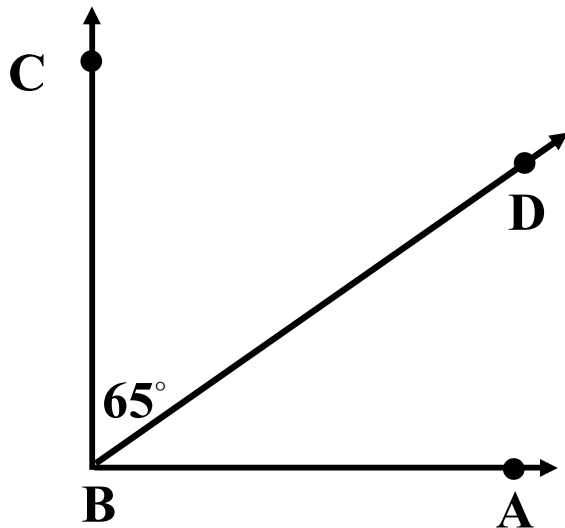
Supplements a.....angle.

3) The right angle complements.....angle and

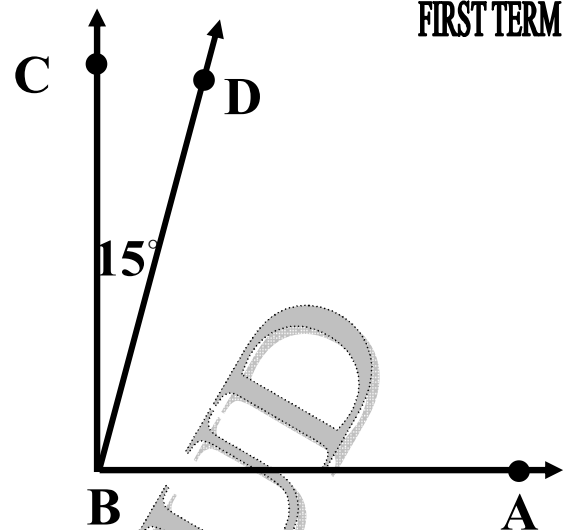
Supplements a.....angle.

4) The obtuse angle supplements.....angle.

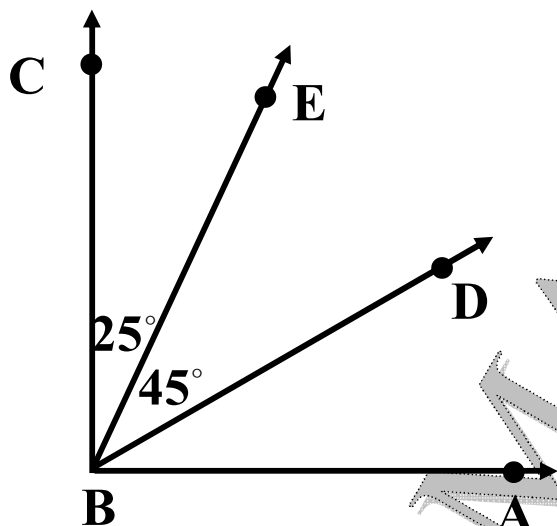
[6] In each of the following figures if $\overrightarrow{BA} \perp \overrightarrow{BC}$ find the Measures of the required angle under each figure :



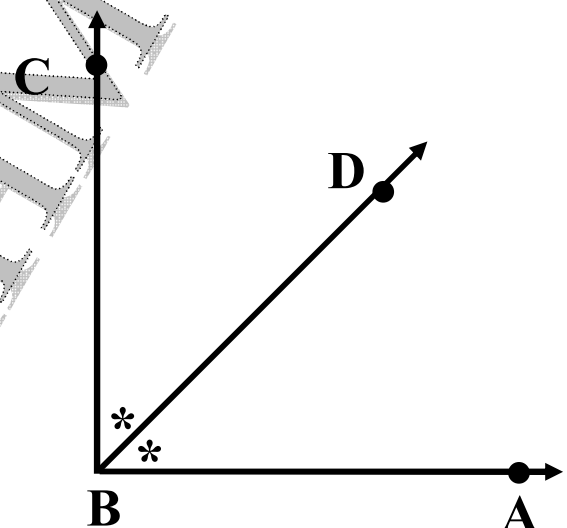
1) $m(\angle ABD) = \dots^\circ$



2) $m(\angle ABD) = \dots^\circ$



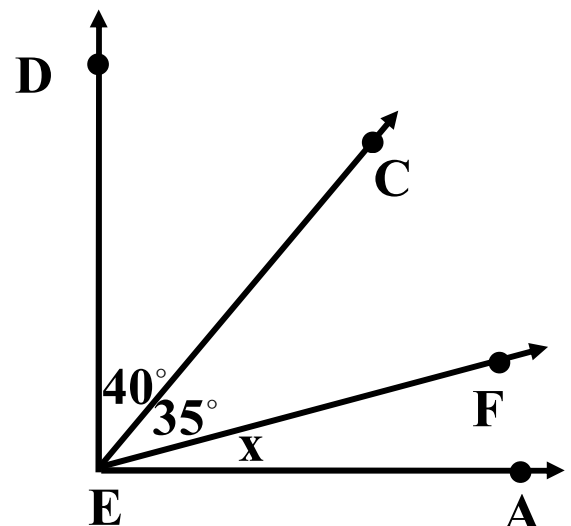
3) $m(\angle ABD) = \dots^\circ$



4) $m(\angle ABD) = \dots^\circ$

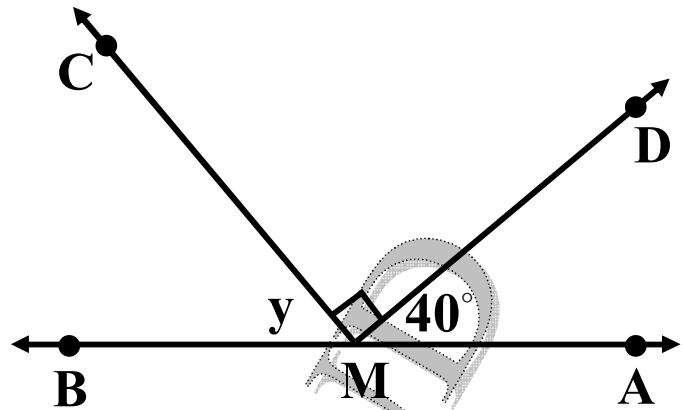
[7] Complete:

1) If $\overrightarrow{EA} \perp \overrightarrow{ED}$
Then $x = \dots^\circ$



2) If $M \in \overleftrightarrow{AB}$

$$y = \dots\dots^\circ$$

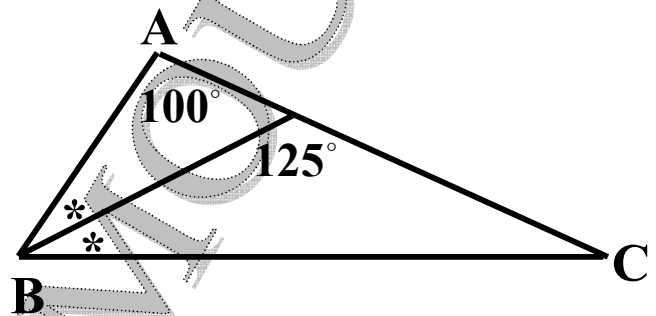


3) ABC is a triangle

$D \in \overline{AC}$ and \overrightarrow{BD} is

A bisector of $\angle B$

Then $m(\angle C) = \dots\dots$



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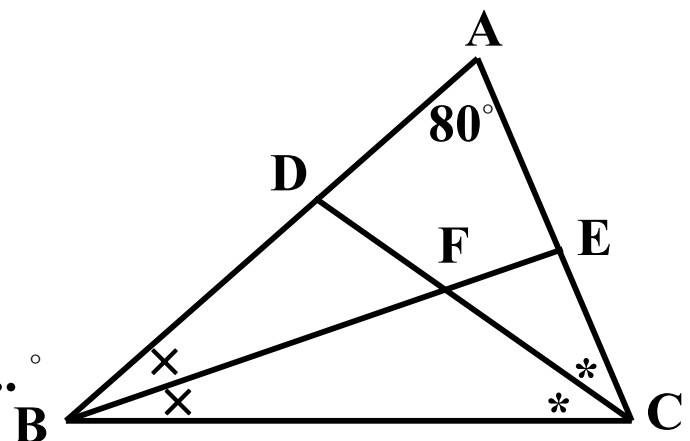
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4) $m(\angle A) = 80^\circ$, \overrightarrow{BE} is

The bisector of $\angle B$

\overrightarrow{CD} is the bisector of

$\angle C$ then $m(\angle BFC) = \dots\dots^\circ$



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Complete:

- 1) The sum of measures of the accumulative angles at a point =
- 2) The angle whose measure is 72° complements the angle whose measure is
- 3) If $m(\angle A) = 150^\circ$, then $m(\text{reflex } \angle A) = \dots\dots\dots$
- 4) The two adjacent complementary angles , their terminal sides are
- 5) If $\angle A$ supplements $\angle B$, $\angle A \cong \angle B$, then $m(\angle B) = \dots\dots\dots$
- 6) The measure of the straight angle =
- 7) If one of the two supplement angles is acute then the other is angle.
- 8) If $m(\angle A) = 170^\circ$, then $m(\text{reflex } \angle A) = \dots\dots\dots$
- 9) < the measure of the obtuse angle <

10) If $\angle A$ supplements $\angle B$, and $m(\angle A) = 2 m(\angle B)$,
then $m(\angle B) = \dots\dots$

11) The sum of measures of the two complementary
angles = $\dots\dots$

12) The sum of measures of the two supplementary
angles equals $\dots\dots$

13) If $m(\angle X) = \frac{1}{2} m(\angle Y)$ and $m(\angle X) = 30^\circ$, then the two
angles X and Y are $\dots\dots$

14) The two adjacent angles formed by intersecting a
straight line and a ray whose start point lies on the
straight line are $\dots\dots$

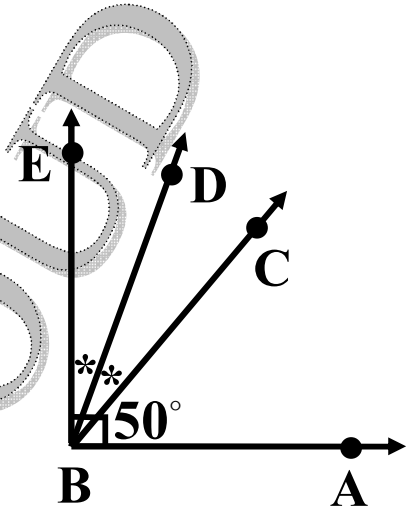
Complete:

1) If $m(\angle X) = \frac{1}{2} m(\angle Y)$ and $m(\angle X) = 60^\circ$, then the two angles X and Y are

2) In the opposite figure:

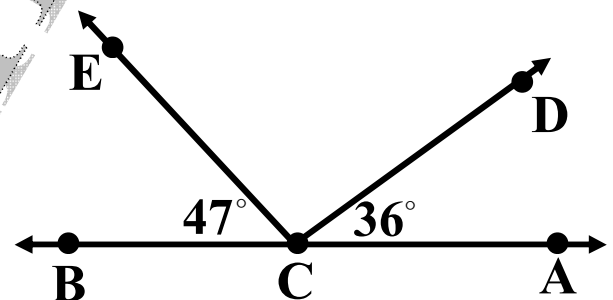
If $m(\angle ABC) = 50^\circ$, \overrightarrow{BD} bisects $\angle CBE$

$\overrightarrow{BD} \perp \overrightarrow{BE}$, then $m(\angle CBD) = \dots$



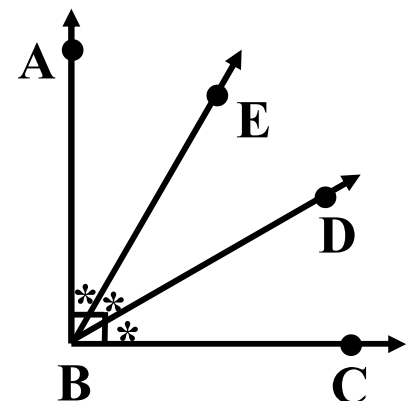
3) In the opposite figure:

$m(\angle DCE) = \dots$



4) In the opposite figure:

If $\overrightarrow{BA} \perp \overrightarrow{BC}$, then $m(\angle CBE) = \dots$

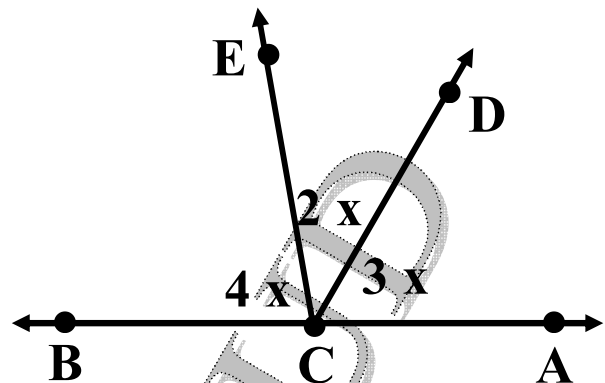


Test (7)

Complete:

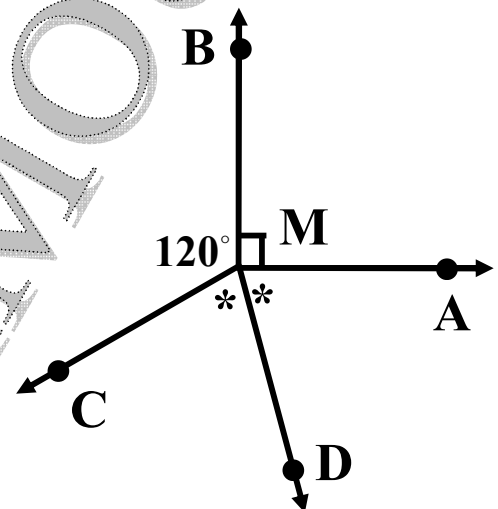
1) In the opposite figure:

If $A \in \overleftrightarrow{BC}$, then $x = \dots\dots$



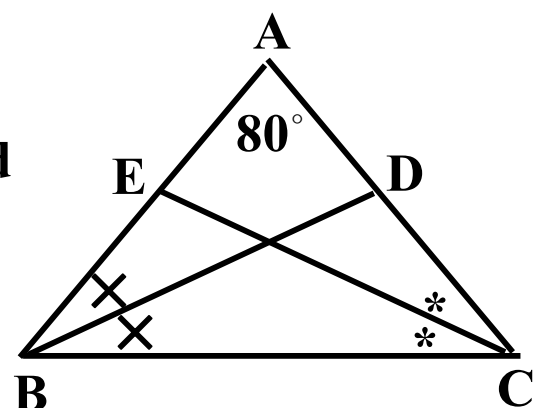
2) In the opposite figure:

\overrightarrow{MD} bisects $\angle AMC$,
then $m(\angle AMD) = \dots\dots$



3) In the opposite figure:

$m(\angle A) = 80^\circ$, \overrightarrow{BD} bisects $\angle B$ and
 \overrightarrow{CE} bisects $\angle C$,
then $m(\angle CFB) = \dots\dots\dots$

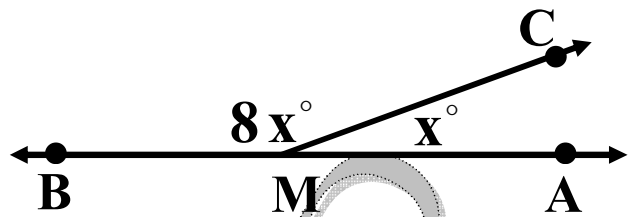


Test (8)

Complete:

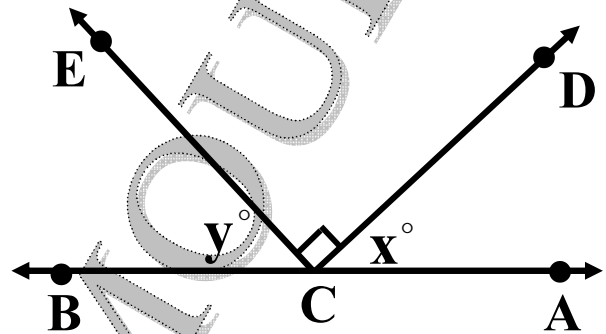
1) In the opposite figure:

If $M \in \overleftrightarrow{AB}$, then $x = \dots\dots$



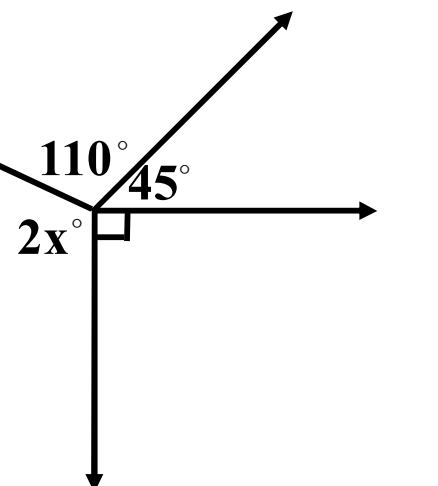
2) In the opposite figure:

If $C \in \overleftrightarrow{AB}$
then $x^\circ + y^\circ = \dots\dots$



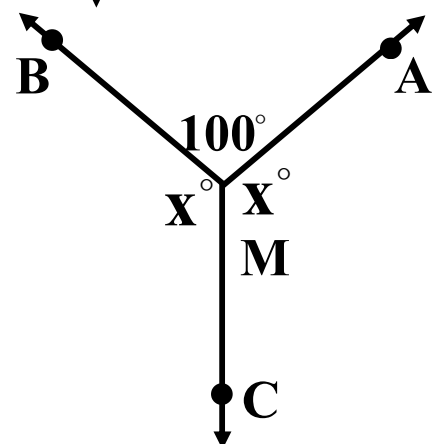
3) In the opposite figure:

$x = \dots$



4) In the opposite figure:

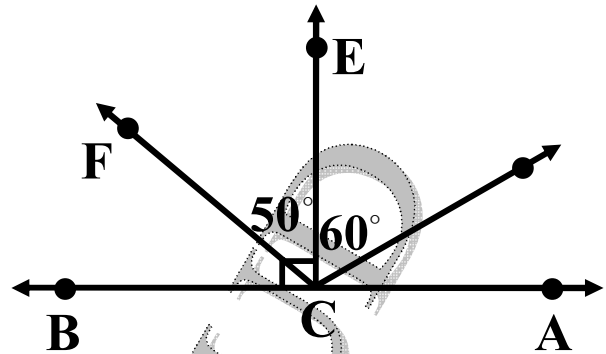
If $m(\angle AMB) = 100^\circ$
, then $x = \dots\dots$



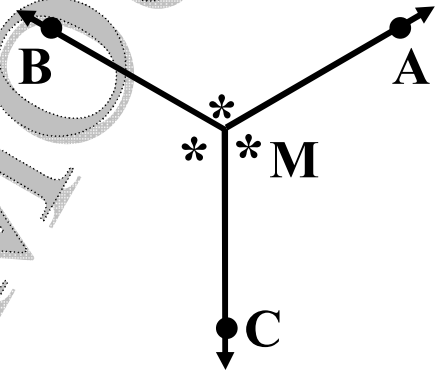
Test (9)

Complete:

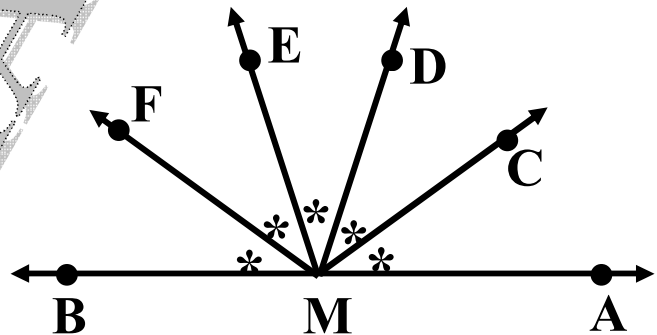
1) The number of obtuse angle in the opposite figure is



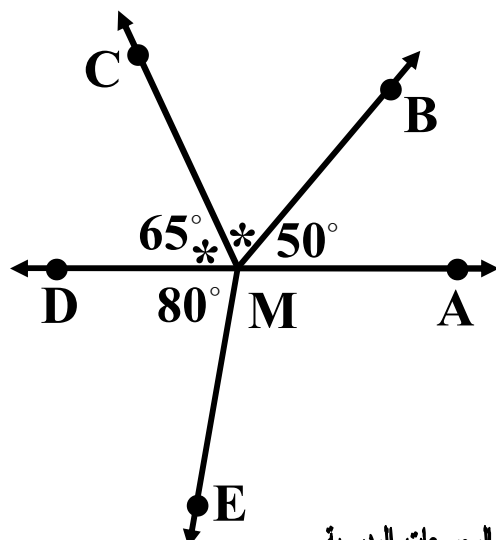
2) In the opposite figure:
 $m(\angle AMC) = \dots\dots^\circ$



3) In the opposite figure:
 If $M \in \overleftrightarrow{AB}$, then
 $m(\angle AMC) = \dots\dots$



4) Find the measure of the required angle:
 If \overrightarrow{MC} bisects $\angle BMD$
 then $m(\angle AME) = \dots\dots$

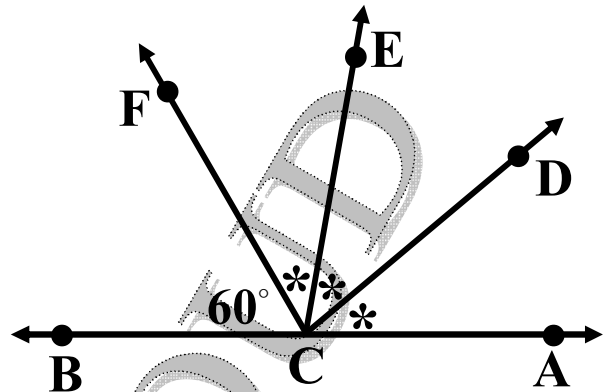


Test (10)

Complete:

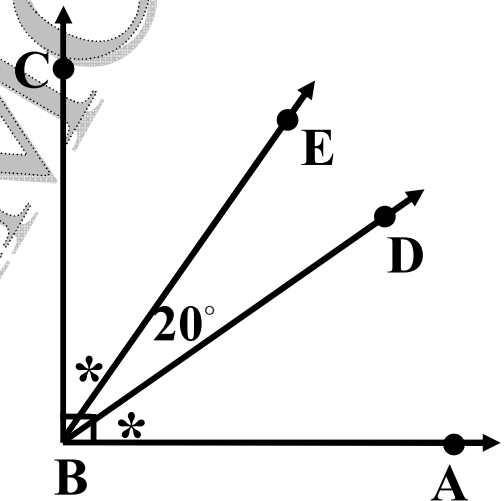
- 1) Find the measure of the required angle:

If $C \in \overleftrightarrow{AB}$ then
 $m(\angle DCB) = \dots\dots$

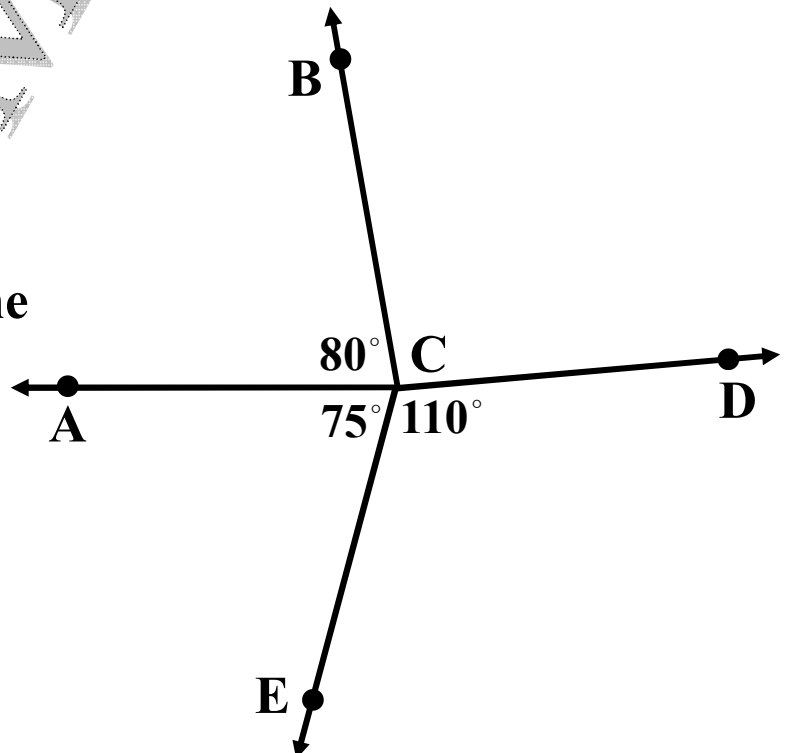


- 2) Find the measure of the required angle:

If $\overrightarrow{BA} \perp \overrightarrow{BC}$
 then $m(\angle ABD) = \dots\dots$



- 3) Find the measure of the required angle
 $m(\angle BCD) = \dots\dots$



Test (11)

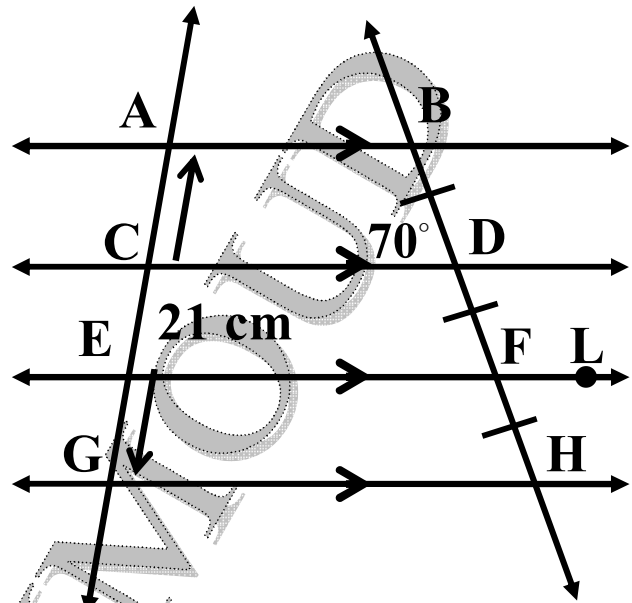
[1] In the opposite figure:

$\overleftrightarrow{AB} \parallel \overleftrightarrow{CD} \parallel \overleftrightarrow{EF} \parallel \overleftrightarrow{GH}$

, $AG = 21 \text{ cm}$, $m(\angle BDC) = 70^\circ$

Find:

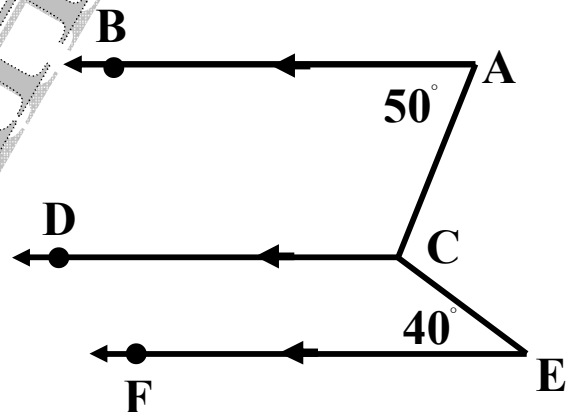
- 1) The length of \overline{AE}
- 2) $m(\angle ABD)$
- 3) $m(\angle HFL)$



[2] Complete:

1) In the opposite figure :

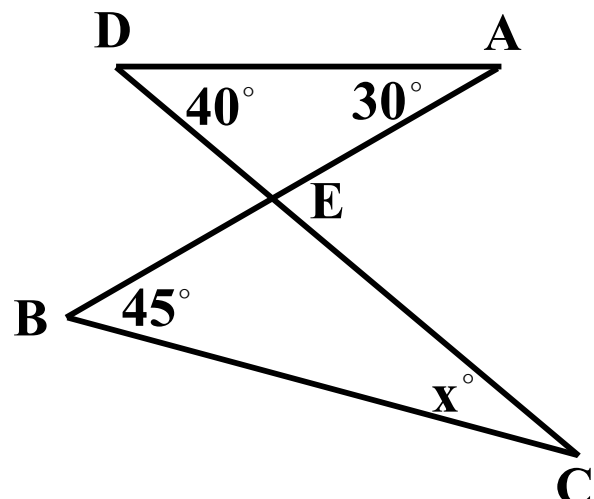
$m(\angle ACE) = \dots\dots\dots$



2) In the opposite figure :

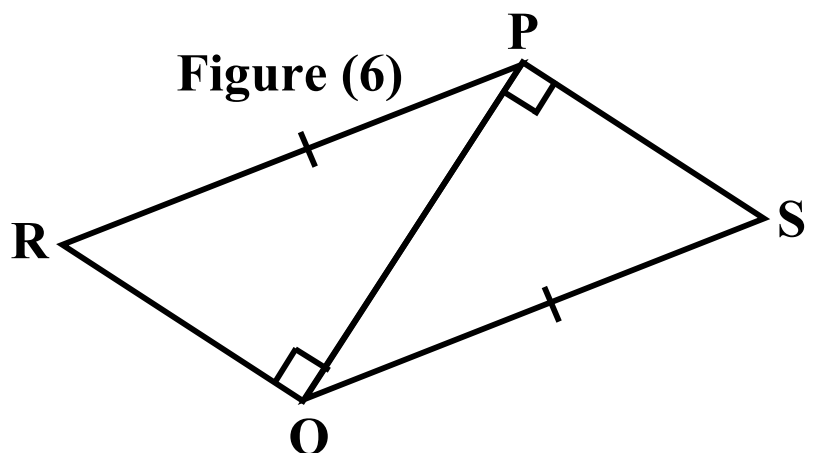
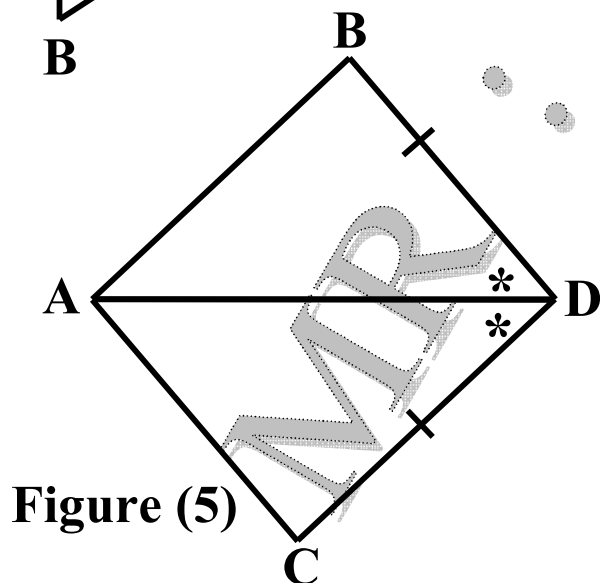
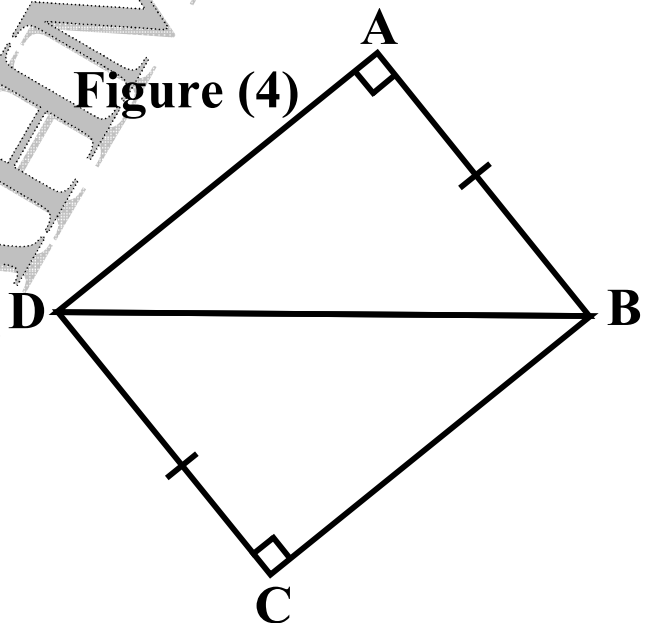
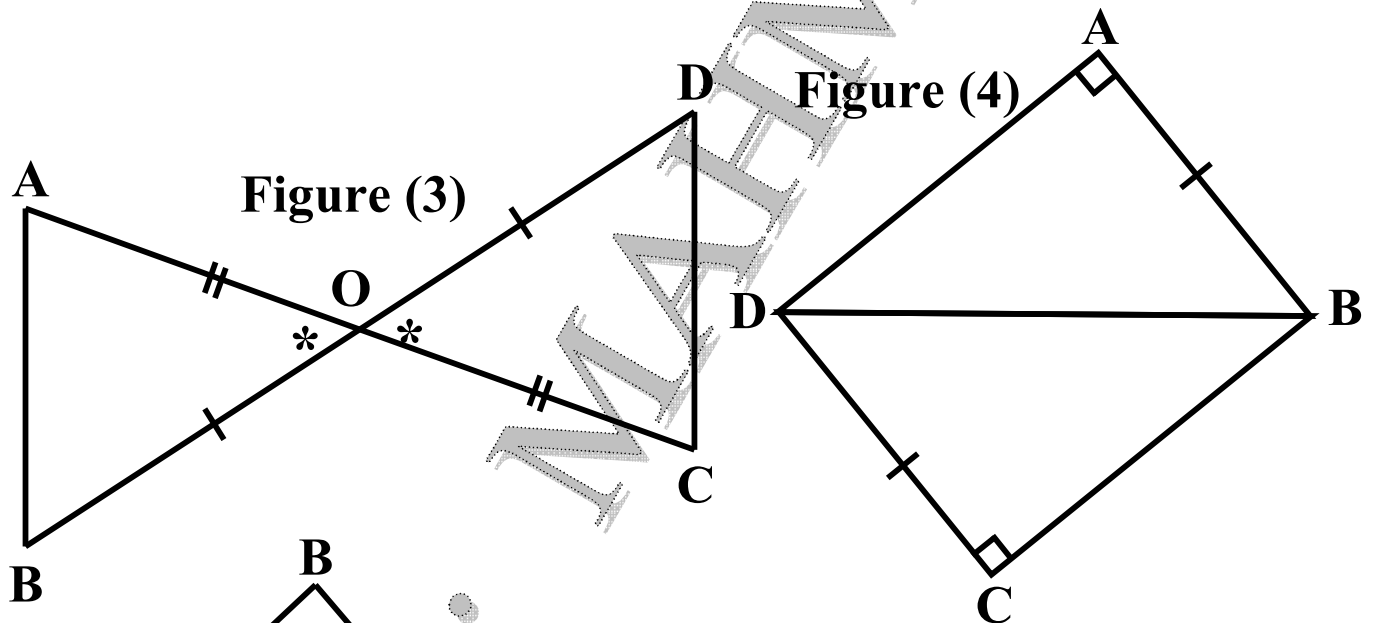
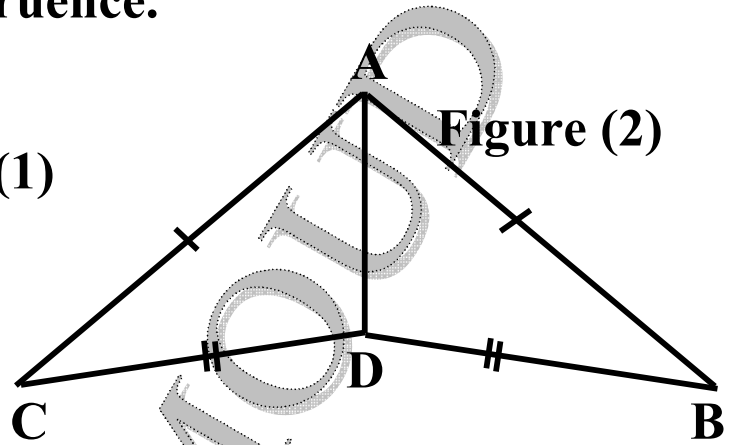
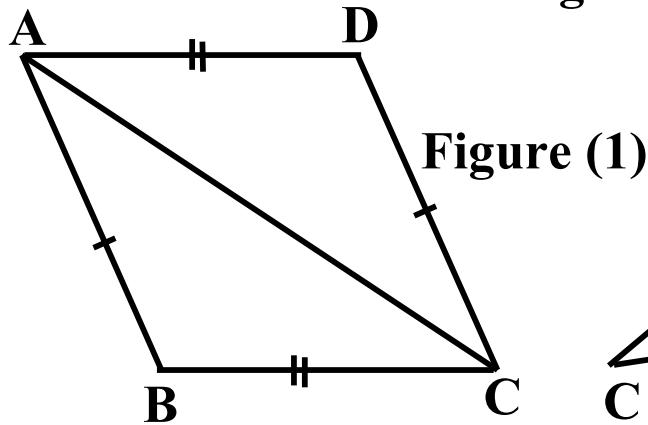
If $\overline{AB} \cap \overline{CD} = \{E\}$

then $x = \dots\dots\dots$



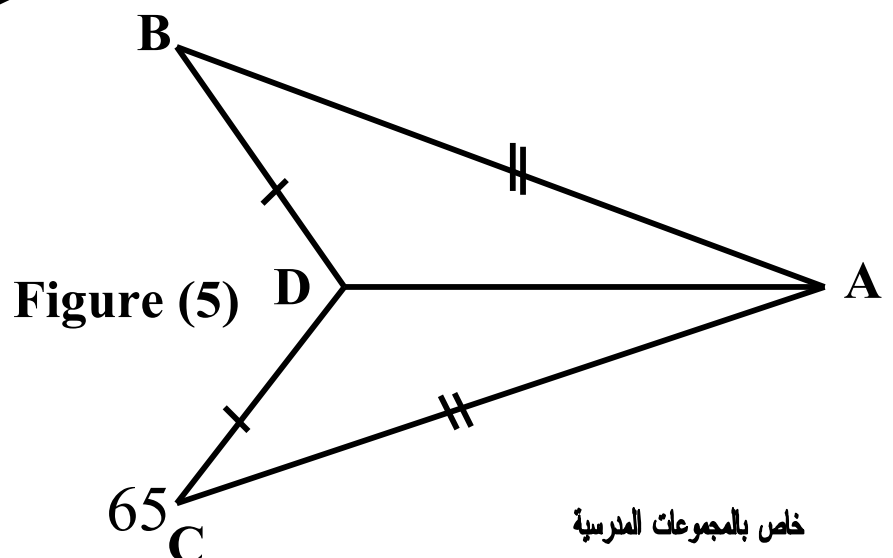
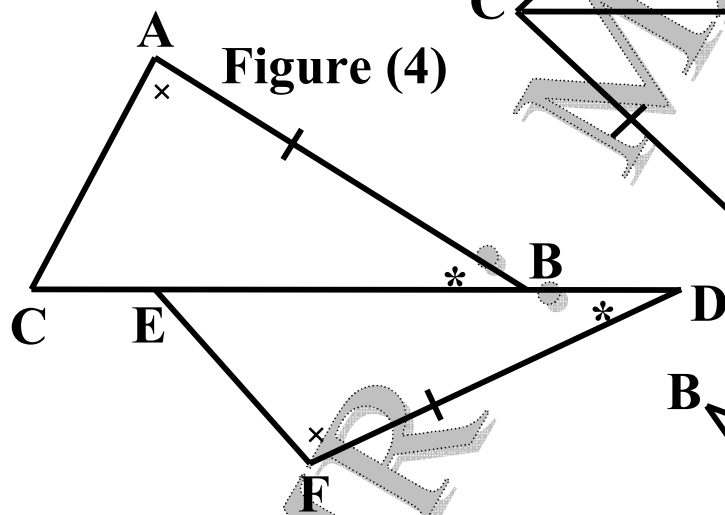
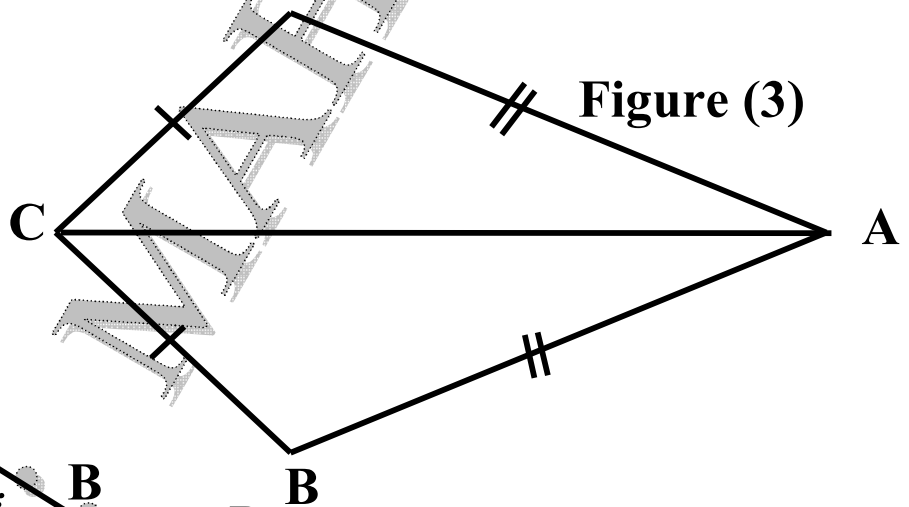
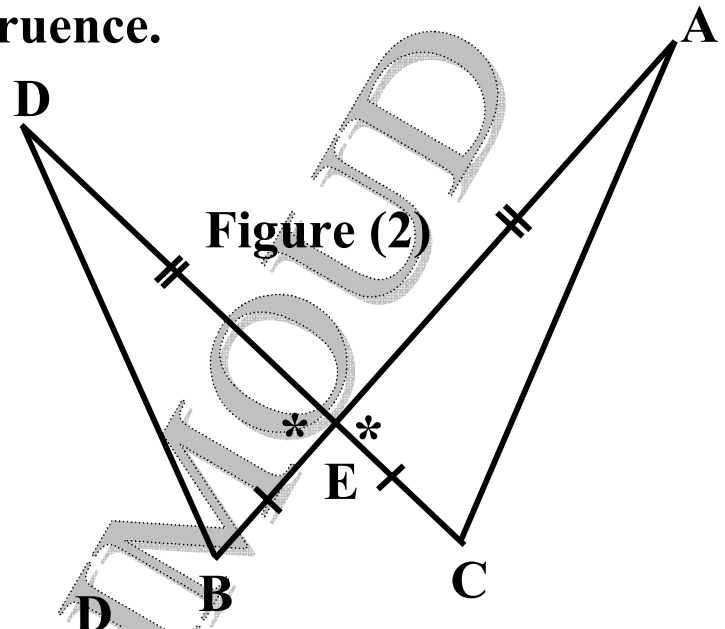
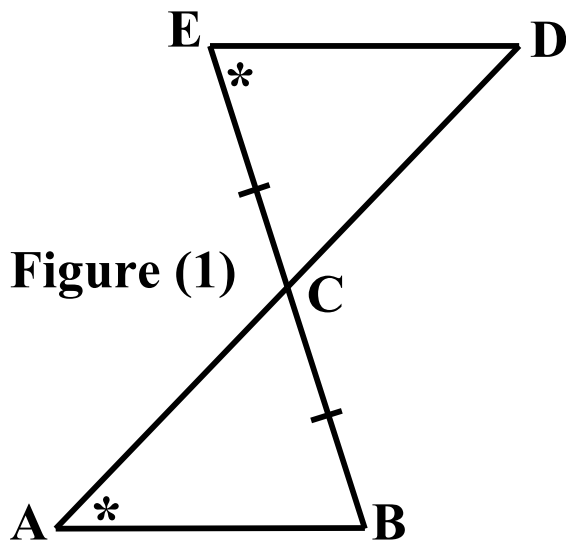
Test (12)

[1] In each of the following figures , show if the two triangles are congruent or not if they are congruent name the case of congruence.



Test (13)

[1] In each of the following figures , show if the two triangles are congruent or not if they are congruent name the case of congruence.



[1] Complete:

- 1) The sum of measures of the accumulative angles at a point =
- 2) The angle whose measure is 72° complements the angle whose measure is
- 3) If $\triangle ABC \equiv \triangle XYZ$ and $m(\angle X) = 50^\circ$, $m(\angle B) = 60^\circ$ then $m(\angle Z) = \dots$
- 4) The diagonal of the rectangle divides its surface into two triangles.
- 7) If $m(\angle A) = 150^\circ$, then $m(\text{reflex } \angle A) = \dots$
- 9) If a line segment is extended from one side without limit, the produced figure is
- 10) If $\angle A$ supplements $\angle B$, $\angle A \equiv \angle B$, then $m(\angle B) = \dots$
- 11) The measure of the straight angle =

- 13) If one of the two supplement angles is acute then the other is angle.
- 14) The two triangles are congruent if two sides and in one of them are congruent to their corresponding elements in the other.
- 16) < the measure of the obtuse angle <
- 17) If ΔXYZ is right-angled at X , $XY = 12 \text{ cm}$, $XZ = 9 \text{ cm}$. then $(YZ)^2 = \dots\dots\dots \text{cm}^2$.
- 19) If $\Delta ABC \equiv \Delta XYZ$ then $BC = \dots\dots\dots$
- 20) If $\angle A$ supplements $\angle B$, and $m(\angle A) = 2 m(\angle B)$, then $m(\angle B) = \dots\dots\dots$
- 26) If ABC is a triangle in which $AB = 5 \text{ cm}$, $BC = 12 \text{ cm}$ and $AC = 13 \text{ cm}$ then $m(\angle \dots\dots\dots) = 90^\circ$
- 27) The two right-angled triangles are congruent if in one of them are congruent with their corresponding elements in the other triangle.

31) In the right-angled triangle , the area of the square set up the hypotenuse equals

35) The two adjacent angles formed by intersecting a straight line and a ray whose start point lies on the straight line are

38) A rectangle of length 4 cm. and width 3 cm , then the area of the square set its diagonal equals cm^2

Solution:

1) 360°

2) $90^\circ + 72^\circ = 18^\circ$

3) $m(\angle C) = 180^\circ - (50^\circ + 60^\circ) = 70^\circ \therefore m(\angle Z) = m(\angle C) = 70^\circ$

4) Congruent

7) $360^\circ - 150^\circ = 210^\circ$

9) Straightline

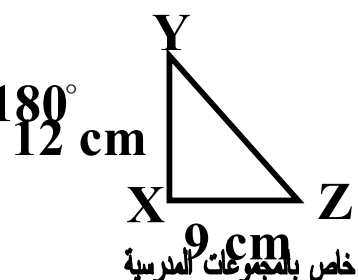
10) $180^\circ \div 2 = 90^\circ$

11) 180°

13) obtuse

14) The included angle

16) $90^\circ < \text{the measure of the obtuse angle} < 180^\circ$



$$17) (YZ)^2 = 12^2 + 9^2 = 225$$

$$19) YZ$$

$$20) 180^\circ \div 3 = 60^\circ \quad \therefore m(\angle B) = 60^\circ$$

$$26) AC^2 = 13^2 = 169, AB^2 + BC^2 = 13^2 + 5^2 = 169$$

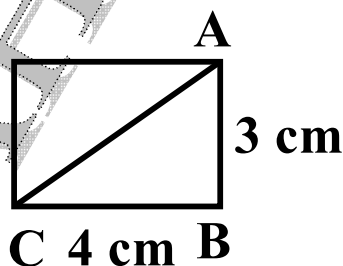
$$\therefore AC^2 = AB^2 + BC^2 \quad \therefore \angle B \text{ is right}$$

27) The hypotenuse and one side

31) The sum of the squares described on the other two sides

35) Supplementary

$$38) 3^2 + 4^2 = 25$$



[1] In each of the following figures, show if the two triangles are congruent or not if they are congruent name the case of congruence.

Figure (1)

$$\triangle ADC \equiv \triangle CAB$$

where :

$$1) AD = BC$$

2) \overline{AC} is a common side

$$3) DC = AB$$

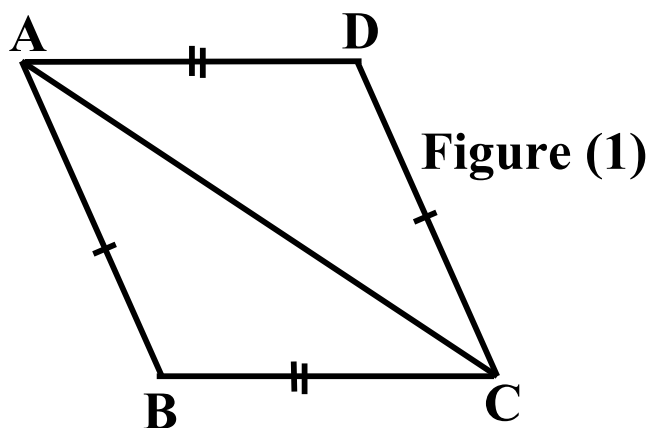


Figure (2)

$$\triangle ADC \equiv \triangle ADB$$

where :

- 1) $AC = AB$
- 2) \overline{AD} is a common side
- 3) $DC = DB$

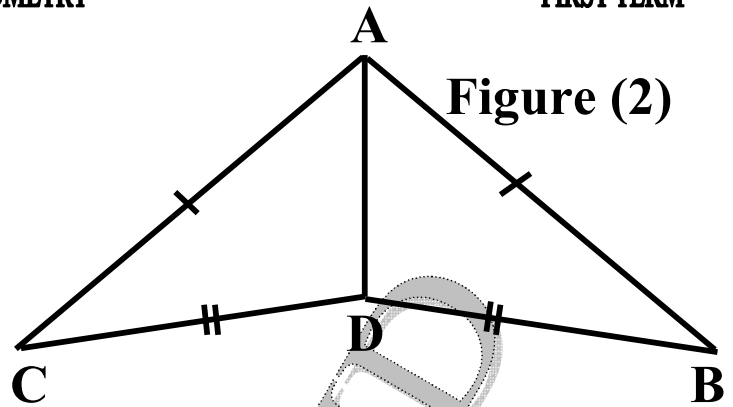


Figure (3)

$$\triangle AOB \equiv \triangle COD$$

where :

- 1) $AO = CO$
- 2) $m(\angle AOB) = m(\angle DOC)$
- 3) $OB = OD$

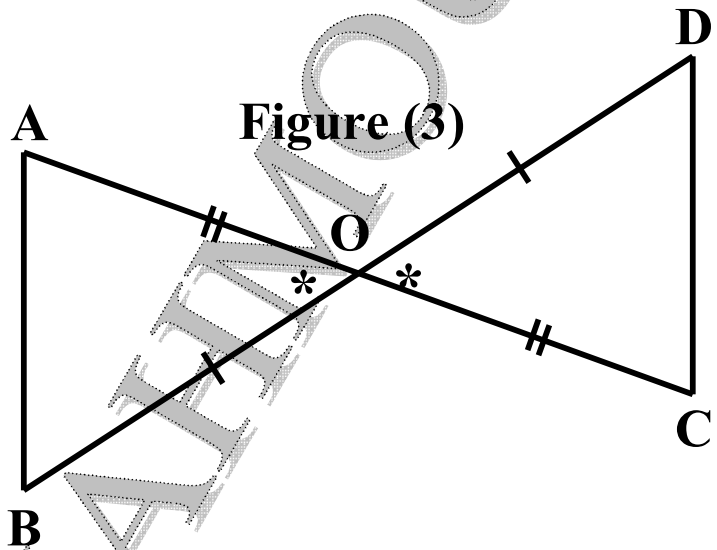


Figure (4)

$$\triangle ADB \equiv \triangle CBD$$

where :

- 1) $AB = DC$
- 2) \overline{BD} is a common side
- 3) $m(\angle BAD) = m(\angle BCD) = 90^\circ$

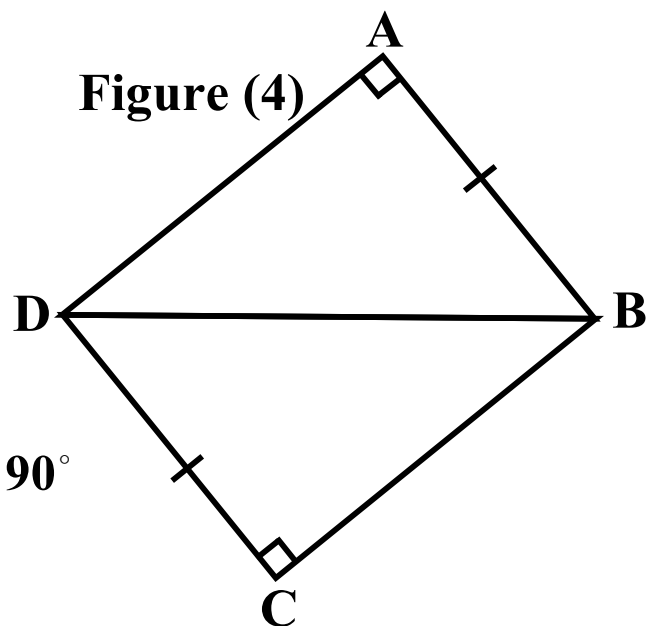


Figure (5)

$$\triangle ADB \equiv \triangle ADC$$

where :

$$1) DB = DC$$

2) \overline{BA} is a common side

$$3) m(\angle BDA) = m(\angle CDA)$$

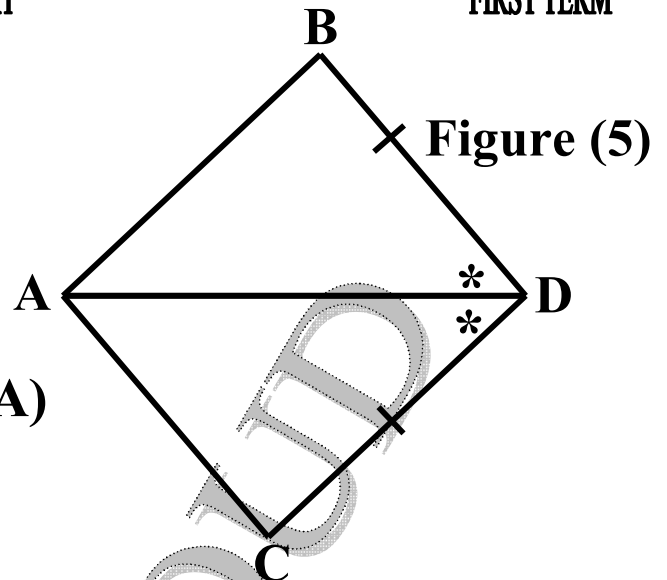


Figure (6)

$$\triangle POR \equiv \triangle OPS$$

where :

$$1) PR = OS$$

2) \overline{PO} is a common side

$$3) m(\angle POR) = m(\angle OPS) = 90^\circ$$

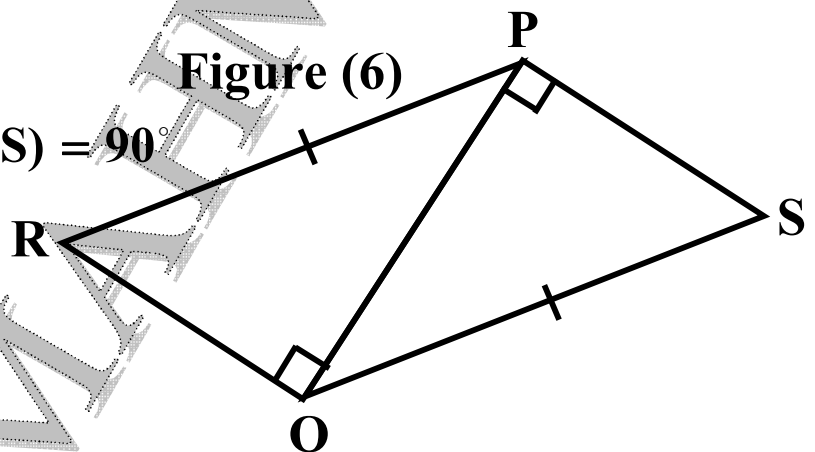


Figure (7)

The two triangles are not congruent

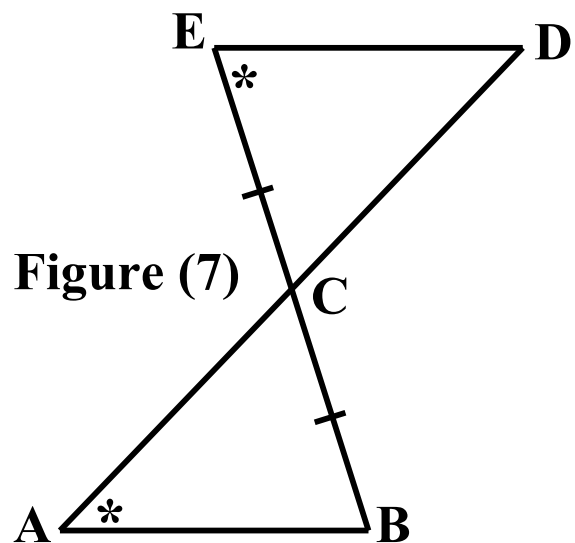


Figure (7)

Figure (8)

$$\triangle DEB \equiv \triangle AEC$$

where :

- 1) $DE = AE$
- 2) $BE = CE$
- 3) $m(\angle DEB) = m(\angle AEC)$

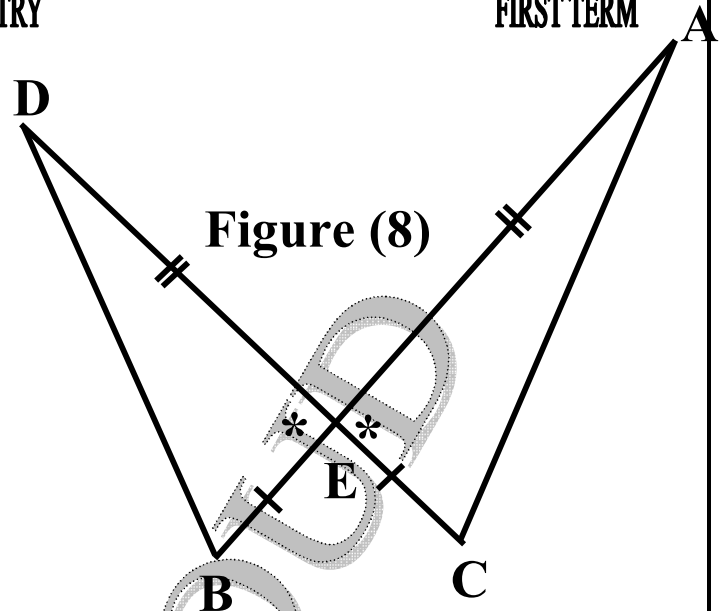


Figure (9)

$$\triangle ADC \equiv \triangle ABC$$

where :

- 1) $AD = AB$
- 2) $DC = BC$
- 3) \overline{AC} is a common side

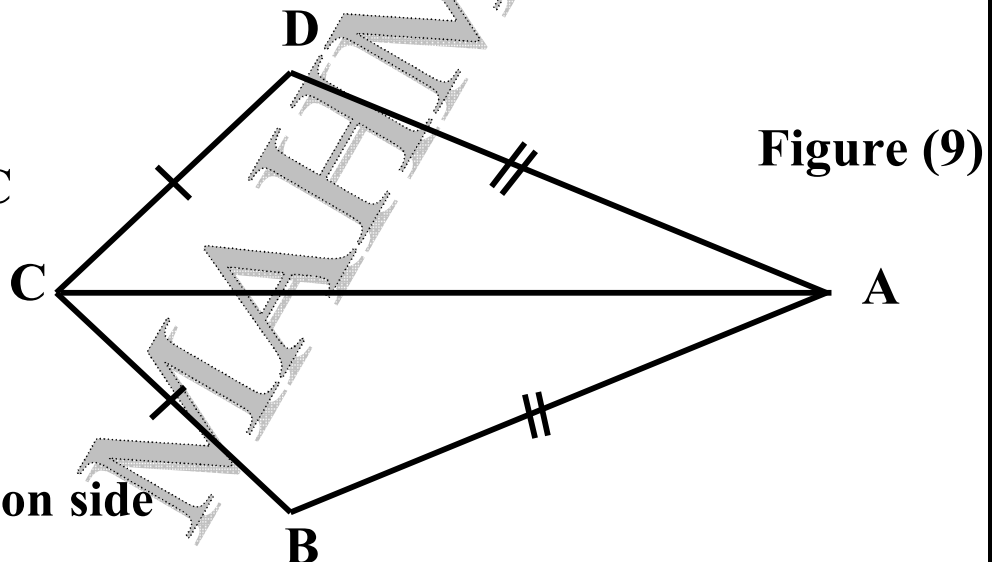


Figure (10)

$$\triangle FDE \equiv \triangle ABC$$

where :

- 1) $FD = AB$
- 2) $m(\angle FDE) = m(\angle ABC)$
- 3) $m(\angle DFE) = m(\angle BAC)$

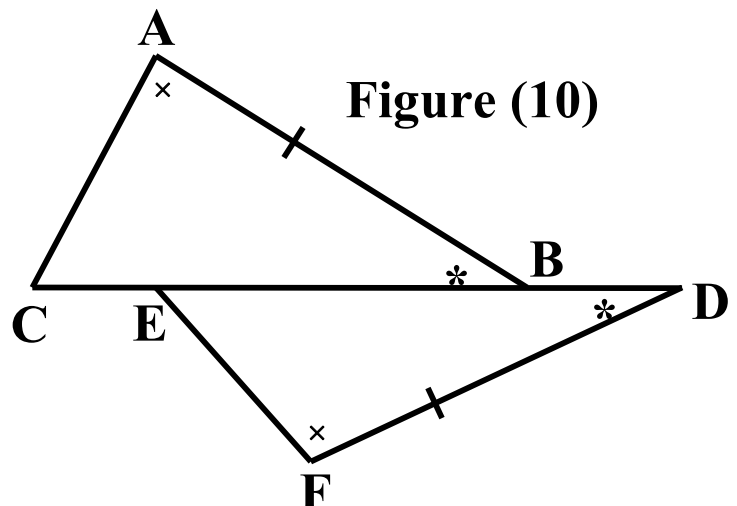


Figure (11)

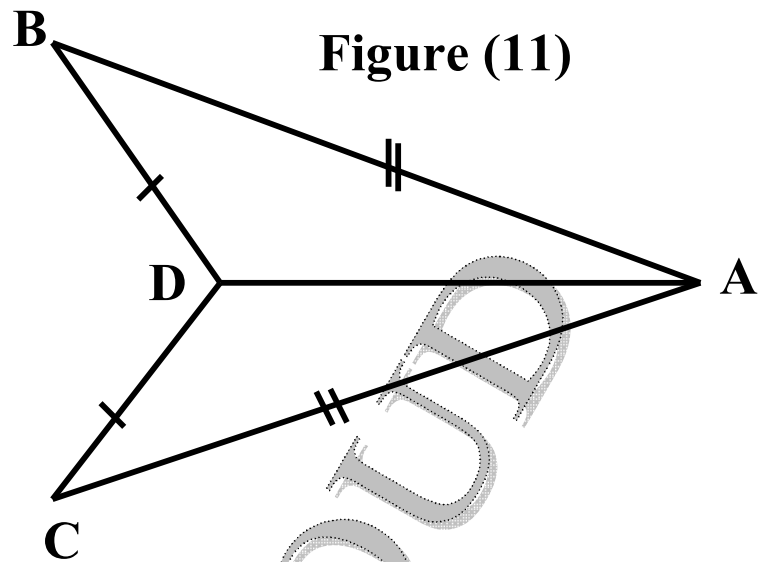
$$\triangle ABD \equiv \triangle ACD$$

where :

1) $AB = AC$

2) $BD = CD$

3) \overline{AD} is a common side



MR. MAHMOUD

Geom.

Sheet (1)

[1] Mention the type of angle whose measure is as following :

- | | | |
|----------------|---------------------|------------------------|
| 1) 57° | 2) 117° | 3) 90° |
| 4) 180° | 3) $43 \frac{1}{2}$ | 6) $89^\circ 59' 60''$ |
| | | 7) $179^\circ 62'$ |

[2] Complete :

- 1) The angle is
- 2) The measure of straight angle
- 3) The measure of zero angle
- 4) The measure of right angle
- 5) The measure of acute angle is less thanand more than
- 6) The measure of obtuse angle is less than more than
- 7) The two complement angles are two angles whose sum of their measure is
- 8) The two supplement angles are the two angles whose sum of their measure is
- 9) The two adjacent angles formed by straight line and ray with same stating point are
- 10) If the two outer sides of two adjacent angles are perpendicular , then these two adjacent angles are
- 11) If the two outer sides of two adjacent angles are on the same straight line , then these adjacent angles are
- 12) The measure of angle which complement with 48° is
- 13) The measure of angle which complement with 90° is
- 14) The measure of angle which complement with $60^\circ \frac{1}{4}$ is
- 15) Measure of angle which supplementary with 90° isangle .
- 16) Measure of angle which supplementary with 180° isangle .

17) Measure of angle which supplementary with 48° .

18) If two straight lines intersect then the measure of each two vertically opposite angle are

19) The sum of measure of accumulative angles at point

20) Angle bisector is

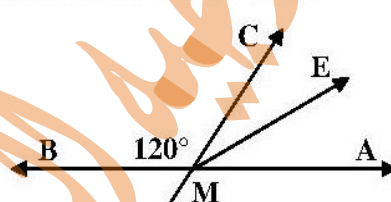
21) If $m(\angle A) = 80$ then (reflex $\angle A$) = $^\circ$

22) In opposite figure :

a) M is the point intersection of \overleftrightarrow{AB} and \overleftrightarrow{CD} , \overrightarrow{ME} bisects $\angle AMC$ and

$m(\angle BMC) = 120^\circ$. Find :

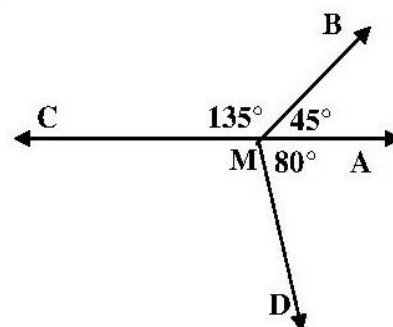
$m(\angle AMC)$, $m(\angle AMD)$, $m(\angle AME)$



b) In the figure :

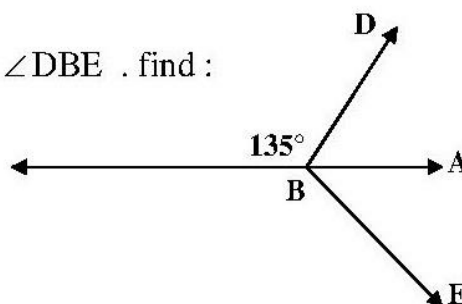
1) $m(\angle CMD) = \dots\dots\dots^\circ$

2)andlie on the same straight line .



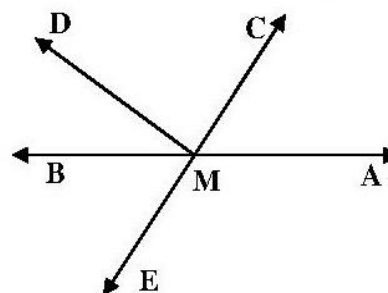
c) If $B \in \overleftrightarrow{AC}$, $m(\angle DBC) = 135^\circ$ and \overrightarrow{BA} bisects $\angle DBE$. find :

$m(\angle ABD)$, $m(\angle DBE)$, $m(\angle CBE)$



d) If $\overleftrightarrow{AB} \cap \overleftrightarrow{CE} = \{M\}$, $\overrightarrow{MD} \perp \overrightarrow{CE}$ and \overrightarrow{MB} bisects $\angle DME$. Find :

$m(\angle BME)$, $m(\angle DME)$, $m(\angle AMC)$, $m(\angle AME)$



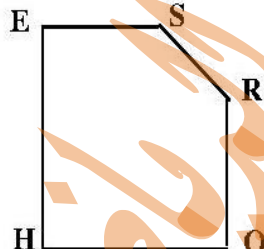
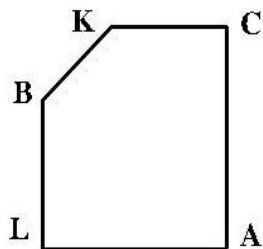
Sheet (2)

[1] Complete :

- 1) The two line segment are congruent if
- 2) The two angles are congruent if
- 3) The two square are congruent if
- 4) The two rectangle are congruent if

[2] In the opposite figure :

The two pentagons shown are congruent



Complete :

- 1) B correspond to
- 2) The polygon BLACK is congruent the polygon
- 3) KB = cm.
- 4) $m(\angle E) = m(\angle \dots)$
- 5) CA =cm
- 6) $m(\angle A) = m(\dots)$

[3] In the opposite figure :

If $C \in BD$, $m(\angle AFC) = 110^\circ$, $BC = 5$ cm and polygon ABCF \cong the polygon EDCF
 $ED = 8$ cm , $EF = 4$ cm .

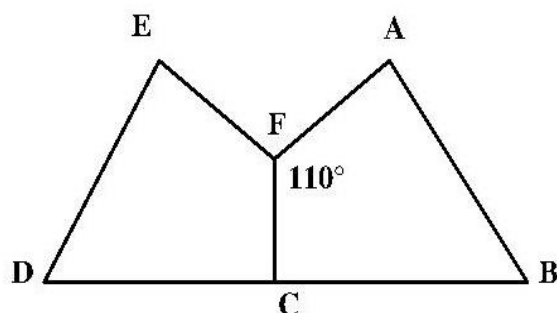
Complete :

$m(\angle EFC) = \dots$

DC =cm

AB =

AF =



Sheet (3)

- 1) Draw the line segment whose length 7 cm. then divid it into two equal parts in length using the compass and the an scaled ruler .
- 2) Draw $\angle ABC$ where $m(\angle B) = 80^\circ$ using the ruler and compasses bisect $\angle B$ by \overrightarrow{BD}
- 3) Use the ruler and compasses to draw the equilateral $\triangle ABC$ of side 6 cm . Draw $\overline{AD} \perp \overrightarrow{BC}$ where $\overrightarrow{AD} \cap \overline{BC} = \{D\}$. what the length of \overline{AD} .
- 4) Draw $\angle XYZ$ whose measure 70° use ruler and draw congruent equal to it .
- 5) Using the protractor , draw $\angle ABC$ with measure 70° and on the other side of BA , draw using ruler and compasses draw $\overrightarrow{AE} \parallel \overrightarrow{BC}$.

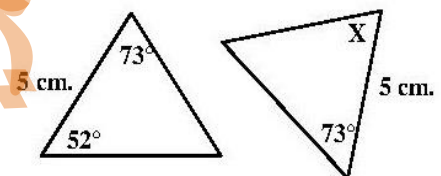
Sheet (4)

[1] Complete the following :

- 1) Any two triangles are congruent if two sides
- 2) Any two triangles are congruent if two angles andin one of the triangles are congruent to their corresponding element in the other .
- 3) Any two triangles are congruent if eachis congruent to its corresponding side in the other triangle .
- 4) Any two right – angled triangles are congruent if
- 5) The diagonal of the rectangle divides its surface into twotriangles .
- 6) If $\triangle ABC \equiv \triangle XYZ$, then $AB = \dots\dots\dots$ and $m(\angle Z) = m(\angle \dots\dots\dots)$

[2] In the opposite figure :

These triangles are congruent , then $X = \dots\dots\dots^\circ$



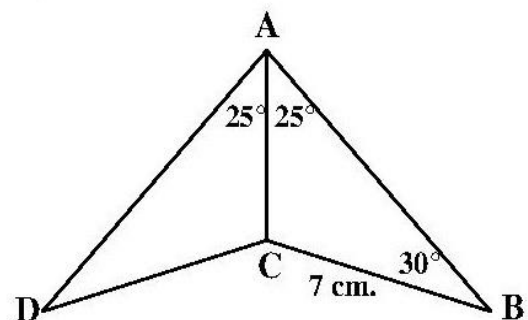
[3] In the opposite figure :

If $AB = AD$, $BC = 7 \text{ cm.}$, $m(\angle BAC) = m(\angle DAC) = 25^\circ$ and $m(\angle B) = 30^\circ$

Complete the following :

If $\triangle ACB \equiv \triangle ACD$

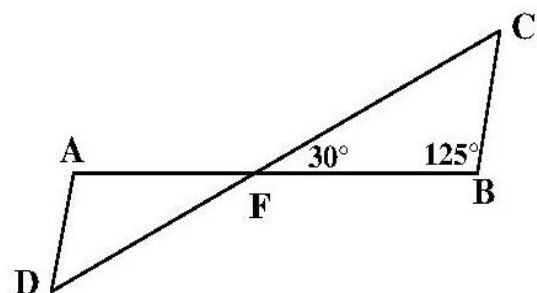
- 1) $m(\angle D) = \dots\dots\dots^\circ$
- 2) $CD = \dots\dots\dots \text{cm.}$
- 3) $m(\angle ACD) = \dots\dots\dots^\circ$



[4] In the opposite = {F} , $FA = FB$, $CF = FD$,

$m(\angle CFB) = 30^\circ$ and $m(\angle B) = 125^\circ$,

Then $m(\angle D) = \dots\dots\dots^\circ$

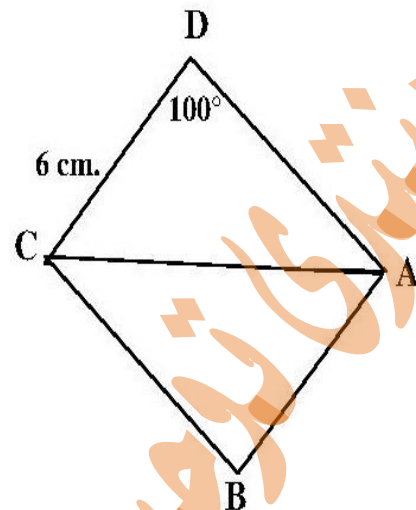


[5] In the opposite figure :

If \overleftrightarrow{AC} bisects $\angle DCB$, $\angle DAB$, $m(\angle D) = 100^\circ$

And $DC = 6$ cm. complete the following :

- 1) $\triangle ADC \equiv \triangle \dots\dots\dots$
- 2) $m(\angle B) = \dots\dots\dots$
- 3) $BC = \dots\dots\dots$ cm .

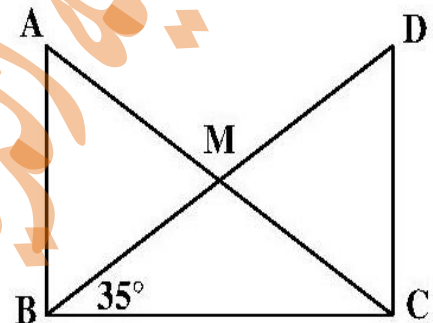


[6] In the opposite figure :

$AB = CD$, $m(\angle DBC) = 35^\circ$,

$\overline{AB} \perp \overline{BC}$ and $\overline{DC} \perp \overline{BC}$,

Then $m(\angle BMC) = \dots\dots\dots$



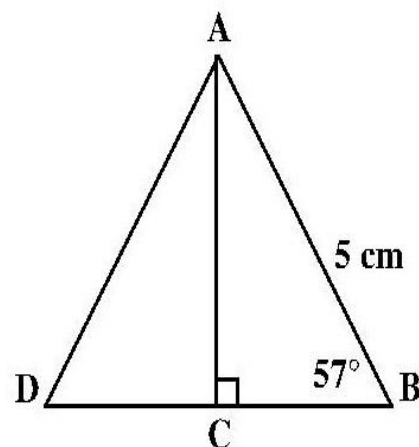
[7] In the opposite figure :

C is the midpoint of \overline{BD} , $\overline{AC} \perp \overline{BD}$,

$AB = 5$ cm. , and $m(\angle B) = 57^\circ$

Find :

- 1) The length of \overline{AD}
- 2) $m(\angle DAC)$

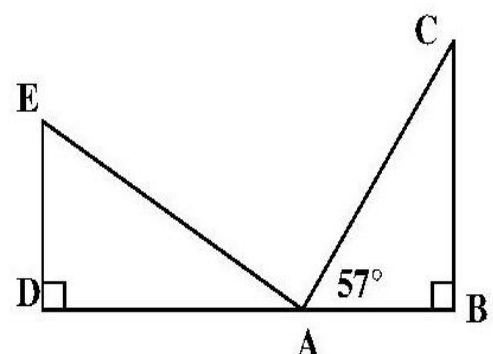


[8] In the opposite figure :

$BC = AD$, $AC = AE$

And $m(\angle CAB) = 57^\circ$

Find the measures of the unknown angles in $\triangle ADE$



Sheet (5)

[1] Complete the following :

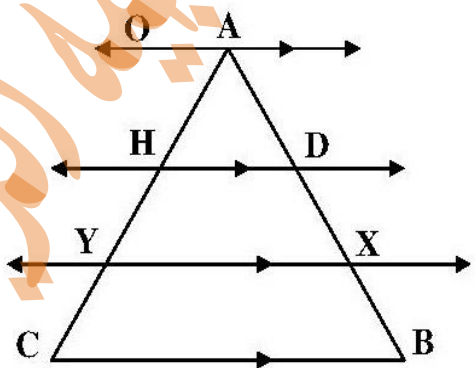
- 1) If two straight lines are parallel to a third straight line , then they are
- 2) If a straight line cuts two parallel straight lines , then each two corresponding angles are
- 3) If a straight line cuts two parallel straight lines , then each two interior angles in the same side of the transversal are

[2] In the opposite figure :

$\overleftrightarrow{AO} \parallel \overleftrightarrow{HD} \parallel \overleftrightarrow{YX} \parallel \overleftrightarrow{CB}$

, $AD = DX = XB$ and $AC = 18$ cm.

Find the length of AY



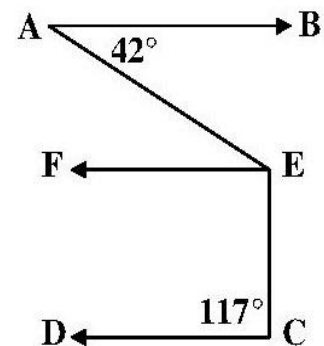
[3] In the opposite figure :

$\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$, $\overleftrightarrow{EF} \parallel \overleftrightarrow{CD}$

, $m(\angle A) = 42^\circ$ and $m(\angle C) = 117^\circ$

Determine :

$m(\angle AEC)$



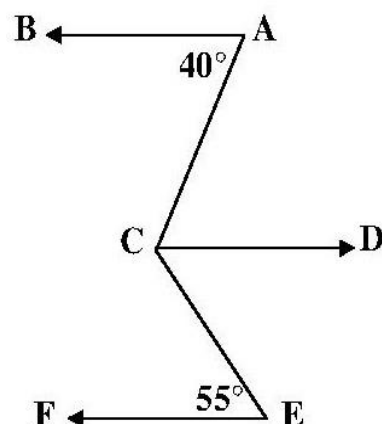
[4] In the opposite figure :

$m(\angle A) = 40^\circ$, $m(\angle E) = 55^\circ$

$\overleftrightarrow{AB} \parallel \overleftrightarrow{EF}$ and $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$

Find :

$M(\angle ACE)$

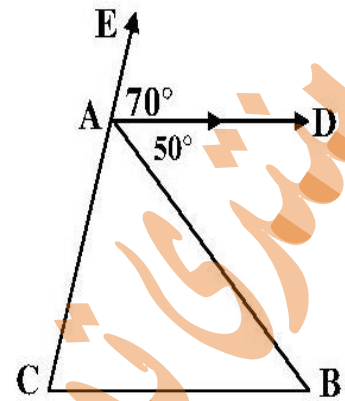


[5] In the opposite figure :

$\overrightarrow{AD} \parallel \overrightarrow{BC}$, $E \in \overrightarrow{CA}$,

$m(\angle DAE) = 70^\circ$ and $m(\angle DAB) = 50^\circ$

Find the measures of the triangle ABC



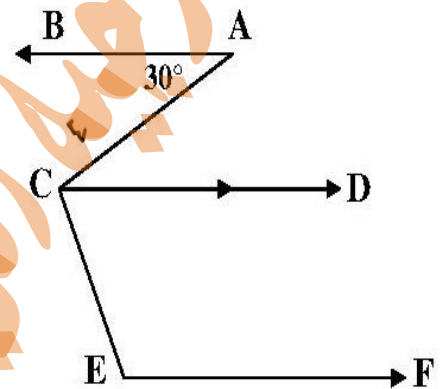
[6] In the opposite figure :

$\overrightarrow{AB} \parallel \overrightarrow{CD} \parallel \overrightarrow{EF}$, $m(\angle A) = 35^\circ$ and

\overrightarrow{CD} bisects $\angle ACE$

Find :

- 1) $m(\angle DCE)$
- 2) $m(\angle CEF)$

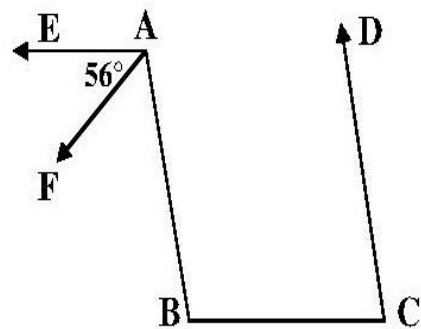


[7] In the opposite figure :

$\overrightarrow{AE} \parallel \overrightarrow{CB}$, $\overrightarrow{BA} \parallel \overrightarrow{CD}$,

\overrightarrow{AF} bisects $\angle BAE$ and $m(\angle EAF) = 56^\circ$

Find : $m(\angle C)$



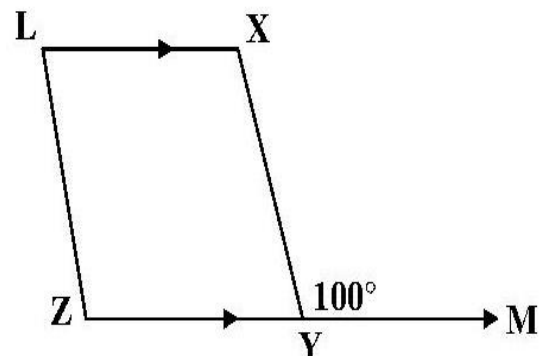
[8] In the opposite figure :

$\overrightarrow{XL} \parallel \overrightarrow{YZ}$, $\overrightarrow{XY} \parallel \overrightarrow{LZ}$ and $m(\angle XYM) = 100^\circ$

Where $M \in \overrightarrow{ZY}$

Find :

- 1) $m(\angle X)$
- 2) $m(\angle Z)$
- 3) $m(\angle L)$



Geometric concepts

The line segment



The straight line



The ray



[1] In the opposite figure :



A , B ,C and D are points lying on one line , $AD \cap BE = \{B\}$

Complete each of the following by using \in , \notin , \subset or \supset :

1) A \overrightarrow{DC}

2) C \overleftrightarrow{AB}

3) \overline{DC} \overleftrightarrow{AB}

4) A $\angle EBC$

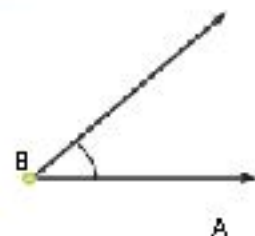
5) AC AD



The angle: is the union of two rays having the same starting point.

*The common point of the two rays is called the **vertex** of the angle. (B)

*Each of the two rays is called a **side** of the angle. (\overrightarrow{BA} , \overrightarrow{BC})



* The Types of angles

1) Zero angle:

- Its measure = 0°



2) Acute angle:

- Its measure is more than 0° and less than 90°



3) Right angle:

- Its measure = 90°



4) Obtuse angle:

- Its measure is more than 90° and less than 180°



5) Straight angle:

- Its measure = 180°



6) Reflex angle:

- Its measure is more than 180° and less than 360°



[1] Mention the type of each of the following angles:

- a) 57°
- b) 90°
- c) 89°
- d) 270°
- e) 0°
- f) $90\frac{1}{2}^\circ$
- g) $65^\circ 15'$
- h) $89^\circ 70'$



Remark

In the opposite figure :

$$m(\angle QOD) + m(\text{reflex } \angle QOD)$$

$$120^\circ + 240^\circ = 360^\circ$$

[2] complete:

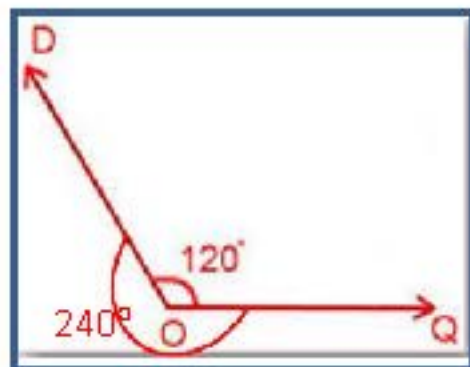
- a) The angle whose measure is 25° , its type is
- b) The angle whose measure is $179^\circ 60'$, its type is
- c) If $m(\angle B) = 160^\circ$, then $m(\text{reflex } \angle B) = \dots\dots\dots^\circ$

[3] Draw the following angles :

a) 115°

b) 80°

c) 300°



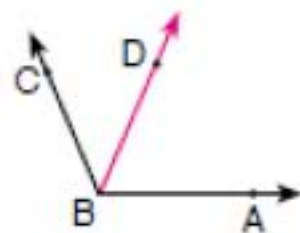
* Some relations between the angles

1) Adjacent angles:

Two angles are said to be adjacent if they have:

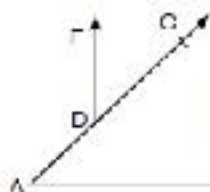
a common vertex,

a common side and the other two sides are on opposite sides of the common side.

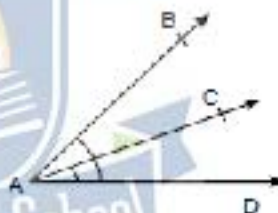


$\angle ABD$, $\angle DBC$ are adjacent

[1] Which of the following angles are adjacent ? (give reason)



$\angle BAC$ and $\angle EDC$

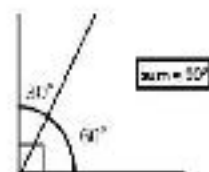


$\angle BAC$ and $\angle BAD$



Complementary angles:

Two angles are said to be complementary if their sum is 90° .



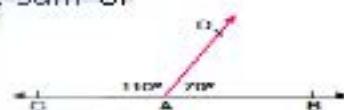
complementary angles

[2] Complete:

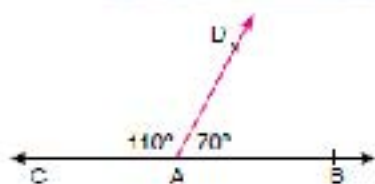
- 1) The angle of measure 40° complements angle of measure $^\circ$
- 2) The acute angle complementsangle
- 3) Zero angle is complemented byangle

Supplementary angles:

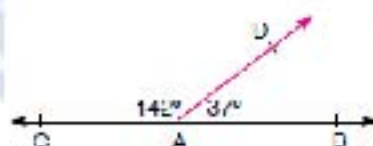
Two angles are said to be supplementary if the sum of their measure is 180°



[3] Which of the following represent supplementary angles? Give reason.



(1)



(2)

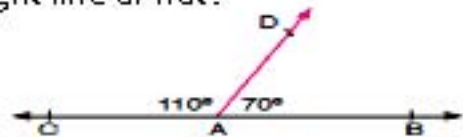
[4] Complete:

- 1) The angle of measure 80° supplements angle of measure
- 2) The obtuse angle supplements angle.



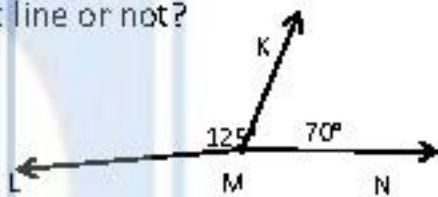
[5] In the opposite figure:

Find if: $\angle CAD$ and $\angle BAD$ are on the same straight line or not?



[6] In the opposite figure:

Find if: $\angle KML$ and $\angle KMN$ are on the same straight line or not?

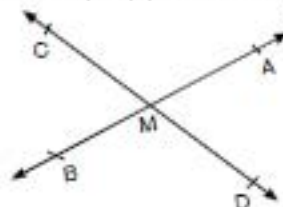


[7] If the ratio between two supplementary angles is 7 : 11, then the measure of the smaller angle is :



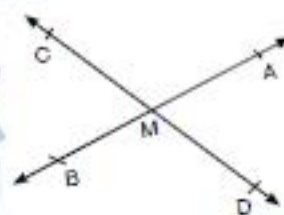
Vertically opposite angles (V.O.A):

If two straight lines intersect, then each two vertically opposite angles are equal in measure



[1] Complete:

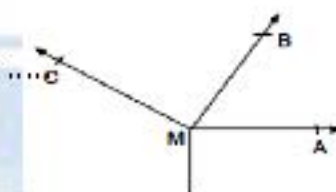
- 1) The angle whose measure is 46° is vertically opposite to an angle whose measure is
- 2) The right angle is vertically opposite angle to
- 3) The two angles AMD, BMC are called



Accumulative angles at a point:

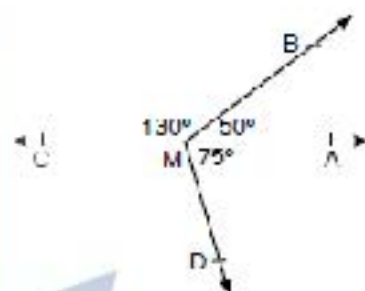
The sum of the measures of the accumulative angles at a point is 360°

1) $m(\angle AMB) + m(\angle BMC) + m(\angle CMD) + m(\angle DMA) = \dots^\circ$



*Find:

$m(\angle CMD) = \dots^\circ$

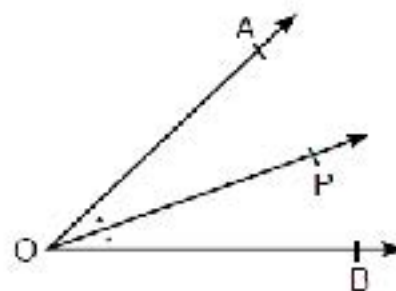


The angle bisector:

It is the ray that divides the angle into two halves
(two equal angles in measure)

[1] \overrightarrow{OP} divides $\angle AOB$ into two angles having the same measure and \overrightarrow{OP} is called the bisector of $\angle AOB$.

Then $m(\angle AOP) = m(\angle BOP)$

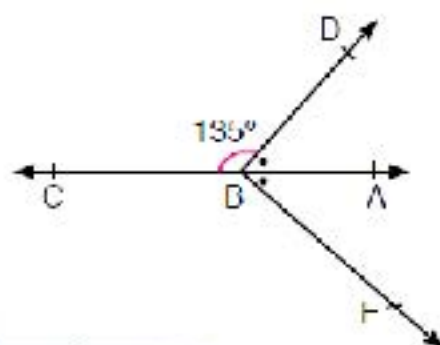


[2] In the figure opposite,

If $B \in AC$, $m(\angle DBC) = 135^\circ$ and

\overrightarrow{BA} bisects $\angle DBE$ find:

$m(\angle ABD)$, $m(\angle DBE)$, $m(\angle CBE)$



.....

.....

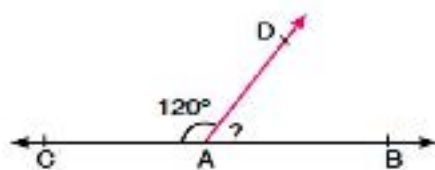
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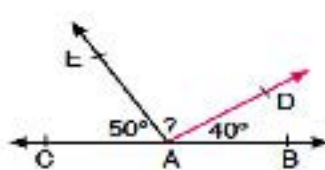


Try by yourself

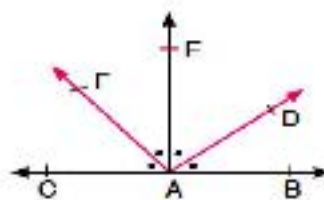
[1] Find the measure of each of the following unknown angles:



$$m(\angle DAB) = \dots\dots^\circ$$

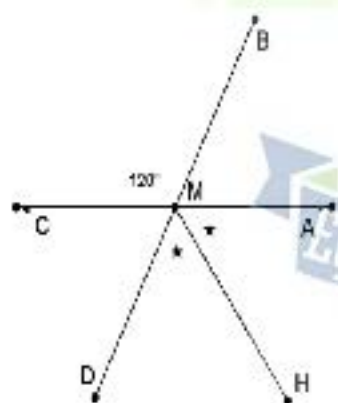


$$m(\angle DAE) = \dots\dots^\circ$$

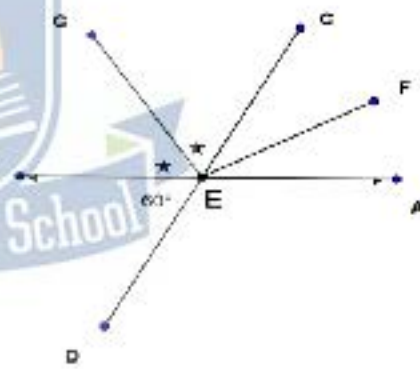


$$m(\angle DAB) = \dots\dots^\circ$$

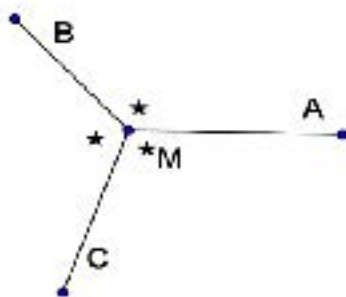
[2] In each of the following figures, find the measure of the required angles:



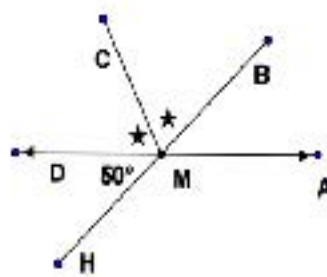
$$m(\angle HMD) = \dots\dots\dots$$



$$m(\angle GEB) = \dots\dots\dots^\circ$$



$$m(\angle AMC) = \dots\dots\dots$$



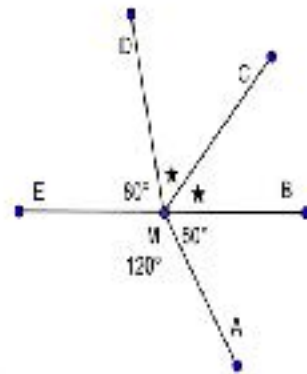
$$m(\angle BMC) = \dots\dots\dots^\circ$$

2) In the opposite figure :

$$m(\angle AMB) = 60^\circ, m(\angle AME) = 120^\circ,$$

$$m(\angle EMD) = 80^\circ$$

→
and MC bisects $\angle BMD$



Find :

1) $m(\angle CMD)$

2) $m(\angle AMC)$

.....

.....

.....

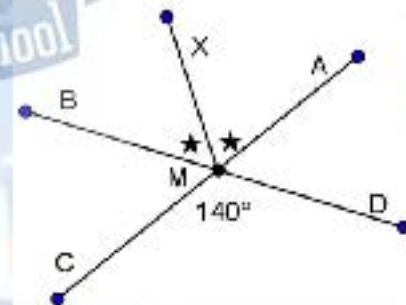
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3) In the opposite figure :

$$\overleftrightarrow{AC} \cap \overleftrightarrow{BD} = \{M\}, MX \text{ bisects } \angle AMB$$

$$\text{and } m(\angle CMD) = 140^\circ$$

$$\text{Find : } m(\angle DMX)$$



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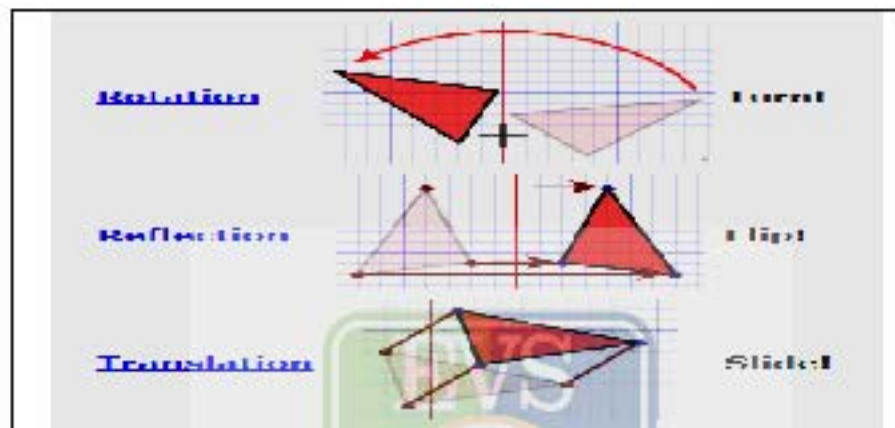
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Congruence



*If one shape can become another using Turns, Flips or Slides, then the shapes are **Congruent**:



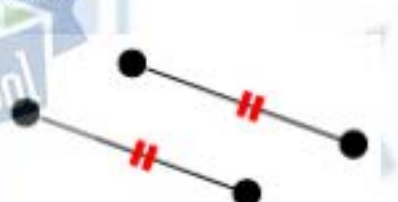
[1] Congruence of two line segments:

*Two line segments are congruent if they are equal in length.

Complete:

1) If $\overline{AB} \equiv \overline{CD}$, Then $AB \dots\dots\dots CD$

2) If $\overline{AB} \equiv \overline{CD}$, Then $AB - CD = \dots\dots\dots$



[3] Congruence of two polygons :

*Two polygons are congruent if there is a correspondence between the vertices such that:

- 1) Corresponding sides are equal in length.
- 2) Corresponding angles are equal in measure.

Example(1):

The polygon BRAKE is congruent to the polygon CHOK, the vertices are written in the same order.

Complete:

CH = , EK =

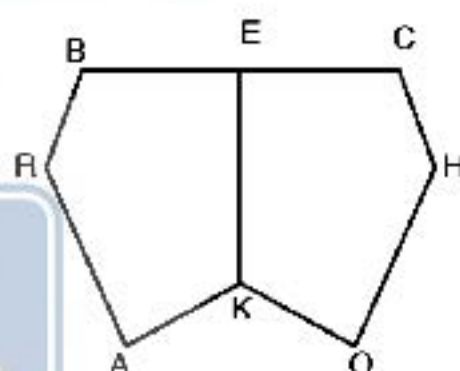
HO = , EC =

KO = , KE is a common side

$m(\angle C) = m(\angle \dots\dots\dots)$, $m(\angle OKE) = m(\angle \dots\dots\dots)$

$m(\angle H) = m(\angle \dots\dots\dots)$, $m(\angle KEK) = m(\angle \dots\dots\dots)$

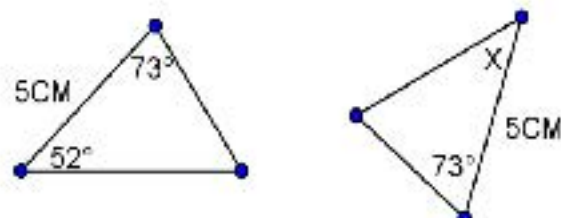
$m(\angle O) = m(\angle \dots\dots\dots)$



Example(2):

In the opposite figure :

These triangles are congruent ,
then $X = \dots\dots\dots^\circ$



Example(3):

a) The diagonal of the rectangle divides its surface into two triangles .

b) If $\triangle ABC \equiv \triangle XYZ$, then $AB = \dots\dots$ and $m(\angle Z) = m(\dots\dots)$

c) If c is the midpoint of \overline{AB} , Then $\overline{AC} \dots\dots\dots \overline{BC}$

d) The two squares are congruent ifare equal .

e) The two rectangles are congruent if are equal.



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Maths

Try by yourself



[1] The polygon BRAKE is congruent to the polygon CHOKE,
the vertices are written in the same order.

***Complete:**

CH = , EK =

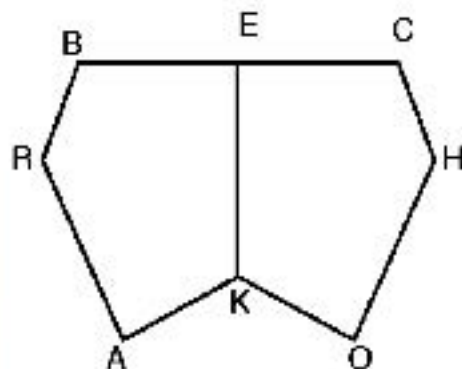
HO = , EC =

KO = , KE is a common side

$m(\angle C) = m(\angle \dots\dots)$, $m(\angle OKE) = m(\angle \dots\dots)$

$m(\angle H) = m(\angle \dots\dots)$, $m(\angle KEC) = m(\angle \dots\dots)$

$m(\angle O) = m(\angle \dots\dots)$



[2] The two pentagons shown are congruent.

Complete

[a] B Corresponds to

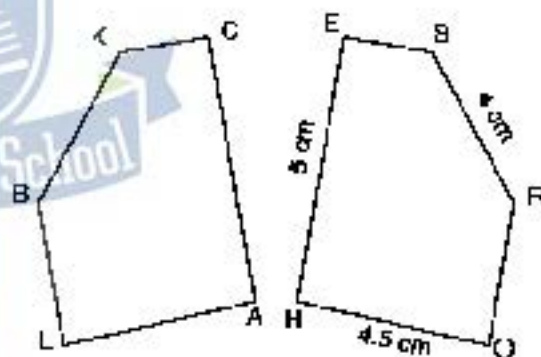
[b] The polygon BLACK is congruent to
the polygon.....

[c] KB = cm.

[d] $m(\angle E) = m(\angle \dots\dots)$

[e] CA =

[f] $m(\angle A) = m(\angle \dots\dots)$



[3] Complete:

a) The diagonal of the rectangle divides its surface into two triangles .

b) If $\triangle ABC \equiv \triangle XYZ$, then AB = and

$m(\angle Z) = m(\dots\dots)$

Congruent Triangles

The first case of congruence of two triangles (side – angle – side) (S.A.S)

Two triangles are congruent if two sides and the included angle of one triangle are congruent to the corresponding parts of the other triangle.

Example 1 :

If $AB = AD$, $BC = 7 \text{ cm}$,

$$m(\angle BAC) = m(\angle DAC) = 25^\circ$$

And $m(\angle B) = 30^\circ$

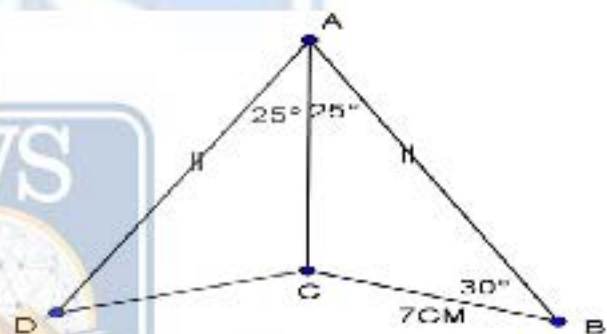
Complete the following :

1) $\triangle ACB \equiv \triangle \dots\dots\dots$

2) $m(\angle D) = \dots\dots\dots$

3) $CD = \dots\dots\dots \text{ cm}$

4) $m(\angle ACD) = \dots\dots\dots$

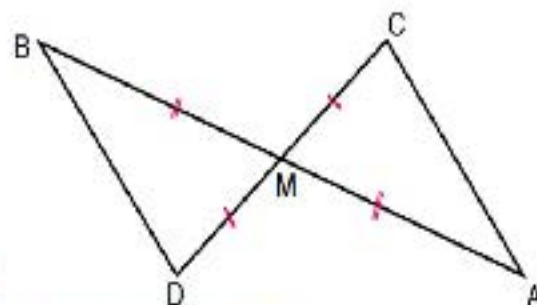


Example 2:

In the figure opposite,

$AB \cap CD = \{M\}$, $AM = BM$, and $CM = DM$.

Does $\triangle AMC \cong \triangle BMD$? why?



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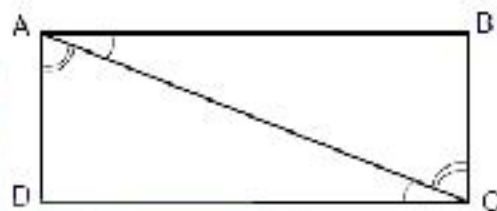
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The second case of congruence of two triangles (angle – side – angle)
(A.S.A)

Two triangles are congruent if two angles and the side drawn between their vertices of one triangle are congruent to the corresponding parts of the other triangle

[1] In the opposite figure:

Find that $\triangle ABC \cong \triangle CDA$



.....

[2] In the opposite figure:

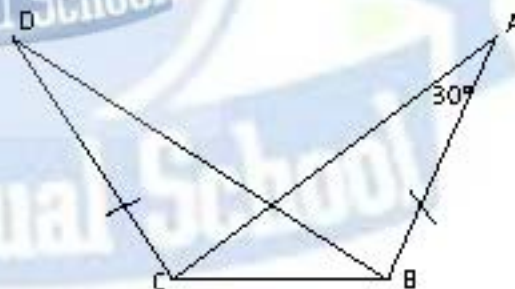
If $AB = DC$, $AC = DB$ and $m(\angle A) = 30^\circ$,

Complete:

1) $\triangle ABC \cong \triangle \dots\dots\dots$

2) $m(\angle D) = \dots\dots\dots^\circ$

3) $m(\angle DBC) = m(\angle \dots\dots\dots)$



Important note

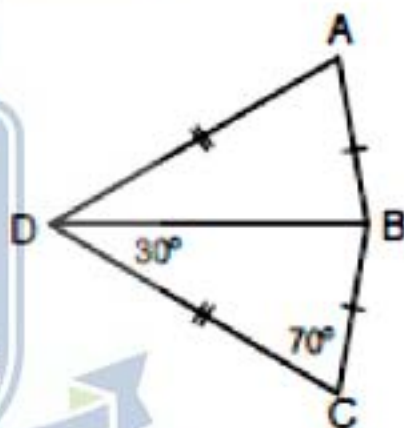
*The diagonal of the rectangle divides its surface into two **congruent** triangles .

[1] mention two cases of congruency of two triangles.

[2] In the figure opposite :

$AB = BC$, $AD = CD$, $m(\angle C) = 70^\circ$,

$m(\angle BDC) = 30^\circ$. find $m(\angle ABD)$.



The third case of congruence of two triangles (side – side – side) (S.S.S)

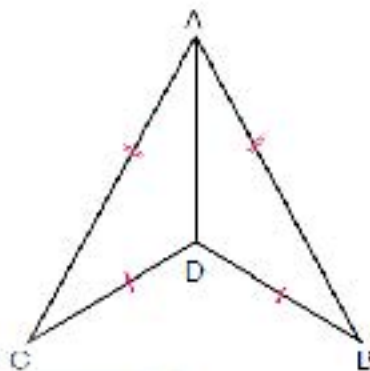
Two triangles are congruent if each side of one triangle is congruent to the corresponding side of the other triangle

[1] In the figure opposite,

$$AB = AC, BD = CD$$

$$\text{Is } \triangle ADB \equiv \triangle ADC$$

verify that: \overrightarrow{AD} bisects $\angle A$



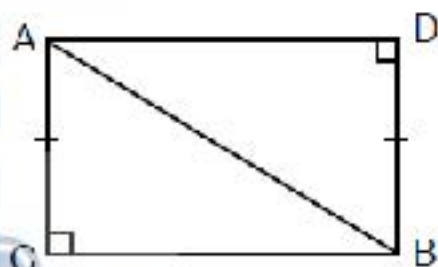
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The fourth case of congruence of two triangles(Hypotenuse and one side in the right – angled triangle R.H.S)

Two right – angled triangles are congruent if the hypotenuse and a side of one triangle are congruent to the corresponding parts of the other triangle

[1] In the figure opposite:

Find the two congruent triangles.



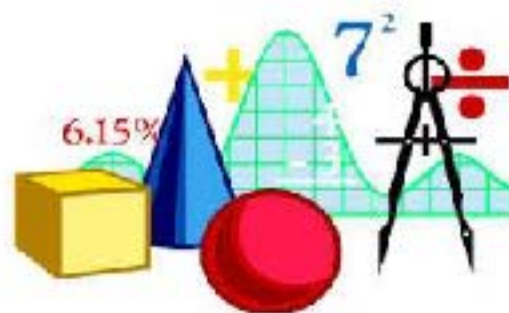
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*** Mark (✓) for the correct statement:**



- [a] Two triangles are congruent if the lengths of sides of one triangle are equal to the corresponding parts of the other.
- [b] Two triangles are congruent if the measures of the angles of one triangle are equal to the measures of the corresponding parts of the other.
- [c] Two right- angled triangles are congruent if the lengths of two sides of One triangle are equal to the corresponding parts of the other triangle.
- [d] Two right- angled triangles are congruent if the length of the hypotenuse and the measure of an angle differs from the right angle are equal to the corresponding parts of the other triangle.
- [e] Two right- angled triangles are congruent if the length of the hypotenuse and the length of a side of one triangle are equal to the corresponding parts of the other triangle.



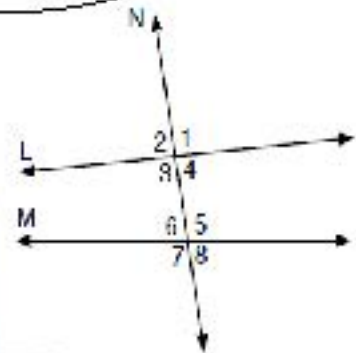
Parallelism

* If a straight line intersects two parallel straight lines, then:

1) Every two alternate angles are equal in measure.

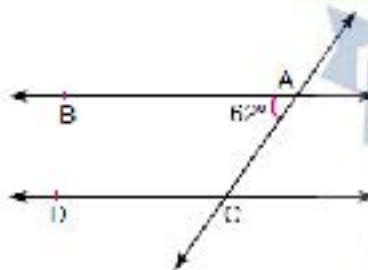
2) Every two corresponding angles are equal in measure.

3) Every two interior angles on one side of the transversal are supplementary.



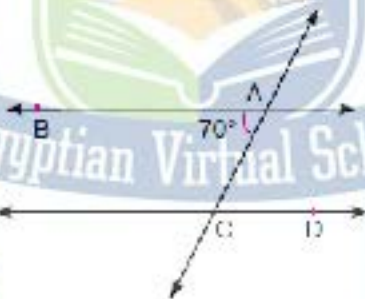
[1] Complete:

a)

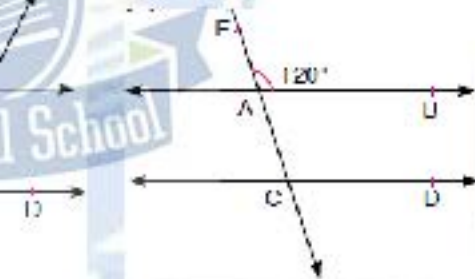


$$m(\angle ACD) = \dots\dots^\circ \quad \dots\dots^\circ$$

b)



$$m(\angle ACD) = m(\angle \dots\dots) = \dots\dots^\circ$$

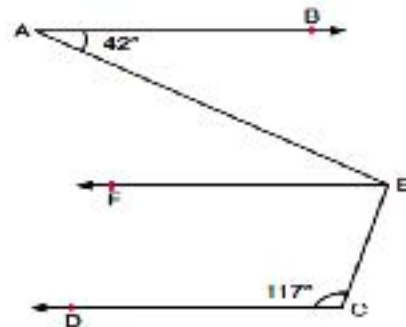


$$m(\angle ACD) = m(\angle \dots\dots) = \dots\dots^\circ$$

[2] In the figure opposite,

$\overrightarrow{AB} \parallel \overrightarrow{CD}$, $\overrightarrow{EF} \parallel \overrightarrow{CD}$,
 $m(\angle A) = 42^\circ$, and $m(\angle C) = 117^\circ$

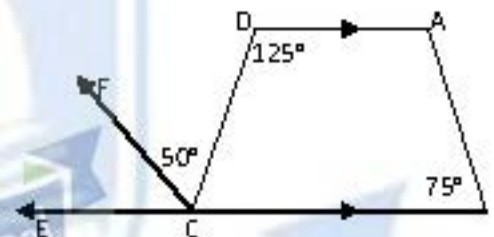
Determine $m(\angle AEC)$



[3] In the opposite figure:

$\overrightarrow{AD} \parallel \overrightarrow{BC}$, $E \in BC$,
 $m(\angle B) = 75^\circ$, $m(\angle D) = 125^\circ$ and $m(\angle DCF) = 50^\circ$

Is $\overrightarrow{AB} \parallel \overrightarrow{CF}$? why?



Try by yourself:



1) If two straight lines are parallel to a third straight line , then they are

2) If a straight line cuts two parallel straight lines , then each two corresponding angles are

3) If a straight line cuts two parallel straight lines , then each two interior angles in the same side of the transversal are

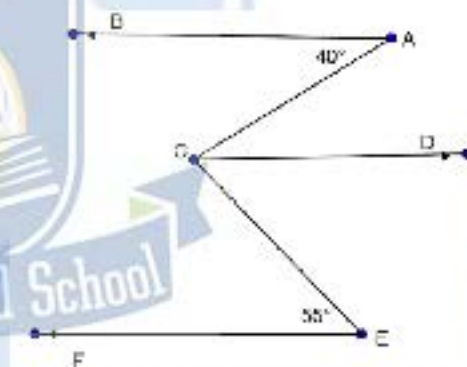
4) In the opposite figure :

$m(\angle A) = 40^\circ$, $m(\angle E) = 55^\circ$

$\overrightarrow{AB} \parallel \overrightarrow{EF}$ and $\overrightarrow{AB} \parallel \overrightarrow{CD}$

Find :

$m(\angle ACE)$



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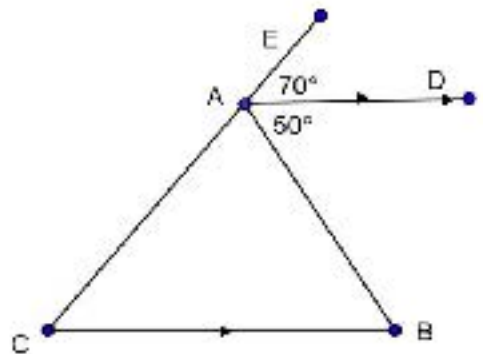
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5- In the opposite figure :

$\overrightarrow{AD} \parallel \overrightarrow{BC}, E \in \overrightarrow{CA},$

$m(\angle DAE) = 70^\circ$ and $m(\angle DAB) = 50^\circ$

Find the measures of the angles of the triangle A B C

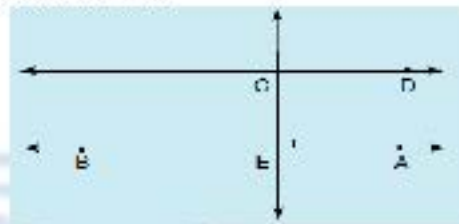


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Important

- 1) A straight line that is perpendicular to one of two parallel lines is also perpendicular to the other.

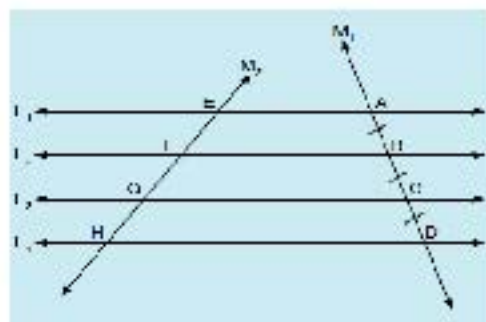


- 2) If each one of two straight lines is perpendicular to a third line in a plane, then the two straight lines are parallel.



- 3) If two straight lines are parallel to a third straight line, then these two straight lines are parallel to each other.

- 4) If Parallel straight lines divide a straight line into segments of equal lengths, then they divide any other straight line into segments of equal lengths



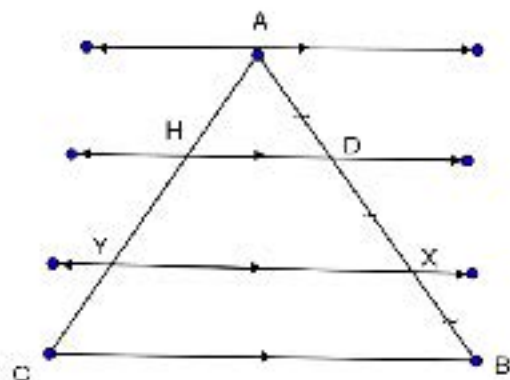
[1] In the opposite figure :

$$\overleftrightarrow{AO} \parallel \overleftrightarrow{HD} \parallel \overleftrightarrow{YX} \parallel \overleftrightarrow{CB}$$

$$AD = DX = XB$$

and $AC = 18 \text{ cm}$.

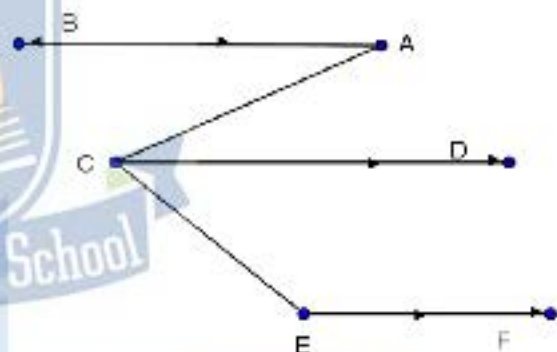
Find the length of \overline{AY}



[2] In the opposite figure :

$$\overleftrightarrow{AB} \parallel \overleftrightarrow{CD} \parallel \overleftrightarrow{EF}, m(\angle A) = 35^\circ \text{ and}$$

\overleftrightarrow{CD} bisects $\angle ACE$



Find :

1) $m(\angle DCE)$

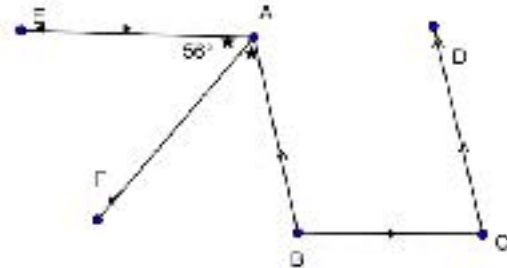
2) $m(\angle CEF)$

[3] In the opposite figure :

$\overline{AE} \parallel \overline{CB}$, $\overline{BA} \parallel \overline{CD}$,

\overrightarrow{AF} bisects $\angle BAE$ and $m(\angle EAF) = 56^\circ$

Find : $m(\angle C)$



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[4] In the opposite figure :

$\overline{XL} \parallel \overline{YZ}$, $\overline{XY} \parallel \overline{LZ}$ and

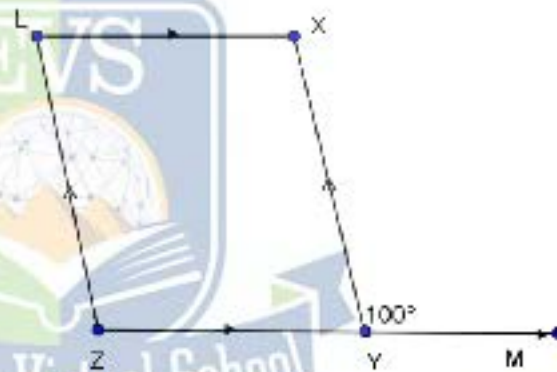
Where $M \in \overrightarrow{ZY}$

Find :

1) $m(\angle X)$

2) $m(\angle Z)$

3) $m(\angle L)$



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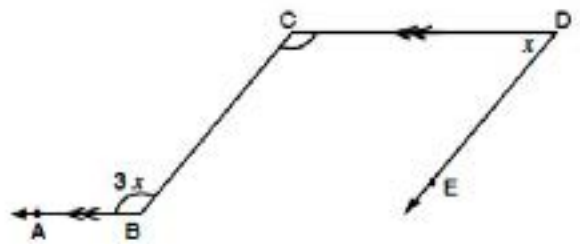
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[5] In the opposite figure, if $\overrightarrow{CD} \parallel \overrightarrow{BA}$ and $\overrightarrow{DE} \parallel \overrightarrow{CB}$, then $x = \dots\dots^\circ$



[6] Find the measure of $(\angle X)$ In each of the following:



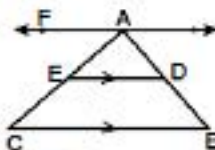
[7] Choose the correct answer:

(1) If two straight lines are on the same plane and do not intersect,
then they are

- (a) skew (b) perpendicular (c) parallel (d) congruent

(2) In the opposite figure :

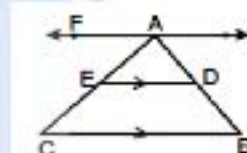
$AD : DB = \dots\dots\dots$



- (a) 1 : 1 (b) 1 : 2 (c) 1 : 3 (d) 1 : 4

(3) In the opposite figure :

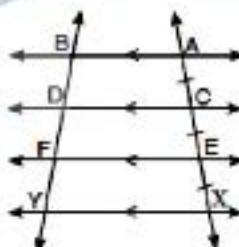
$AD : AB = \dots\dots\dots$



- (a) 1 : 1 (b) 1 : 2 (c) 1 : 3 (d) 1 : 4

(4) In the figure opposite :

If $BF = 2$ cm then $BY = \dots\dots\dots$ cm



Geometric Constructions

1) Using the geometric instruments , draw an angle of measure 120°

and bisect it

(Don't remove the arcs)

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2) Using the geometric instruments , draw an angle of measure 120°

and divide it into four congruent angles

(Don't remove the arcs)

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- 3) Draw an angle whose vertex is A and its measure is 130° , use a ruler and a compasses to divide the angle A into 4 equal angles in measure

(Don't remove the arcs).

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- 4) Using the ruler and the compasses , draw $\triangle ABC$ in which

$AB = AC = 5 \text{ cm}$, $BC = 6 \text{ cm}$, then draw $AD \perp BC$ where

$\overline{AD} \cap \overline{BC} = \{D\}$. Then find the length of AD

(Don't remove the arcs)

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5) Using the ruler and the compasses , draw $\triangle ABC$ in which

$AB = AC = 3\text{ cm}$, $BC = 5\text{ cm}$ then bisect $\angle A$ by the bisector

\overline{AD} where $D \in \overline{BC}$

(Don't remove the arcs).

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5) Using the ruler and the compasses , draw $\triangle XYZ$ in which:

$m(\angle X) = 50^\circ$, $m(\angle Y) = 70^\circ$, then draw $ZL \perp XY$ to cut it at L.

then find:

1) The length of ZL

2) The area of $\triangle XYZ$

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- 6) Using the ruler and the compasses, draw the equilateral triangle ABC of side length 6cm. Bisect each of A, B and C to intersect at M .prove that $MA = MB = MC$

(Don't remove the arcs)

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- 7) Using the geometric instruments, Draw AB where $AB = 6$ cm, Draw the axis of symmetry of AB, take $C \in$ the axis of symmetry and of distance 4 cm from AB.What is the type of ΔABC according to its sides?

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8) Using the ruler and the compasses, Draw $\triangle ABC$ in which

$AB = AC = 5$ cm and $BC = 6$ cm, then draw $\overline{AD} \perp \overline{BC}$ where

$\overline{AD} \cap \overline{BC} = \{D\}$, then find by measuring the length of \overline{AD} .

(Don't remove the arcs)

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Geometric concepts

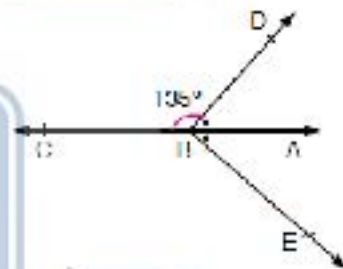
[1] Complete each of the following:

- 3) The angle is
- 4) The measure of the straight angle is° and the measure of zero angle is°
- 5) The measure of the right angle =°
- 6) The measure of the acute angle is less than° and more than°
- 7) The measure of the obtuse angle is less than° and more than°
- 8) The angle whose measure is greater than 180° but less than 360° is called
- 9) The angle whose measure is 179° , its type is
- 10) The two complementary angles are two angles whose sum of their measures is°
- 11) The complements of the equal angles in measure are
- 12) The two supplementary angles are two angles whose sum of their measures is°
- 13) The two adjacent angles formed by a straight line and a ray with a starting point on this straight line are
- 14) If the two outer sides of two adjacent angles are perpendicular then these two angles are
- 15) The two adjacent angles are complementary ,then their outer sides are
- 16) If the two outer sides of two adjacent angles are on the same straight line then these two angles are
- 17) The two adjacent angles are supplementary ,then their outer sides are
- 18) The angle of measure 43° complements angle of measure° and supplements angle of measure°
- 19) The angle of measure complements an angle of measure 50° and supplements angle of measure 140°
- 20) The acute angle complements angle and supplements angle.
- 21) Zero angle is complemented by angle and supplemented by angle.
- 22) The obtuse angle supplements angle.
- 23) If two straight lines intersect, then each two vertically opposite angles are

- 24) The right angle is vertically opposite angle to
- 25) The measure of an angle which equivalent to two right angles= \dots° and it's called
- 26) If: $m(\angle B) = 160^\circ$, then $m(\text{reflex } \angle B) = \dots^\circ$
- 27) If: $\angle A$ supplements $\angle B$ and $\angle A \equiv \angle B$, then $m(\angle B) = \dots^\circ$
- 28) the angle whose measure is 46° vertically opposite to an angle whose measure is
- 29) The sum of the measures of the accumulative angles at a point equals

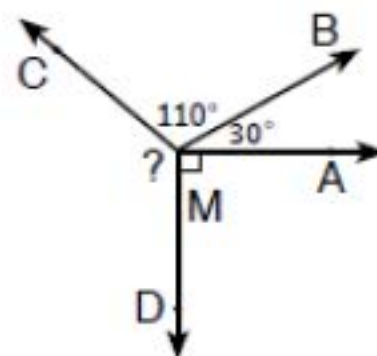
[2] In the figure opposite,

If $B \in AC$, $m(\angle DBC) = 135^\circ$ and
 BA bisects $\angle DBE$ find:
 $m(\angle ABD)$, $m(\angle DBE)$, $m(\angle CBE)$



[3] In the figure opposite :

$m(\angle AMB) = 30^\circ$, $m(\angle BMC) = 110^\circ$ and
 $m(\angle AMD) = 90^\circ$. Find $m(\angle CMD)$.



The congruency & the congruent triangles

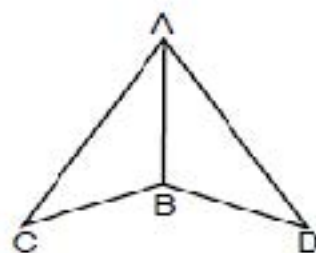
1] Complete each of the following:

-) Two angles are congruent if
-) Two line segments are congruent if
- 3) Two polygons are congruent if
- 4) Two polygons are congruent if there is a correspondence between their vertices such that
- 5) mention two cases of congruency of two triangles.
- 6) The two adjacent angles formed by a straight line and a ray with a starting point on this straight line are
- 7) If: $\overline{AB} \equiv \overline{CD}$, then $AB - CD = \dots\dots\dots$
- 8) If Z is the midpoint of \overline{XY} , then: $\overline{XZ} \dots\dots\dots \overline{YZ}$
- 9) If the ratio between two supplementary angles is 4 : 5, then the measure of the greater angle is
- 10) If $m(\angle A) = 2 m(\angle B)$, $\angle A$ complements $\angle B$, then $m(\angle A) = \dots\dots\dots$
- 1) The two triangles are congruent if
- 2) The two triangles are congruent if two sides and are congruent with their corresponding in the other triangle.
- 3) The two triangles are congruent if two angles and are congruent with their corresponding in the other triangle.
- 4) Two right angled triangles are congruent if
- 5) The diagonal of the rectangle divides its surface into two triangles .
- 6) If the two triangles ABC and DEF are congruent, then : $BC = \dots\dots\dots$, $m(\angle E) = m(\angle \dots\dots\dots)$
- 7) If $DE = XY$, $DF = XZ$ and $m(\angle D) = m(\angle X)$, then $\triangle \dots\dots\dots$, are congruent.
- 8) The two triangles XYZ and MNL are congruent, if $YZ = 8$ cm, $m(\angle Y) = 40^\circ$ then in the other triangle : = 8 cm , $m(\angle \dots\dots\dots) = 40^\circ$
- 9) If $AB = DF = 5$ cm , $AC = DE = 7$ cm , $m(\angle A) = m(\angle D) = 55^\circ$ then the two triangles ABC , DFE are congruent with
- 10) In $\triangle ABC$: if $m(\angle B) = 3 m(\angle A) = 90^\circ$, then $m(\angle C) = \dots\dots\dots$
- 1) $\triangle ABC$ is congruent to $\triangle XYZ$, $m(\angle A) + m(\angle B) = 140^\circ$, then $m(\angle Z) = \dots\dots\dots^\circ$



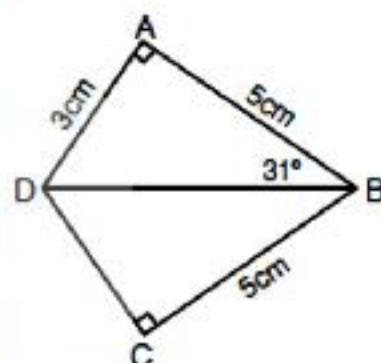
[2] In the figure opposite :

If $\triangle ABC \cong \triangle ABD$ let the perimeter of the figure
 $ACBD = 20$ cm and $AB = 6$ cm,
 then perimeter of $\triangle ABC = \dots\dots\dots$ cm.



[3] In the figure opposite :

$m(\angle BAD) = m(\angle BCD) = 90^\circ$
 $m(\angle ABD) = 31^\circ$,
 $AB = CB = 5$ cm, $AD = 3$ cm



(a) Prove that :

the two triangles ABD and CBD are congruent.

(b) find the length of CD.

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The parallelism



1] Complete each of the following:

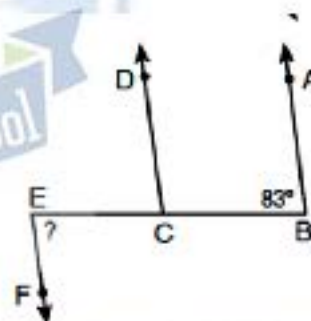
- 1) When a transversal cuts two parallel lines, Then :
The alternate angles are
The corresponding angles are
The interior angles on the same side of the transversal are
- 2) A straight line that is perpendicular to one of two parallel lines is also to the Other.
- 3) A straight line that is parallel to one two parallel lines is also to the other.
- 4) A straight line that is perpendicular to one of two parallel lines is
- 5) The two straight lines perpendicular to a third one are

[2] In the figure opposite :



$BA \parallel CD$, $CD \parallel EF$ and

$m(\angle ABC) = 83^\circ$ find $m(\angle CEF)$.



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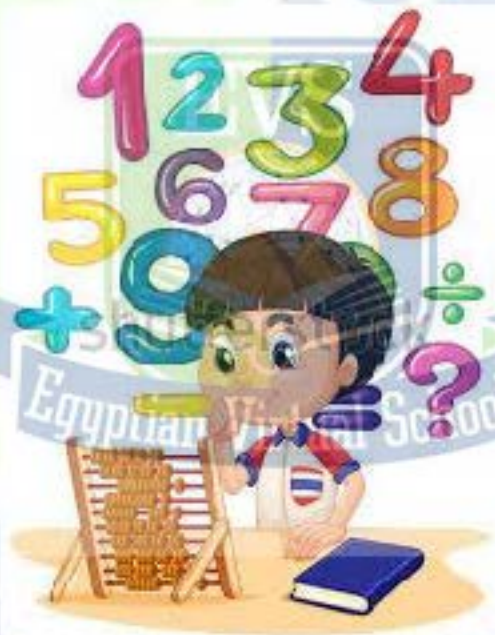
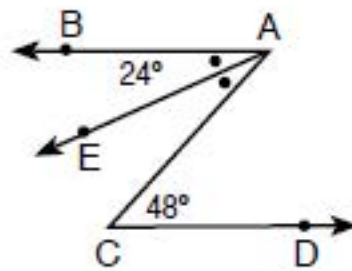
[3] In the figure opposite :

AE bisects $\angle BAC$, $m(\angle BAE) = 24^\circ$

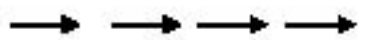
$m(\angle ACD) = 48^\circ$. Complete :

First : $m(\angle BAC) = \dots\dots\dots^\circ$

Second : $\overrightarrow{AB} \parallel \dots\dots\dots$



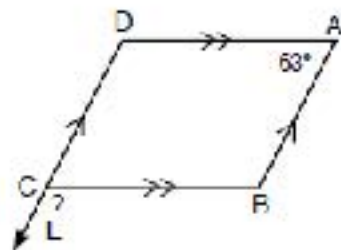
[4] In the figure opposite :



$AB \parallel DC$, $AD \parallel BC$ and

$m(\angle BAD) = 63^\circ$

find $m(\angle BCE)$.

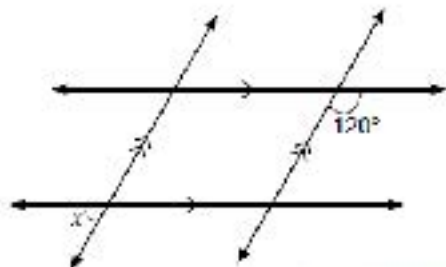


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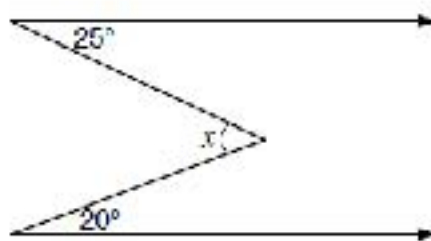


[5] Find the value of x in each figure:

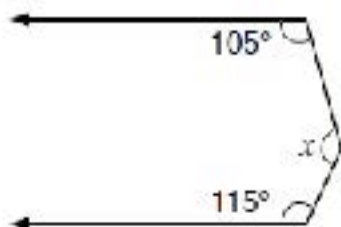
a)



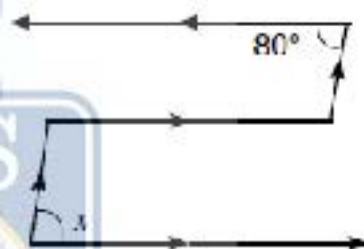
b)



c)



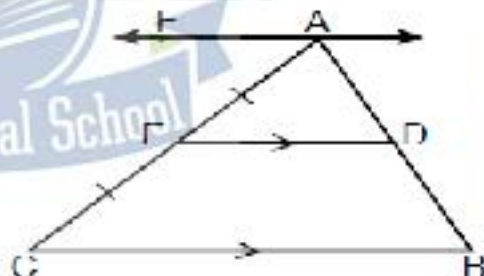
d)



[6] In the figure opposite :

If $AB = 3$ cm

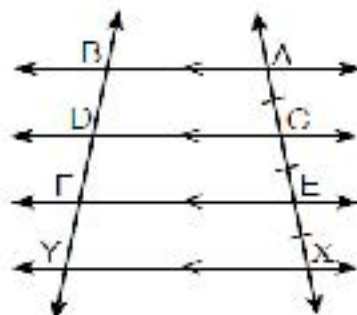
then $BD = \dots\dots\dots$ cm



[7] In the figure opposite :

If $BF = 2$ cm

then $BY = \dots\dots\dots$ cm



Geometric constructions

*Constructing the bisector of a given angle

[1] Draw an angle of measure 80° , then use the compass to bisect it.

(Don't remove arcs)

[2] Draw an angle of measure 120° , then use the compass to divide it

into four equal angles in measure . (Don't remove arcs)

[3] Using the ruler and the compass ,draw the equilateral triangle

ABC of side length 6cm. Bisect each of $\angle A$, $\angle B$, $\angle C$ by bisectors

Intersecting at M , What is the relation between MA, MB and MC?



Summary of geometry

for prep one (1st term)

- 1) The sum of measures of two complementary angles equals 90
- 2) The sum of measures of two supplementary angles equals 180
- 3) The measure of the straight angle is 180
- 4) The measure of the right angle is 90
- 5) The two adjacent angles formed by a straight line and a ray with a starting point on this straight line are supplementary
- 6) The outer sides of the two supplementary adjacent angles are on the same straight line
- 7) If the two adjacent angles are not supplementary, then their outer sides are not on the same straight line
- 8) If the two adjacent angles are complementary, then their outer sides are perpendicular
- 9) The sum of measures of the accumulative angles at a point = 360
- 10) The two adjacent angles in which the two outer sides are on the same straight line are supplementary
- 11) If two straight lines intersect, then each two vertically opposite angles are equal in measure
- 12) In the right angled triangle, the area of the square drawn on its hypotenuse is equal to the sum of the areas of the squares drawn on the other two sides
- 13) The acute angle is supplemented by an obtuse angle
- 14) The right angle is supplemented by a right angle
- 15) If two angles are supplementary, then one of them is an acute and the other is an obtuse or both of them are right angles.

16) Two triangles are congruent :

1- if two sides and the included angle of the first triangle are congruent to their corresponding from the other triangle

2- if two angles and the included side of the first triangle are congruent to their corresponding from the other triangle

3- If each side of the first triangle is congruent to its corresponding from the other triangle

4- The two right angled triangle are congruent if the hypotenuse and a side of one triangle are congruent to their corresponding from the other triangle

17) If a straight line intersects two parallel straight lines then each two alternate angles are equal in measure

18) If a straight line intersects two parallel straight lines then each two corresponding angles are equal in measure

19) If a straight line intersects two parallel straight lines then each two interior angles at one side of the transversal are supplementary

20) If a straight line intersect two straight lines and two alternate angles are equal in measure then the two lines are parallel

21) If a straight line intersect two straight lines and two corresponding angles are equal in measure, then the two lines are parallel

22) If a straight line intersect two straight lines and two interior angles at one side of the transversal are supplementary , then the two lines are parallel

23) If two straight lines are parallel to a third straight line , then the two straight lines are parallel

24) The two perpendicular straight lines to a third line are parallel

25) The perpendicular straight line to one of two parallel straight lines is perpendicular to the other

26) If parallel straight lines divide a straight line into segments of equal lengths, then they divide any other straight line into segments of equal lengths.

27) The supplements of one angle are equal in measures

28) The complements of one angle are equal in measures

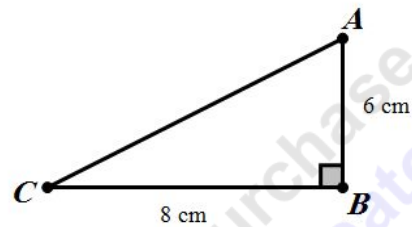
29) The acute angle complements an acute angle

30) If the triangle ABC is right-angled triangle at B, then

$$(AC)^2 = (AB)^2 + (BC)^2$$

$$(AB)^2 = (AC)^2 - (BC)^2$$

$$(BC)^2 = (AC)^2 - (AB)^2$$



Best wishes

Mr/ Gamal Serag

Geometry

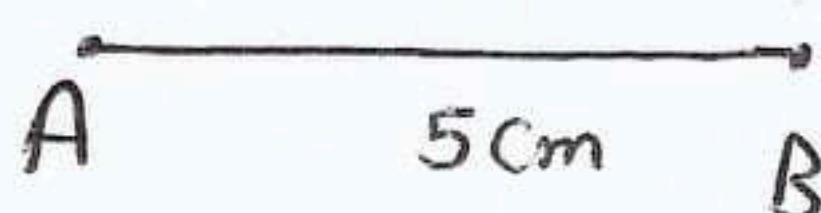
Unit 4 : Geometry and measurement

- ① Geometric concepts and the relations between angles.
- ② Congruence.
- ③ Parallelis.
- ④ Geometric constructions.

① Geometric concepts and the relations between the angles.

* The line segment

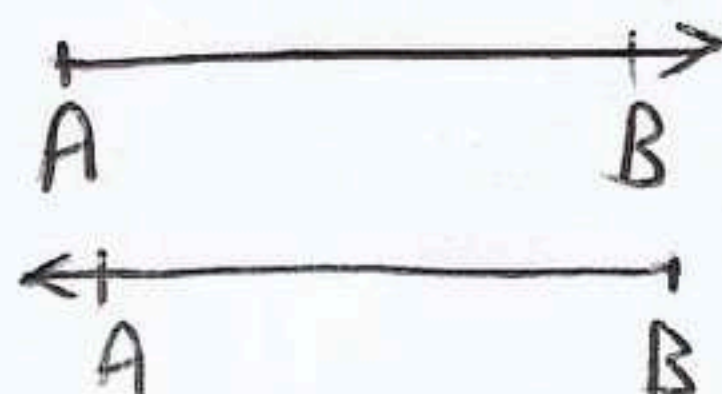
is a set of points consisting of two distinct points and all points between them when we join them by a ruler, it has two end points \overline{AB} or \overline{BA} and its length is 5cm ($AB=5\text{cm}$)



* The ray

is a line segment extended from only one of its terminals without limit, it has a starting point and it hasn't end point

$\overrightarrow{AB} \neq \overrightarrow{BA}$ and it has no length $\overline{AB} \subset \overrightarrow{AB}$



* The straight line

is a line segment extended from both directions infinitely, it has not a starting and hasn't ending point

\overleftrightarrow{AB} or \overleftrightarrow{BA} it has no length. $\overline{AB} \subset \overrightarrow{AB} \subset \overleftrightarrow{AB}$

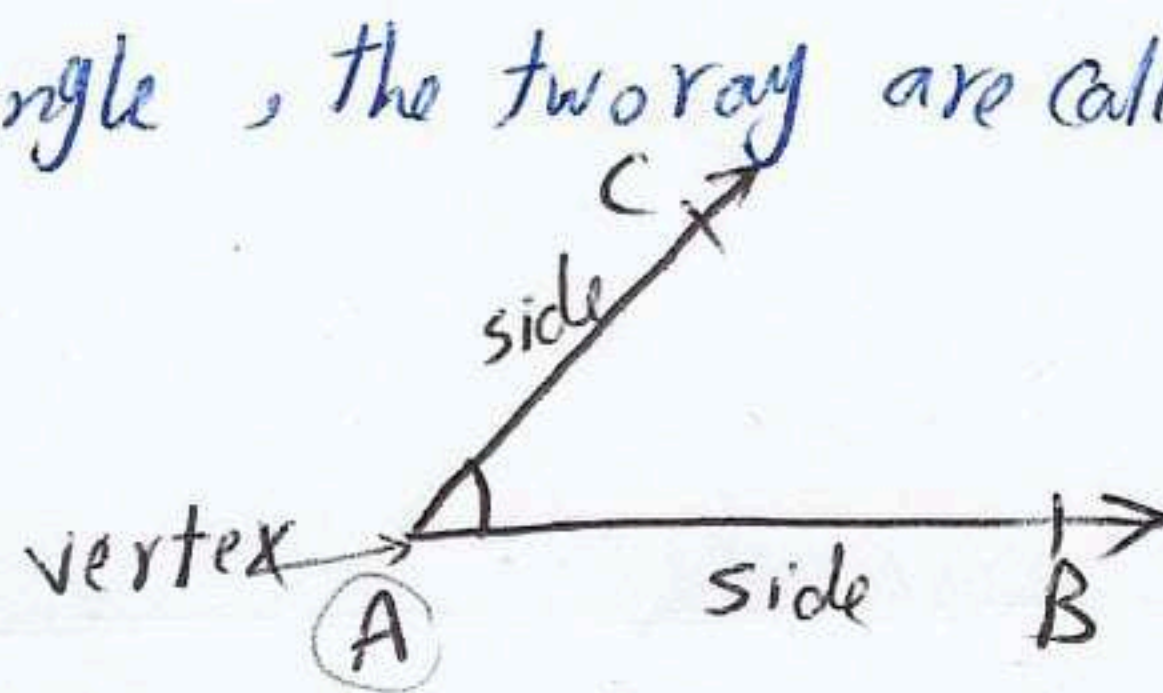


* The angle

is the union of two rays with the same starting point

and this point is called the vertex of the angle, the two rays are called two sides of the angle

$\angle A$ or $\angle BAC$ or $\angle CAB$



The types of angles

its measure

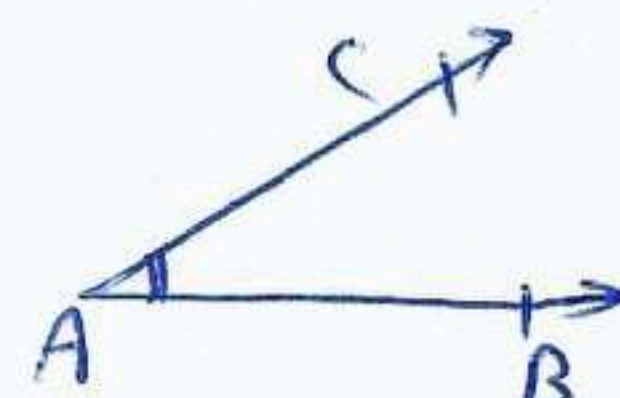
① Zero angle

its measure = 0°
its sides are coincident



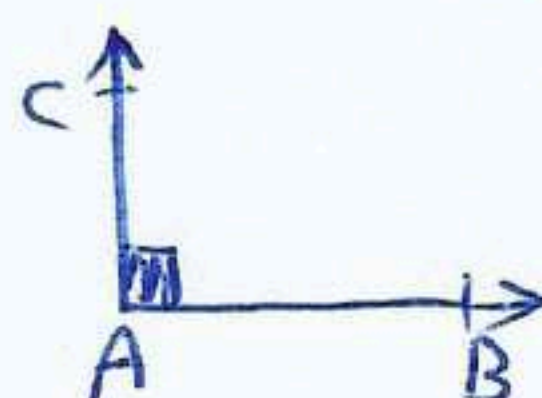
② Acute angle

$0^\circ < \text{its measure} < 90^\circ$
for example $32^\circ 30'$ & 60°



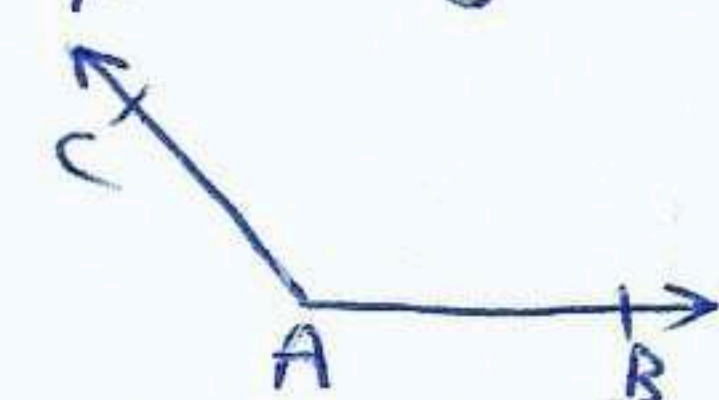
③ Right angle

its measure = 90°
or $89^\circ 60'$ ($60' = 1^\circ$)



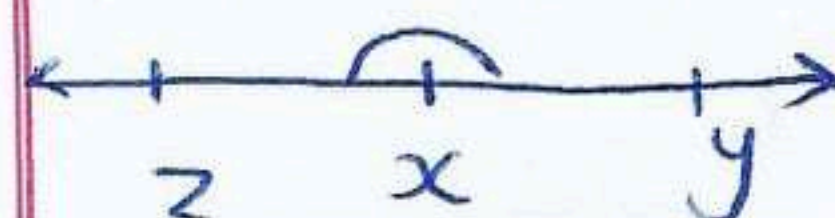
④ obtuse angle

$90^\circ < \text{its measure} < 180^\circ$
for example 100° & $179^\circ 30'$



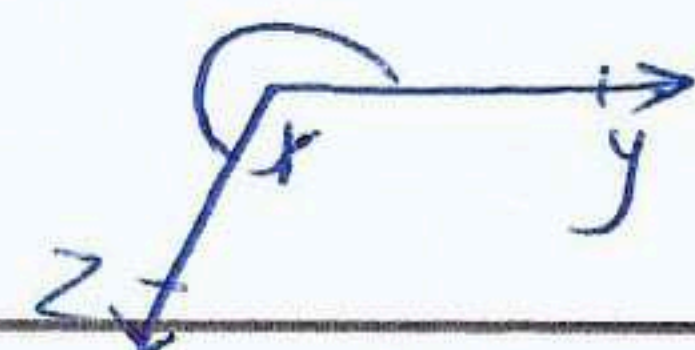
⑤ straight angle

its measure = 180°
its sides are forming one straight line



⑥ Reflex angle

$180^\circ < \text{its measure} < 360^\circ$
for example 200° & 350°



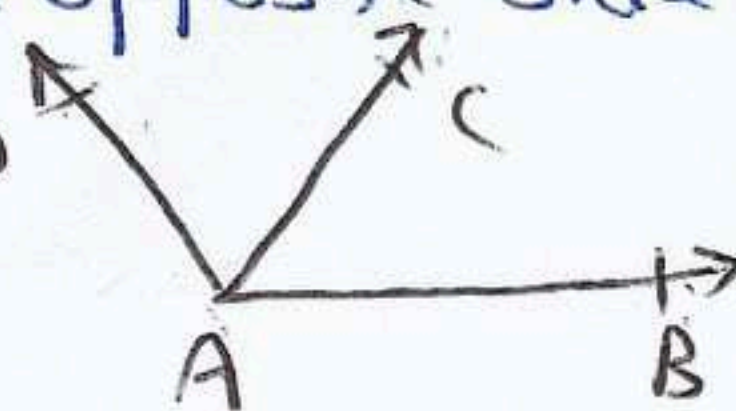
$$m(\angle yxz) + m(\text{reflex } \angle yxz) = 360^\circ$$

The relations between the angles.

① Adjacent angles

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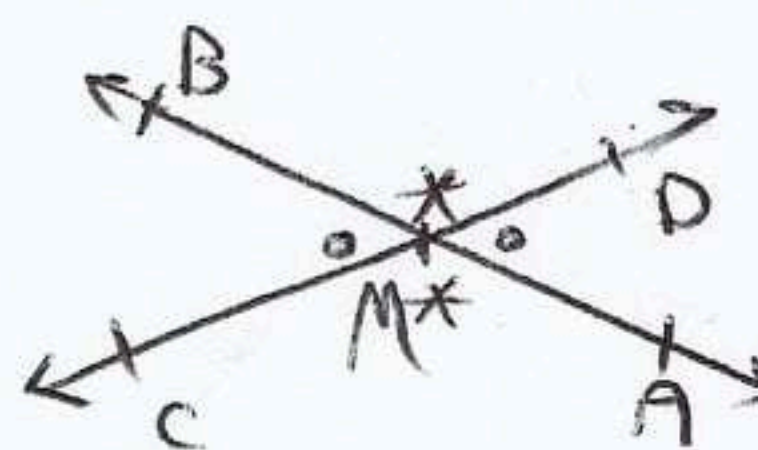
Two angles are said to be adjacent if they have a common vertex and a common side and the other two sides are on opposite sides of this common side. $\angle CAB$ and $\angle CAD$ adjacent.



② Vertically opposite angles (V.O.A)

If two straight lines intersect, then the measures of each two vertically opposite angles are equal.

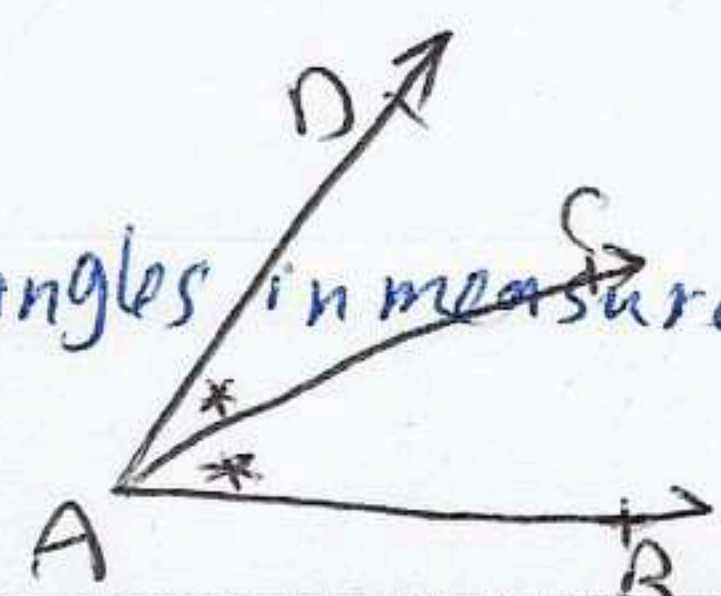
$$m(\angle DMA) = m(\angle BMC) \quad \& \quad m(\angle DMB) = m(\angle AMC)$$



③ The angle bisector.

it is the ray that divides the angle into two equal angles in measure

$$m(\angle CAB) = m(\angle CAD) = \frac{1}{2} m(\angle BAD)$$

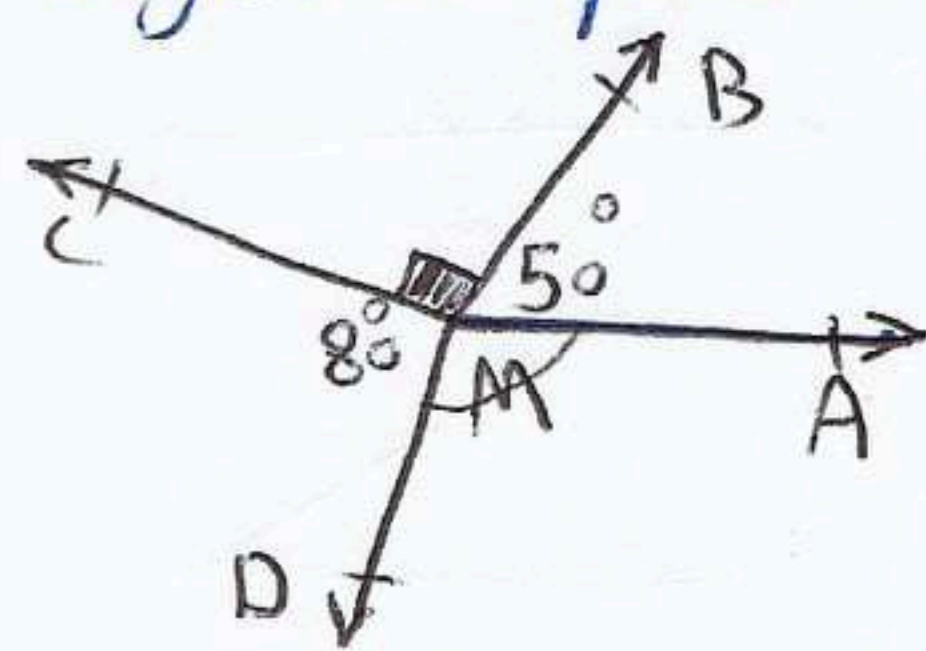


④ Accumulative angles at a point

The sum of the measures of the accumulative angles at a point is 360°

$$m(\angle AMB) + m(\angle BMC) + m(\angle CMD) + m(\angle DMA) = 360^\circ$$

$$\text{Then } m(\angle DMA) = 360^\circ - (50^\circ + 90^\circ + 80^\circ) = 140^\circ$$



⑤ Complementary angles

Two angles are said to be Complementary if the sum of their measures is 90°

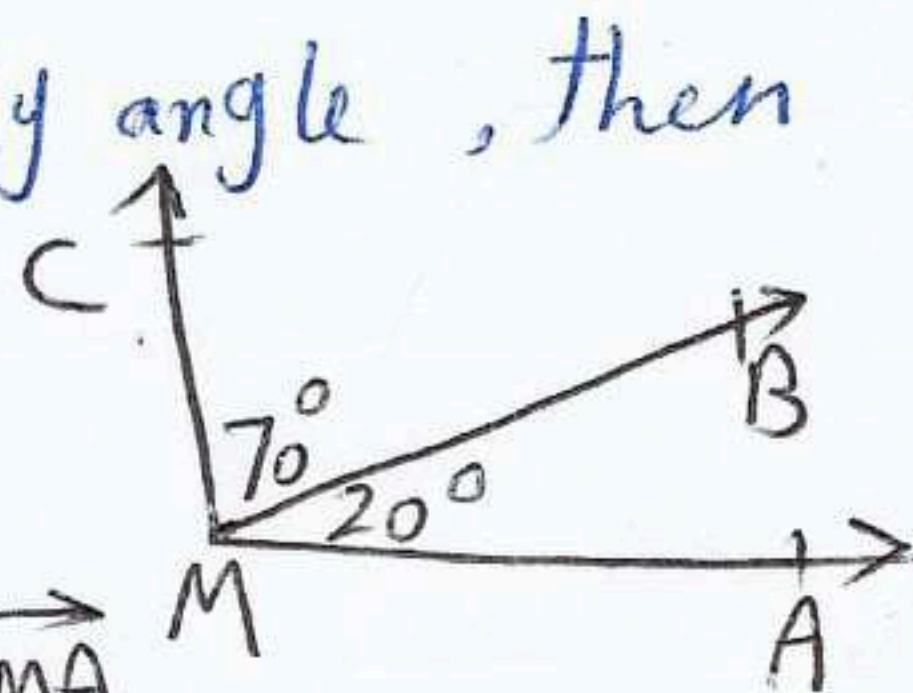
* Two angles are either acute angles or one is zero angle and the other is a right angle.

* The complements of the same angle are equal in measure

If $\angle A$ complements $\angle B$ & $\angle C$ complements $\angle B$ then $m(\angle A) = m(\angle C)$

* If the two adjacent angles are complementary angles, then their outer sides are perpendicular.

$$m(\angle AMB) + m(\angle BMC) = 90^\circ \quad \text{then } \overrightarrow{MC} \perp \overrightarrow{MA}$$



⑥ Supplementary angles

Two angles are said to be Supplementary if the sum of their measures is 180°

* Two angles (obtuse and acute) or (right and right) or (zero and straight angle)

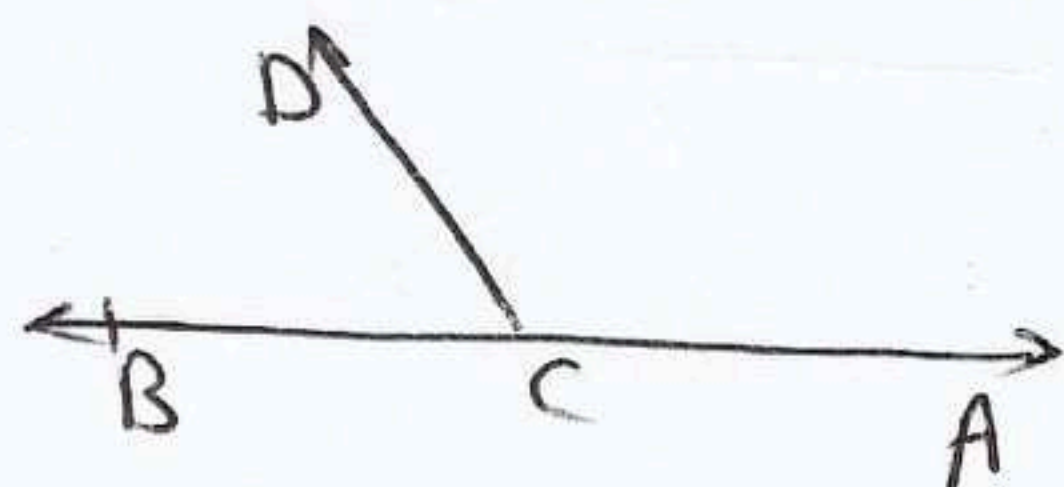
* The supplement of the same angle are equal in measure

If $\angle A$ supplements $\angle B$ and $\angle C$ supplements $\angle B$ then $m(\angle A) = m(\angle C)$

* two adjacent angles formed by a straight line and a ray with a starting point on this straight line are supplementary.

$$\text{If } \overrightarrow{AB} \cap \overrightarrow{CD} = \{C\}$$

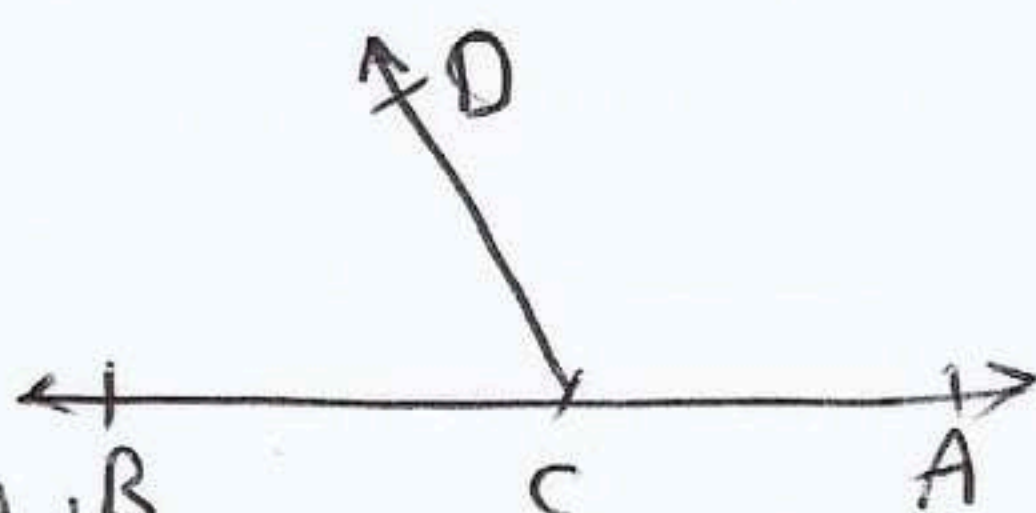
$$\text{Then } m(\angle ACD) + m(\angle DCB) = 180^\circ$$



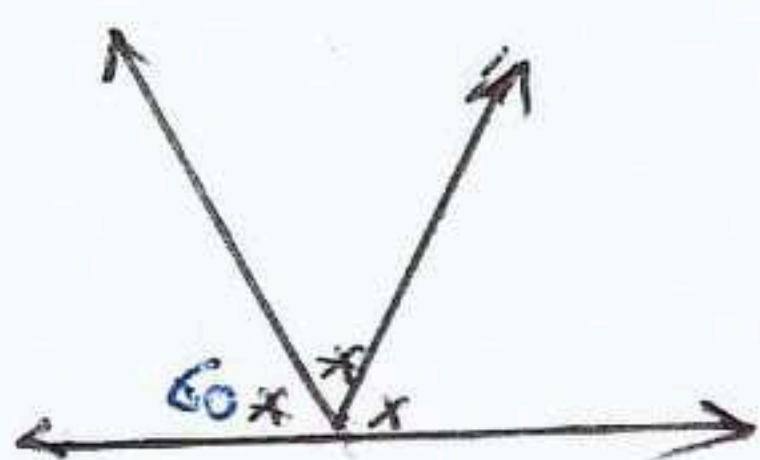
* If two adjacent angles are supplementary, then their outer sides are on the same straight line

$$\text{If } m(\angle ACD) + m(\angle DCB) = 180^\circ$$

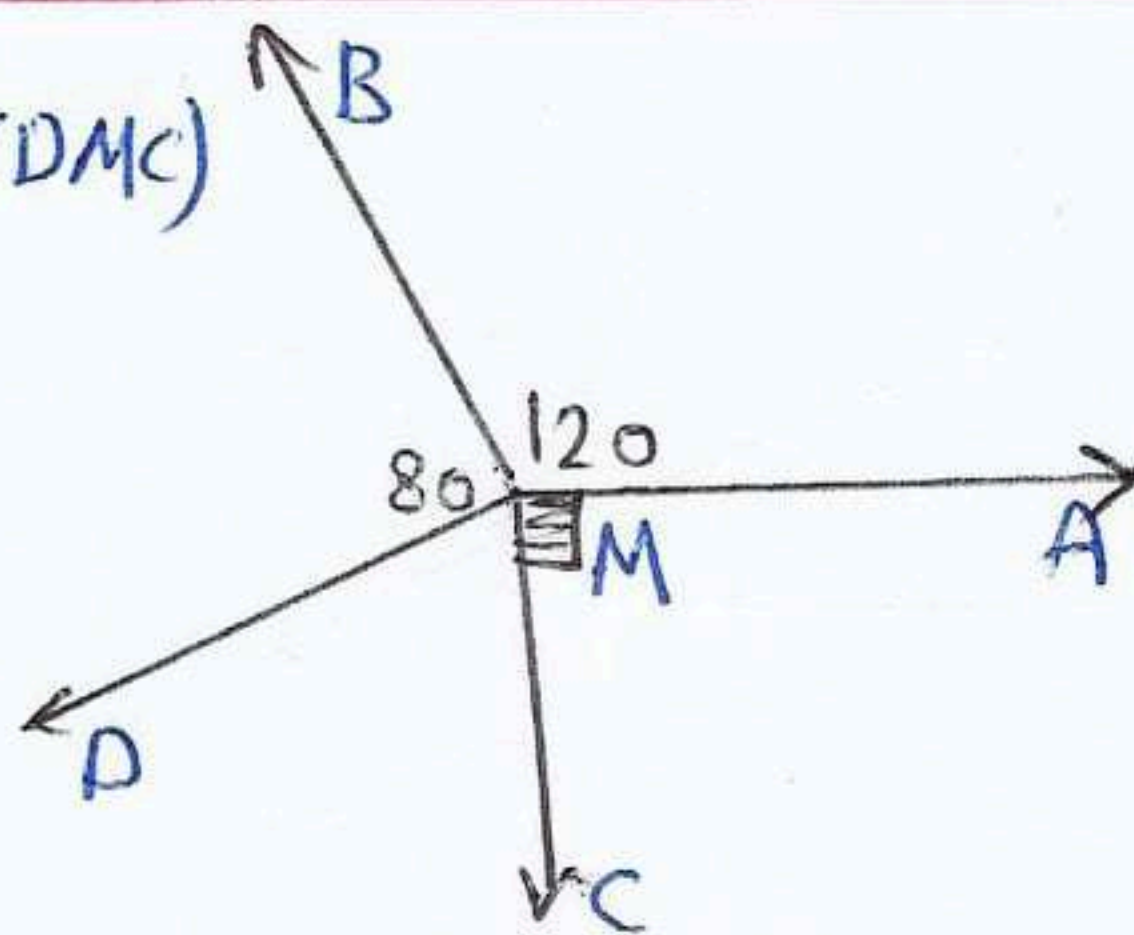
Then \overrightarrow{CA} and \overrightarrow{CB} are on the same straight line
or $\angle ACB$ is a straight angle. *try by your self.*



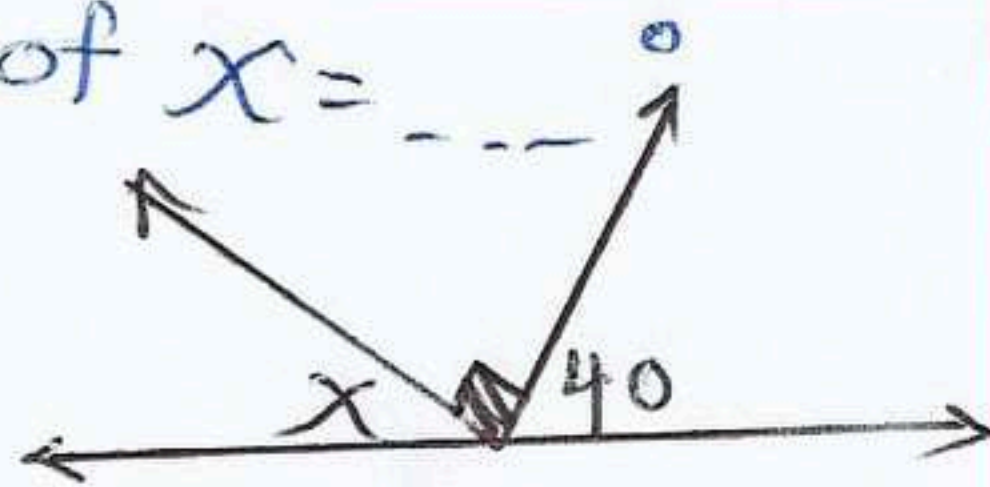
① Are \overrightarrow{CA} and \overrightarrow{CB} on same straight line? why?



② Find $m(\angle DMC)$

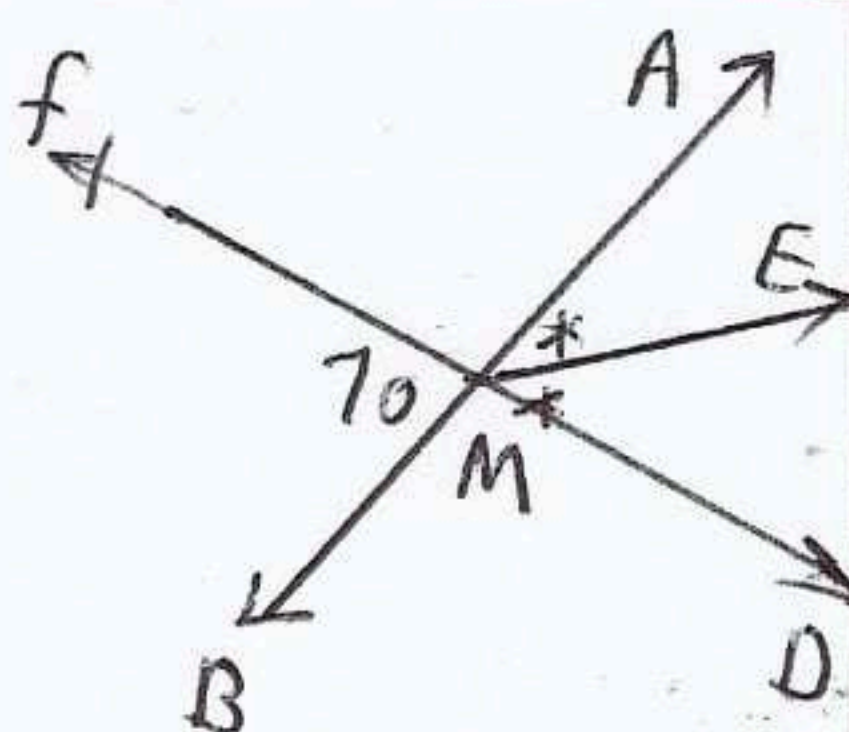


③ the value of $x = \dots$



④ $\overrightarrow{AB} \cap \overrightarrow{DF} = \{M\}$

find $m(\angle AMF)$
 $m(\angle AMD)$
 $m(\angle DME)$

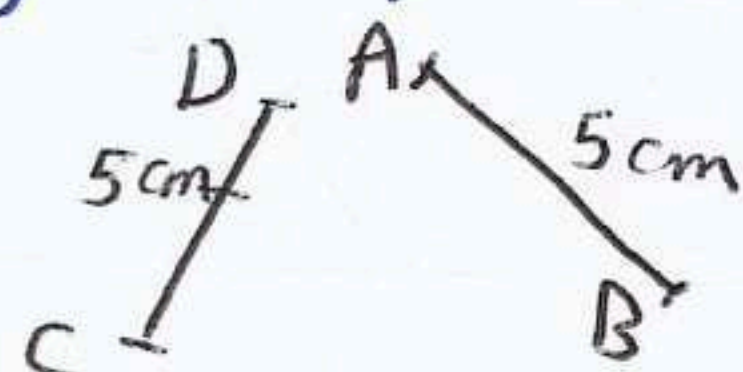


2) Congruence

① Congruence of two line segments

Two line segments are congruent if they are equal in length

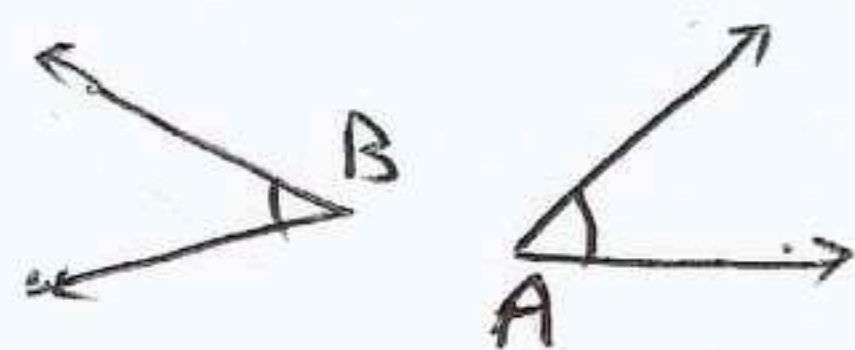
If $AB = CD$ then $\overline{AB} \equiv \overline{CD}$



② Congruence of two angles

Two angles are congruent if they are equal in measure

$\therefore m(\angle A) = m(\angle B) = 50^\circ$ then $\angle A \equiv \angle B$

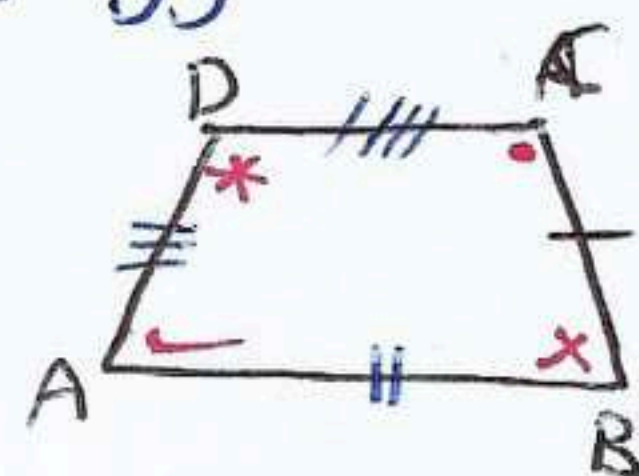
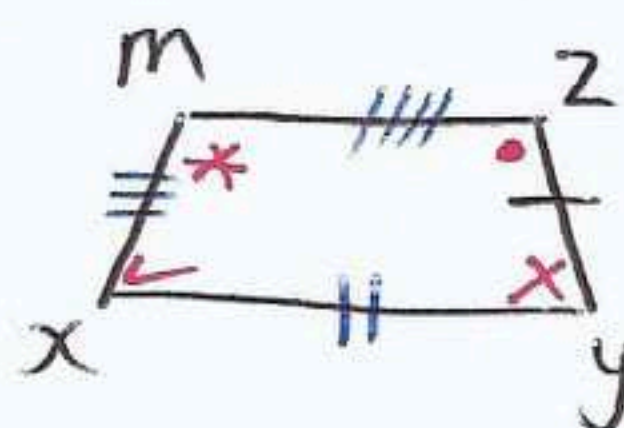


③ Congruence of two polygons

Two polygons are congruent if there is correspondence between their vertices such that each side and each angle in the first polygon is congruent to its corresponding element in the other polygon.

If $m(\angle A) = m(\angle X)$, $m(\angle B) = m(\angle Y)$

$m(\angle C) = m(\angle Z)$, $m(\angle D) = m(\angle M)$



and $AB = XY$, $BC = YZ$, $CD = ZM$, $DA = MX$

then the polygon $ABCD \equiv$ the polygon $XYZM$

Notes

- * The two squares are congruent if their sides are equal in length.
- * The two rectangles are congruent if their dimensions are equal.
- * The axis of symmetry of a polygon divides it into two congruent polygons.
- * The diagonal of the rectangle divides its surface into two congruent triangles.

④ Congruent triangles

The first case (S.A.S)

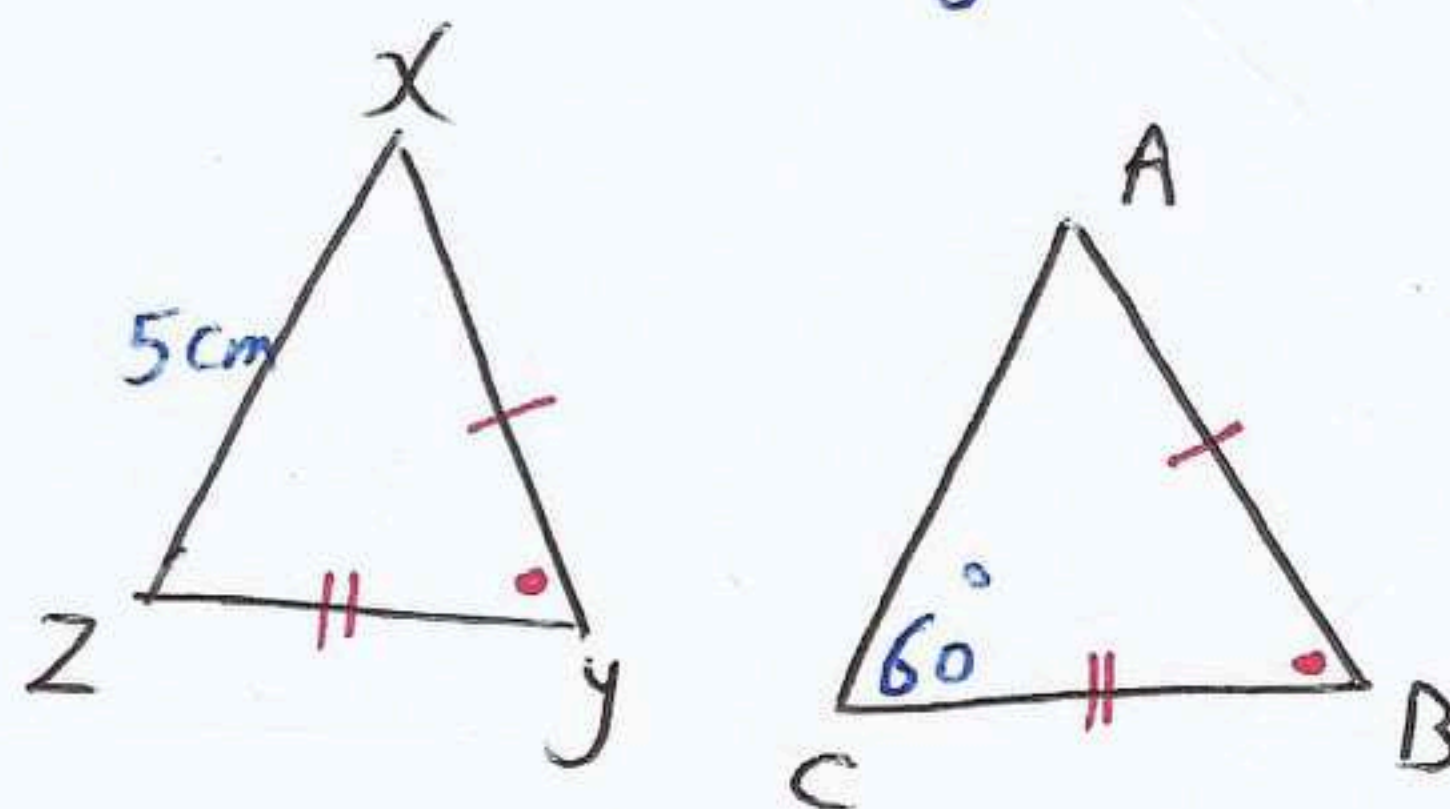
Two triangles are congruent if two sides and the included angle of one triangle are congruent to the corresponding parts of the other triangle.

In $\triangle ABC, xyz$

① $AB = xy$ S

② $m(\angle B) = m(\angle y)$ A

③ $BC = yz$ S



then $\triangle ABC \equiv \triangle xyz$, and we deduce that

① $AC = xz = 5cm$, ② $m(\angle C) = m(\angle z) = 60^\circ$, ③ $m(\angle A) = m(\angle x)$

The second case (A.S.A)

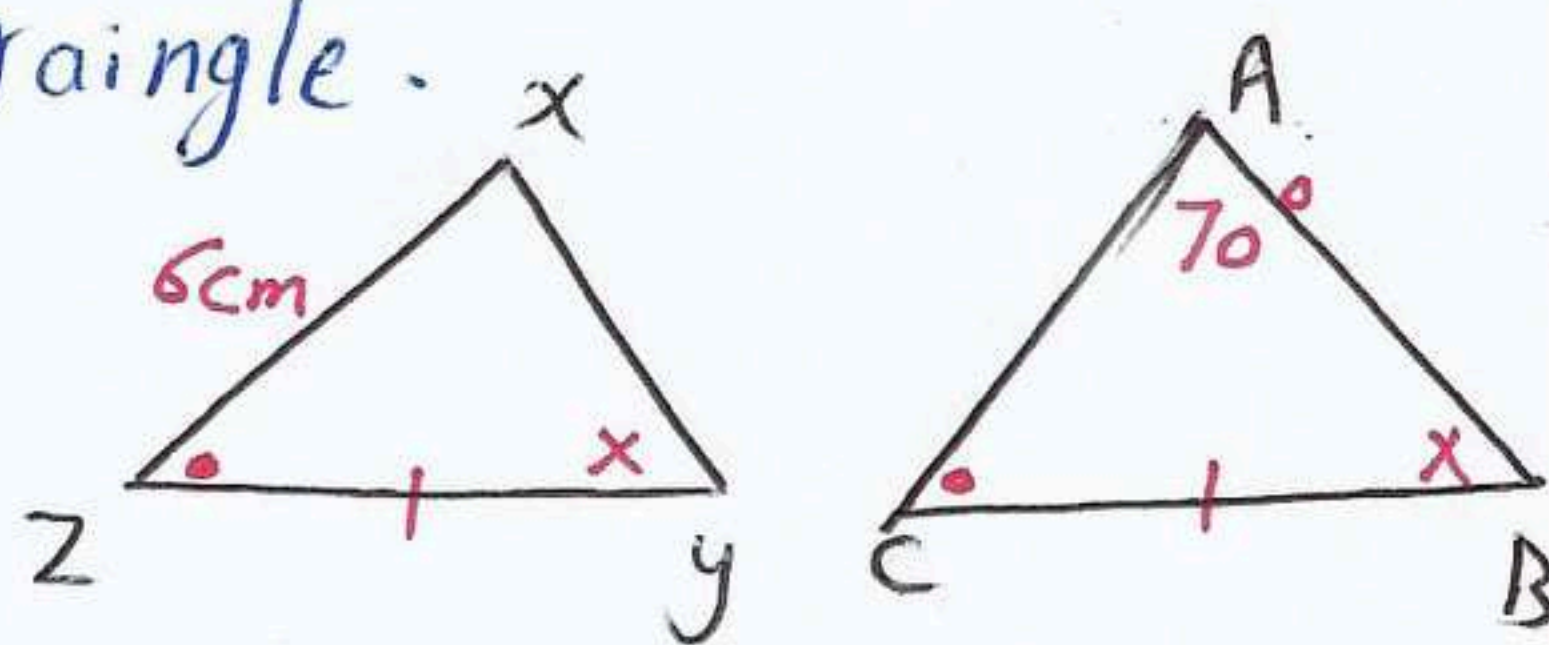
Two triangles are congruent if two angles and the side drawn between their vertices of one triangle are congruent to the corresponding parts of the other triangle.

In $\triangle ABC, xyz$

① $m(\angle B) = m(\angle y)$ A

② $BC = yz$ S

③ $m(\angle C) = m(\angle z)$ A



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Then $\triangle ABC \equiv \triangle xyz$ and we deduce that

① $m(\angle A) = m(\angle x) = 70^\circ$, ② $CA = zx = 6cm$, ③ $AB = xy$

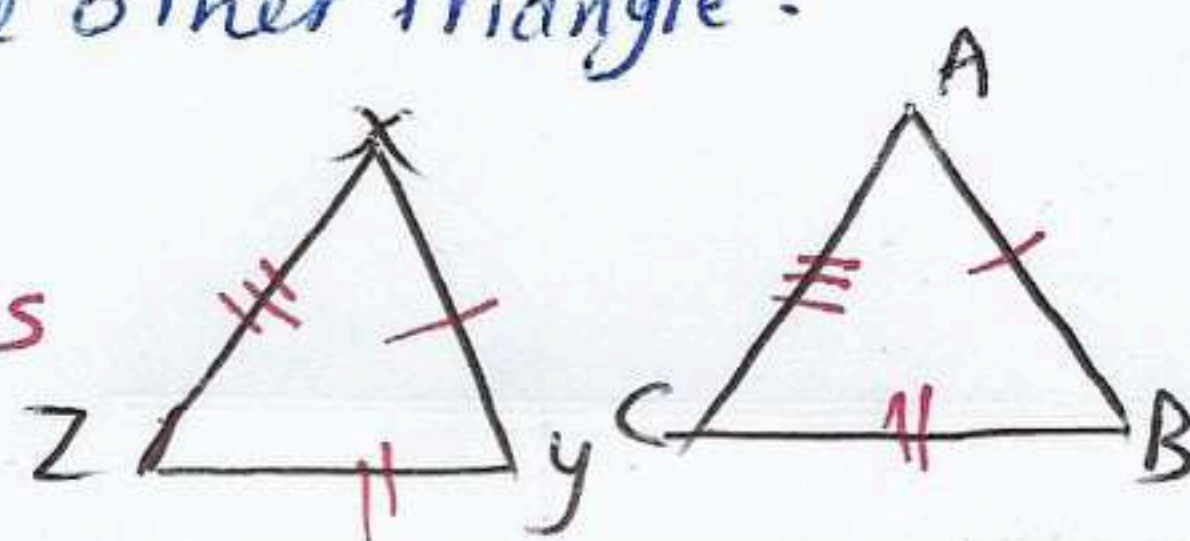
The third case (S.S.S)

Two triangles are congruent if each side of one triangle is congruent to the corresponding side of the other triangle.

In $\triangle ABC, xyz$

① $AB = xy$ S ② $BC = yz$ S ③ $AC = xz$ S

Then $\triangle ABC \equiv \triangle xyz$ 6



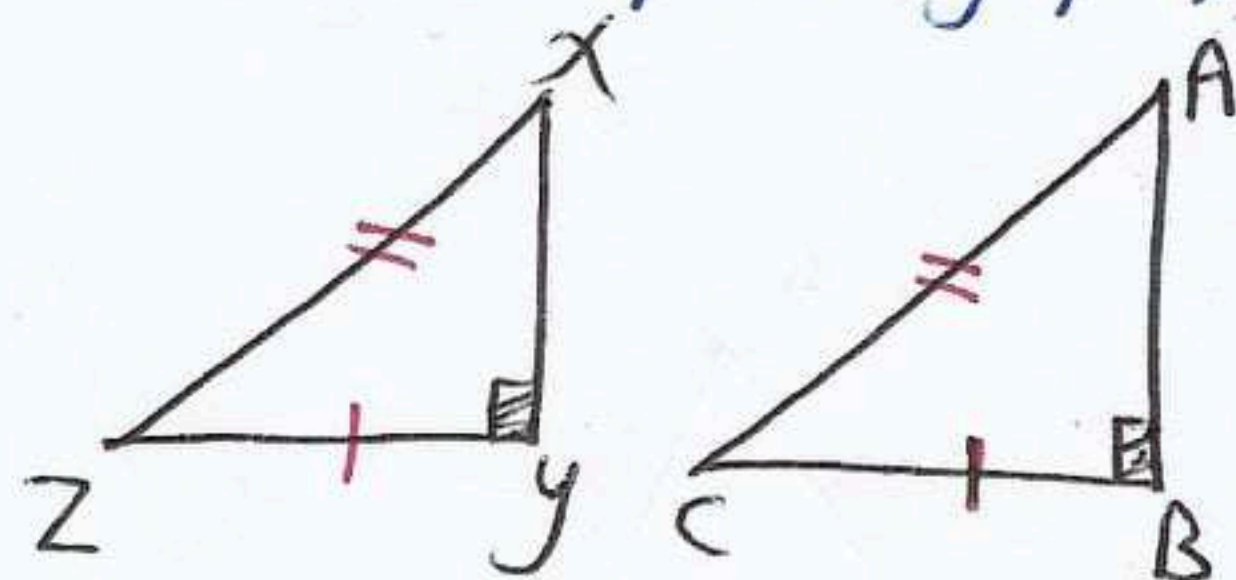
The fourth case (R.H.S)

Two right-angled triangles are congruent if the hypotenuse and side of one triangle are congruent to the corresponding parts of the other triangle.

In $\triangle ABC, xyz$

- $$\begin{cases} \textcircled{1} m(\angle B) = m(\angle y) = 90^\circ \\ \textcircled{2} AC = xz \\ \textcircled{3} BC = yz \end{cases}$$

Right angle
hypotenuse
side



Then $\triangle ABC \cong \triangle xyz$

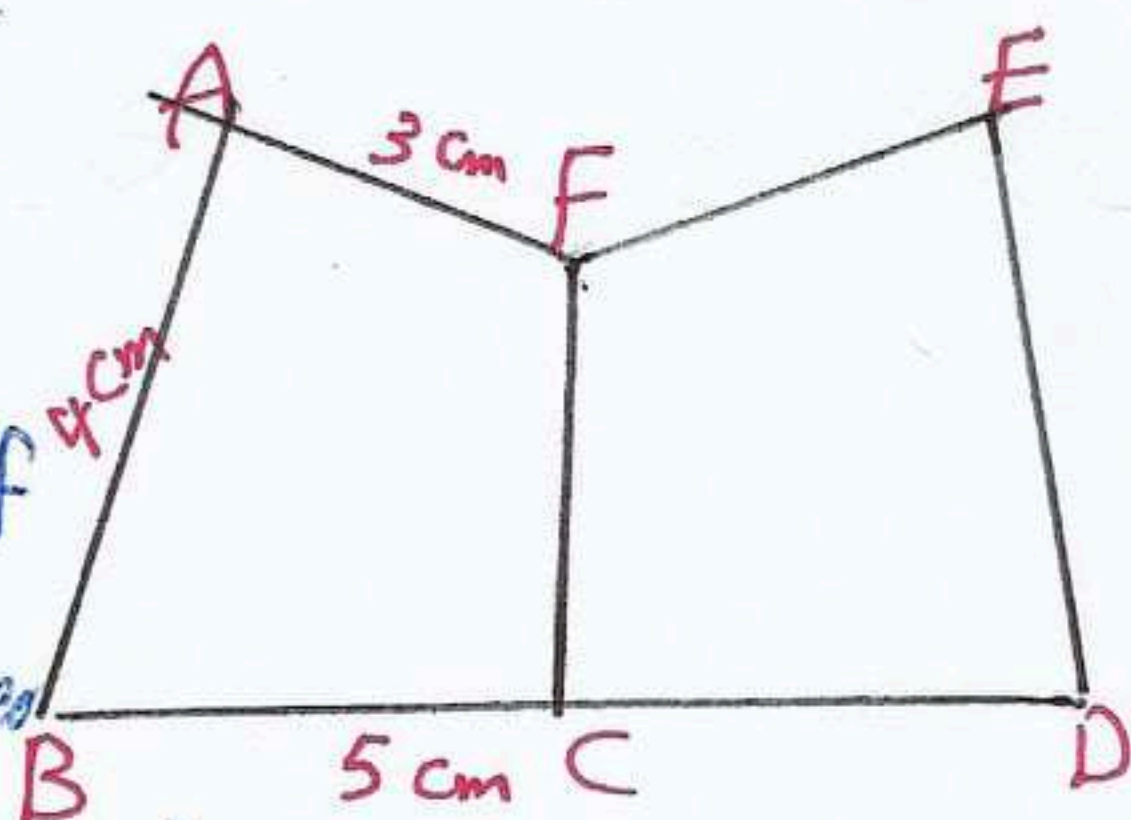
try by yourself.

① If $C \in \overline{BD}$

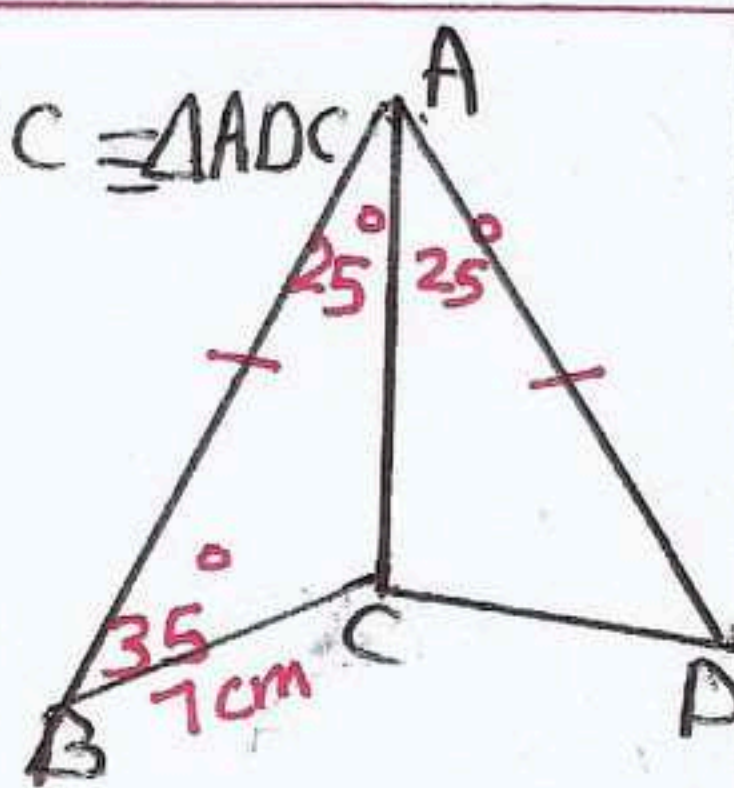
and polygon

$ABCF \cong EDCF$

Find the perimeter of figure ABDEF

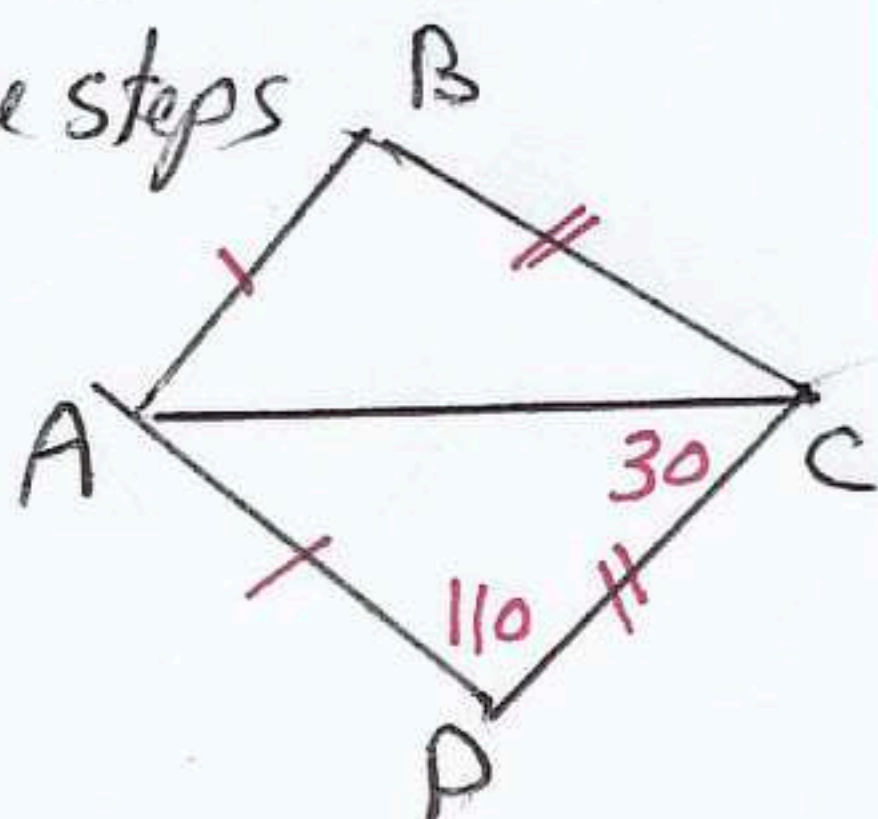


② Prove that $\triangle ABC \cong \triangle ADC$
find $m(\angle D)$
length of \overline{CD}



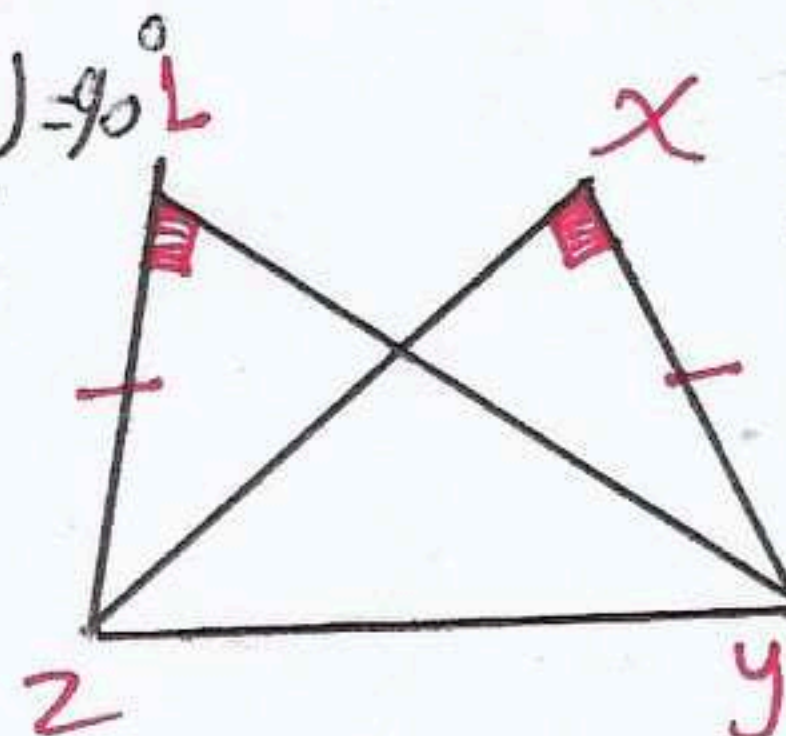
③ Find showing the steps

$m(\angle ABC)$



④ $m(\angle x) = m(\angle l) = 90^\circ$

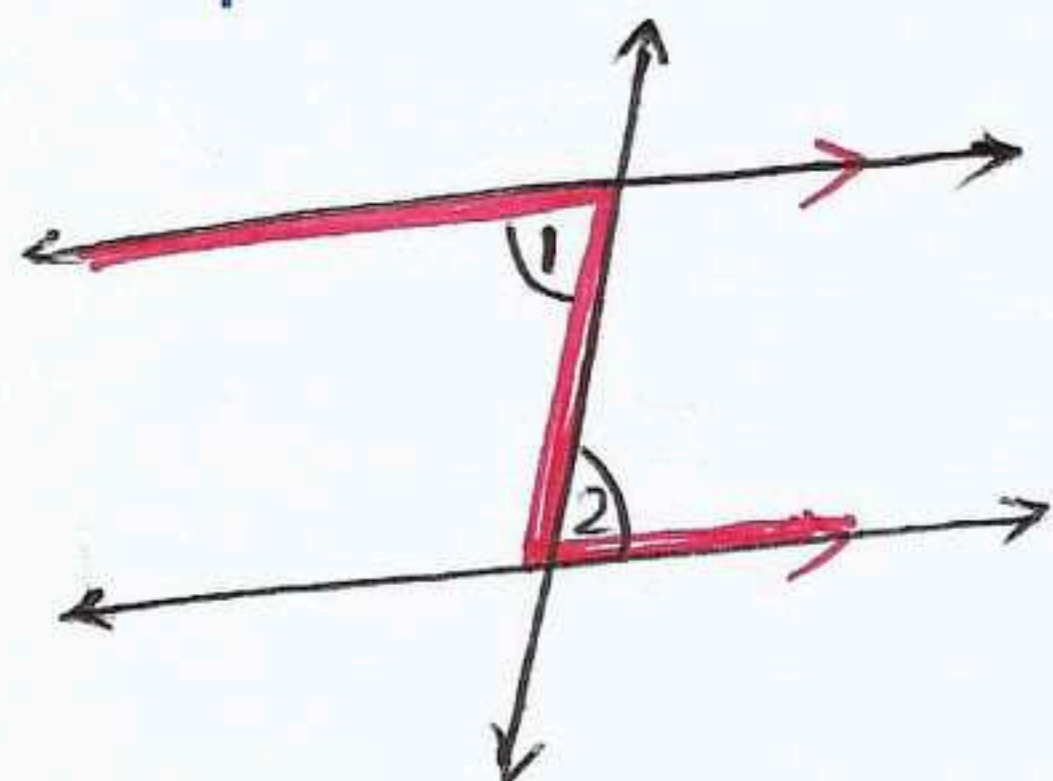
Is $\triangle xyz \cong \triangle lzy$
why?



3 Parallelism

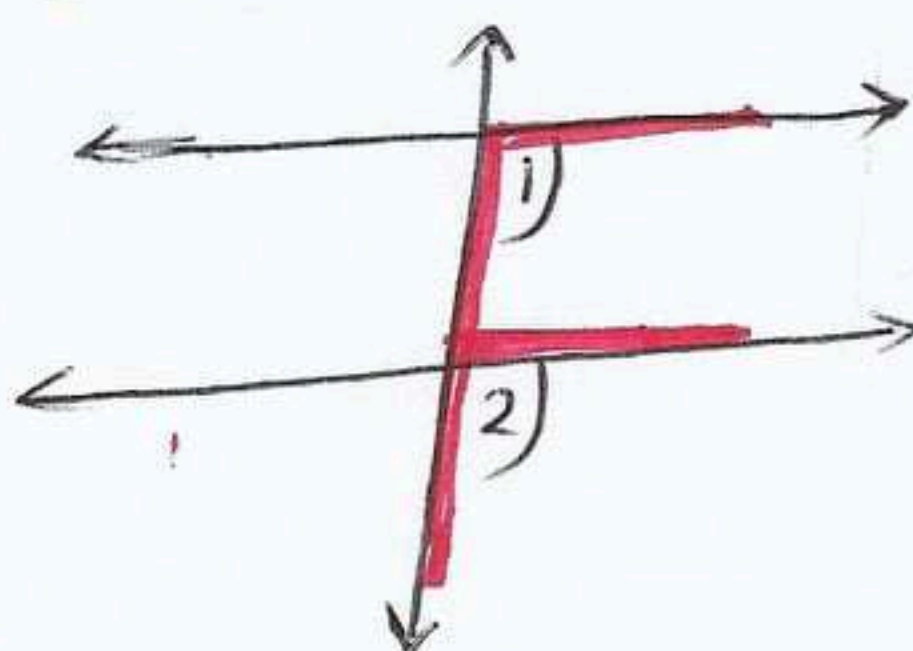
If a straight line intersects two parallel straight lines, then

Each two alternate angles are equal in measure. **Z**



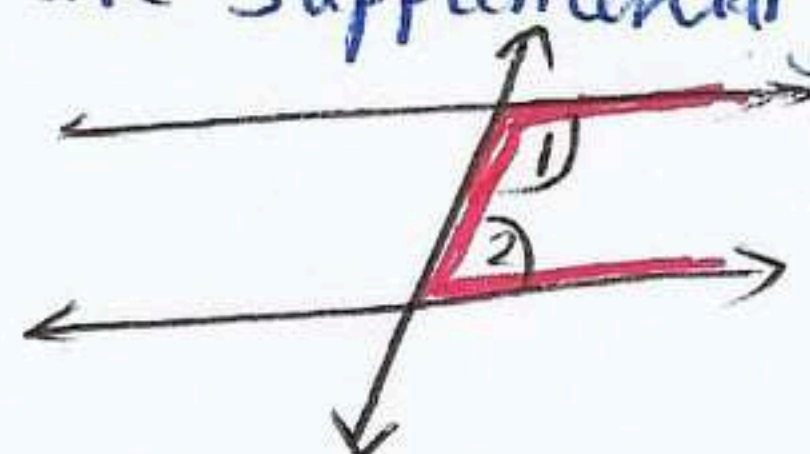
$m(\angle 1) = m(\angle 2)$
alternate angles

Each two corresponding angles are equal in measure. **F**



$m(\angle 1) = m(\angle 2)$
corresponding angles

Each two interior angles in the same side of the transversal are supplementary. **U**



$m(\angle 1) + m(\angle 2) = 180$
interior angles

How to prove the Parallelism

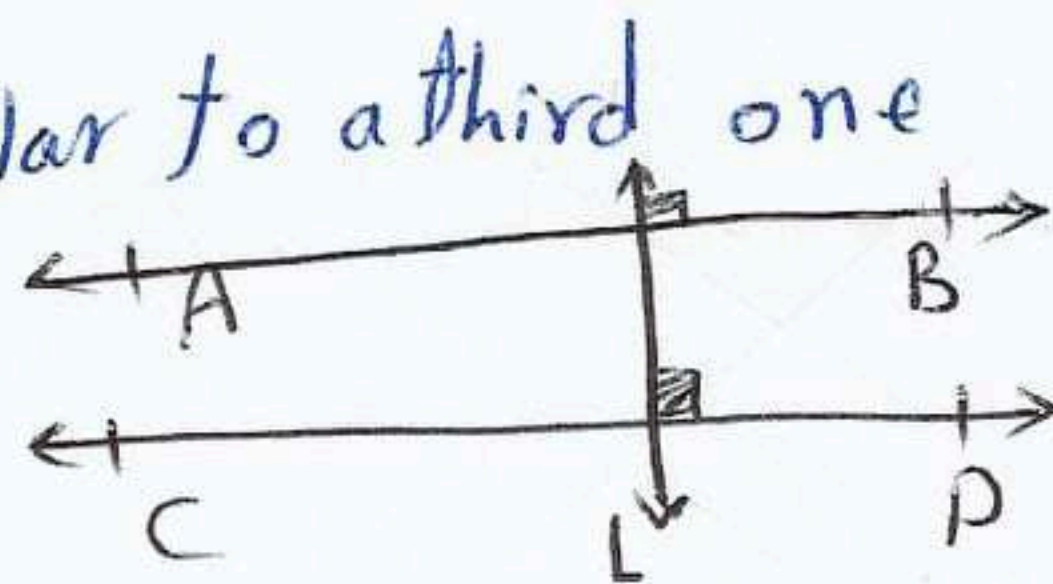
Two straight lines are parallel if a third straight line intersects them and one of the following cases is satisfied

- ① Two alternate angles have the same measure. or
- ② Two corresponding angles have the same measure. or
- ③ Two interior angles in the same side of the transversal are supplementary.

Geometric facts.

The perpendicular to one of two coplaner parallel straight lines is perpendicular to the other, and vice versa

if two coplaner straight lines are perpendicular to a third one then the two straight lines are parallel.



If $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$ and $\overleftrightarrow{L} \perp \overleftrightarrow{AB}$

then $\overleftrightarrow{L} \perp \overleftrightarrow{CD}$ and vice versa

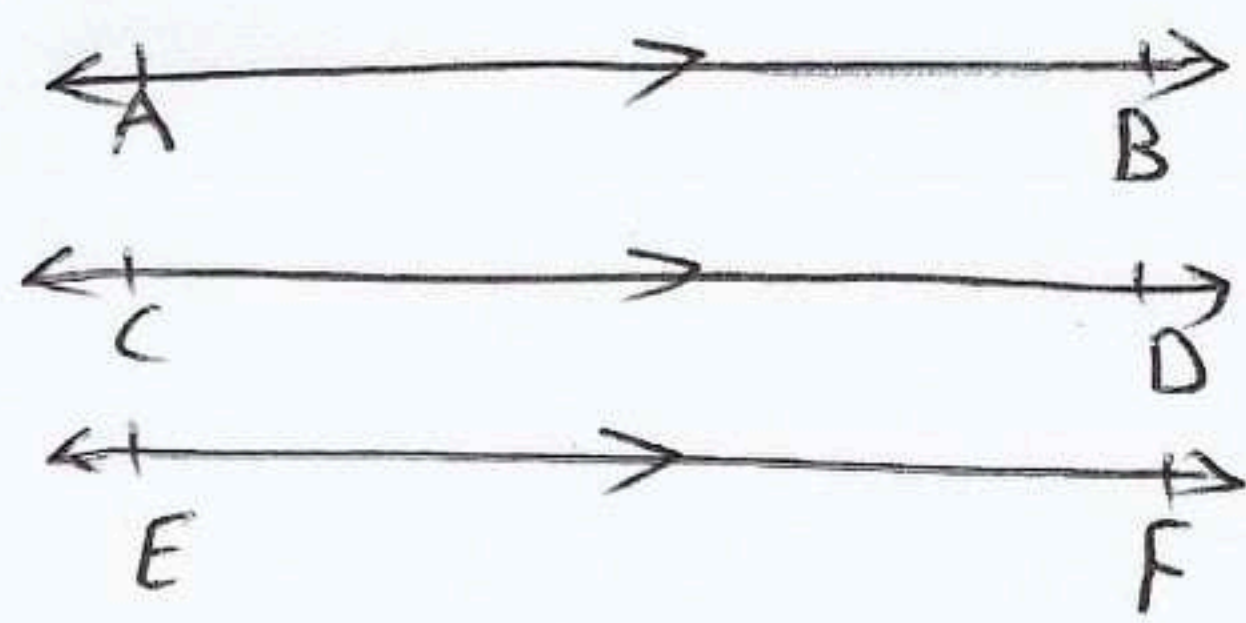
If $\overleftrightarrow{AB} \perp \overleftrightarrow{L}$ and $\overleftrightarrow{CD} \perp \overleftrightarrow{L}$

Then $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$

■ If two straight lines are parallel to a third, then these two straight lines are parallel

If $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$ and $\overleftrightarrow{EF} \parallel \overleftrightarrow{CD}$

Then $\overleftrightarrow{AB} \parallel \overleftrightarrow{EF}$

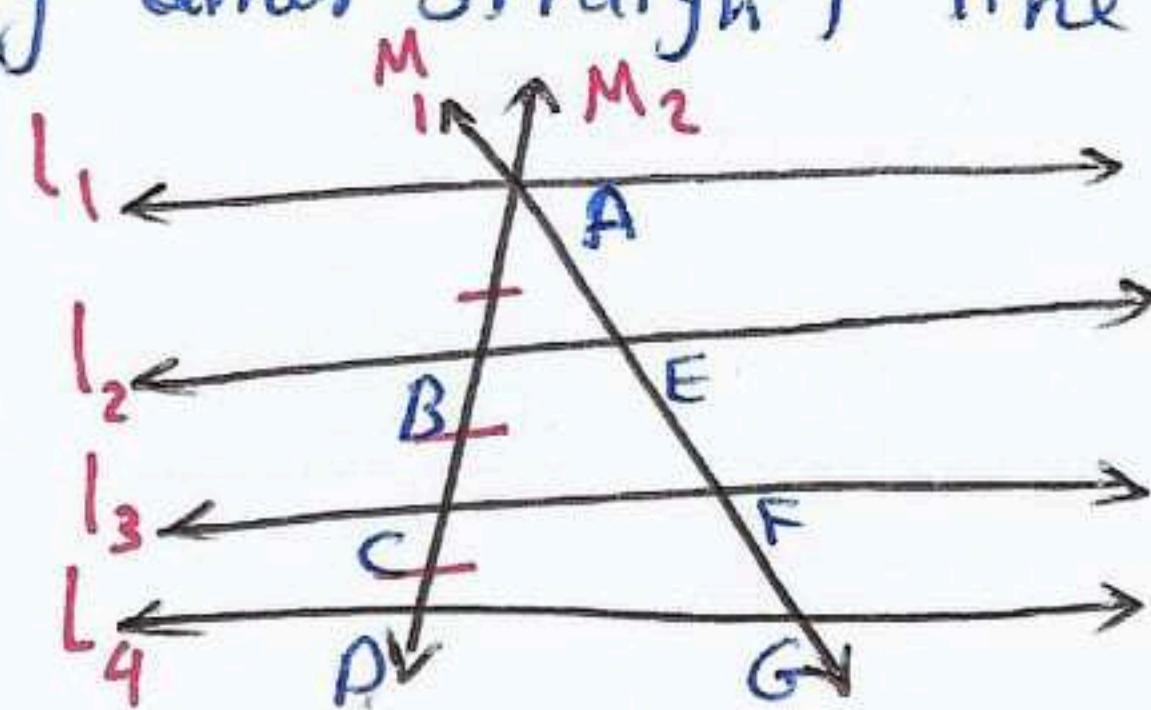


■ If parallel straight lines divide a straight line into segments of equal lengths, then they divide any other straight line into segments of equal lengths.

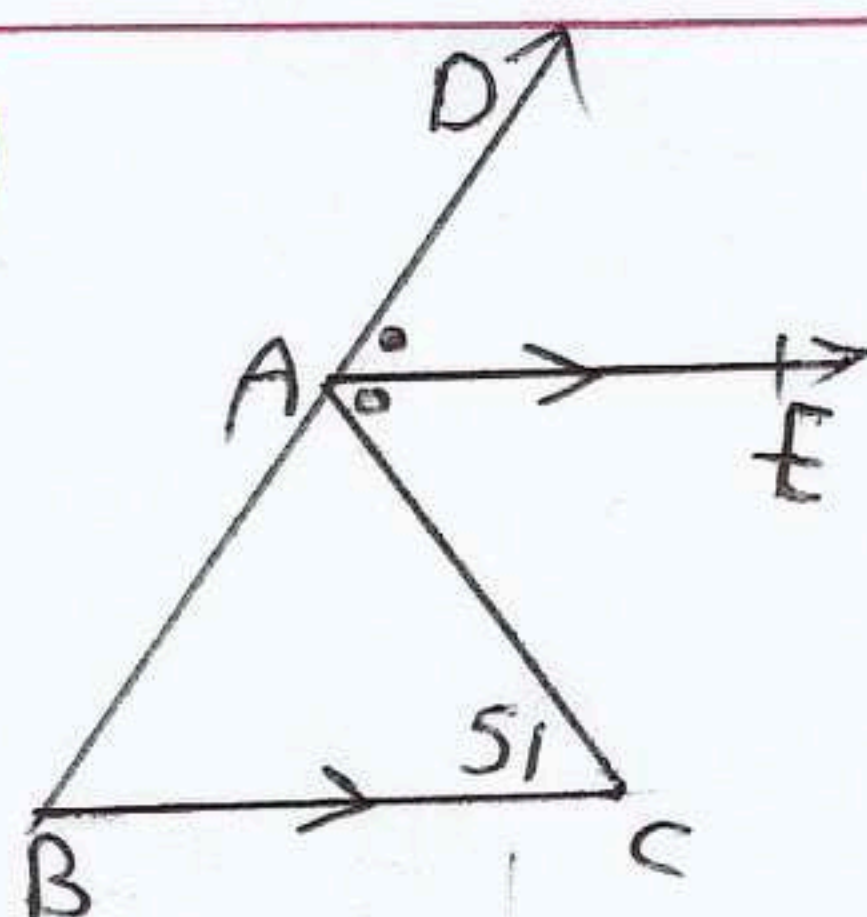
If $\overleftrightarrow{l_1} \parallel \overleftrightarrow{l_2} \parallel \overleftrightarrow{l_3} \parallel \overleftrightarrow{l_4}$ and $AB = BC = CD$

Then $AE = EF = FG$

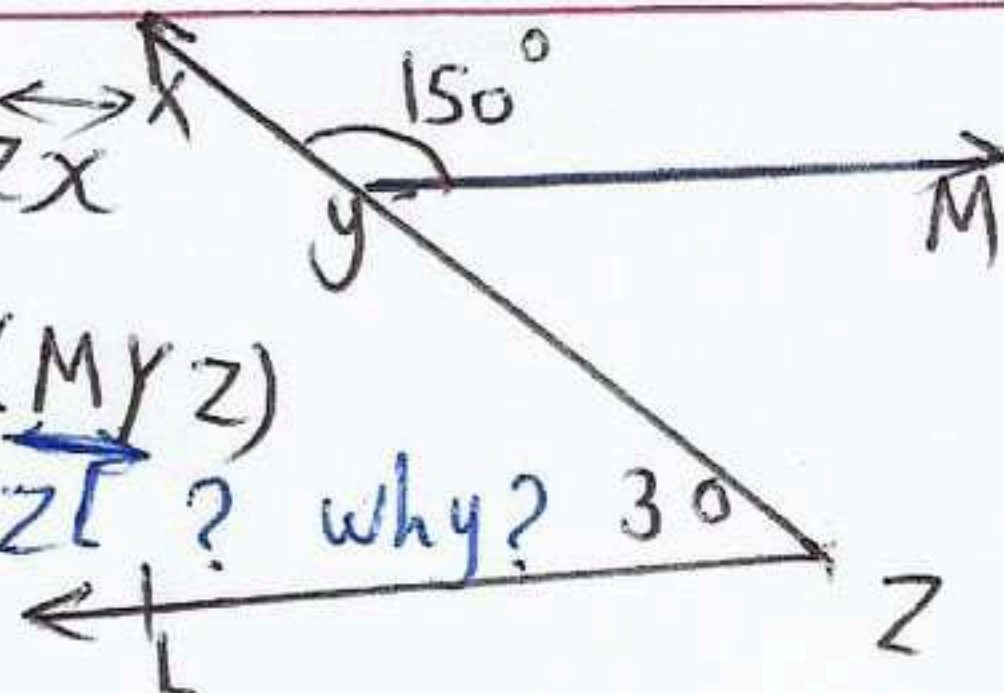
Try by yourself



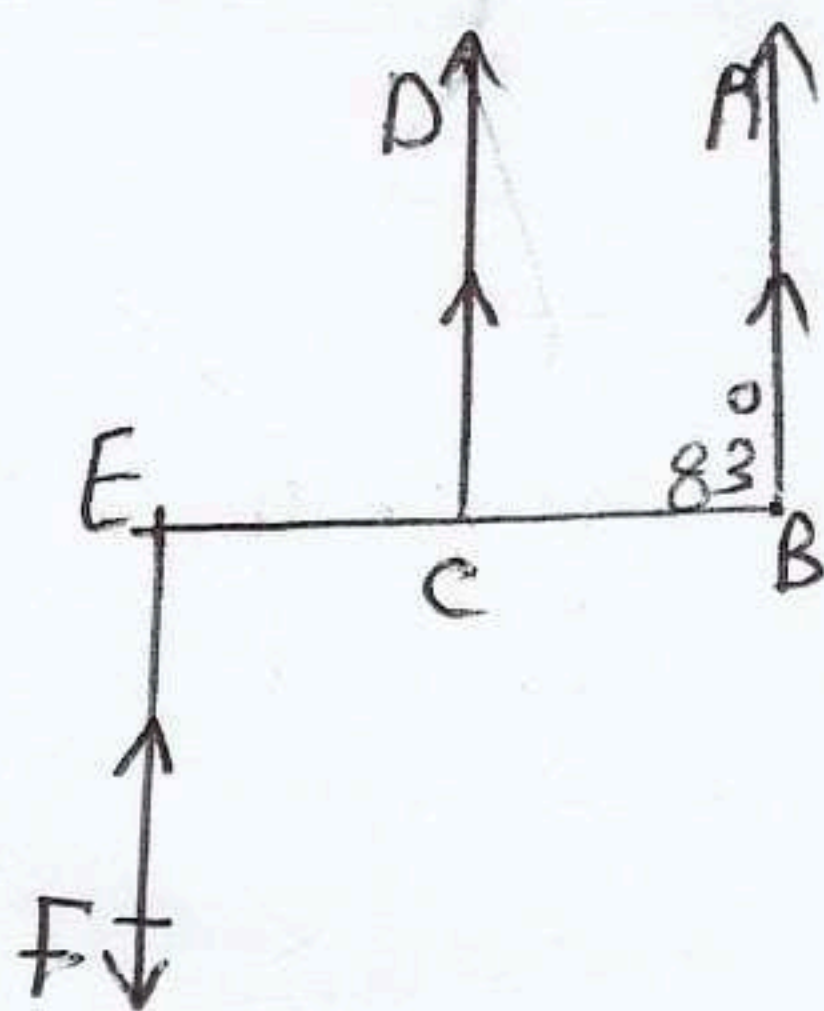
① Find $m(\angle CAE)$
 $m(\angle B)$



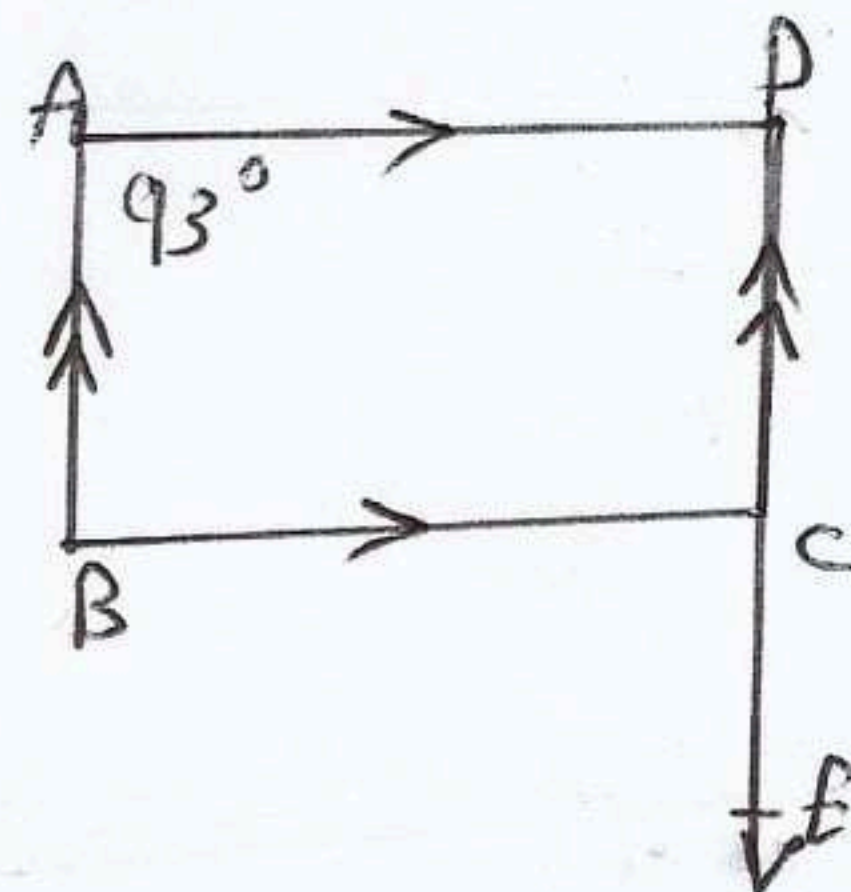
② $y \in \angle ZX$
Find $m(\angle MYZ)$
Is $\overleftrightarrow{YM} \parallel \overleftrightarrow{ZL}$? why? 30



③ Find $m(\angle CEF)$
 $m(\angle DCE)$



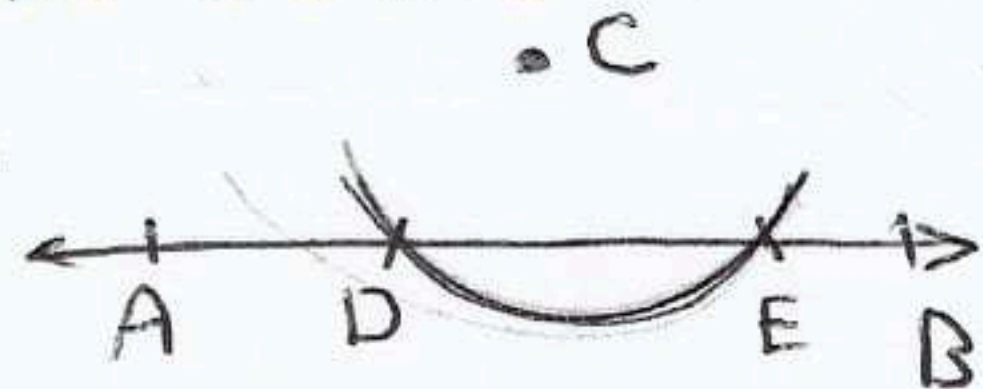
④ Find $m(\angle BCE)$
 $m(\angle D)$



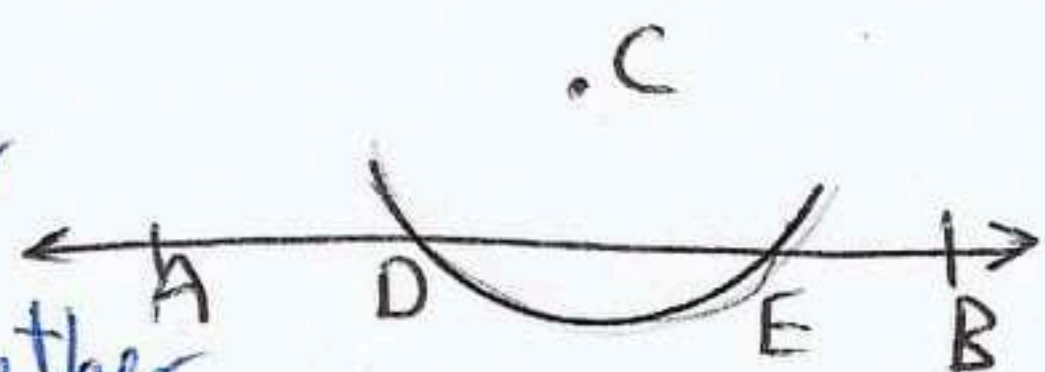
4] Geometric Constructions

① Drawing a perpendicular from a point outside a straight line:

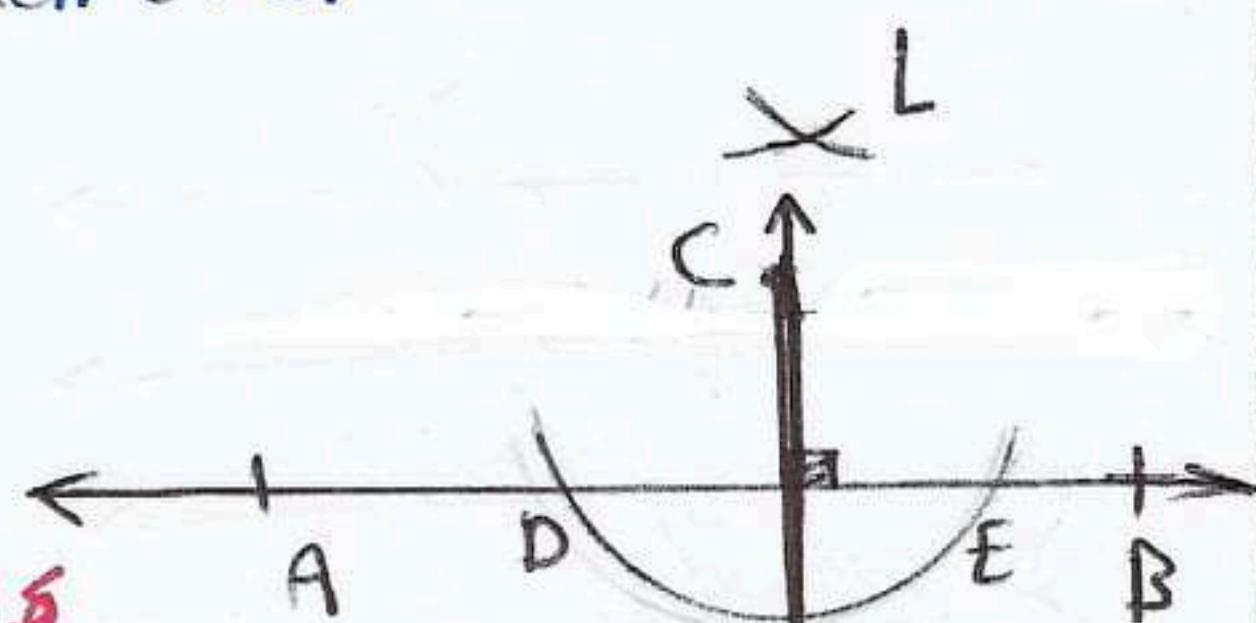
① using the compasses at C as a centre and with a suitable radius draw an arc to intersect \overleftrightarrow{AB} at the two points D and E



② At D and E as a centre with a radius greater than $\frac{1}{2} DE$ draw two arcs to intersect each other at L



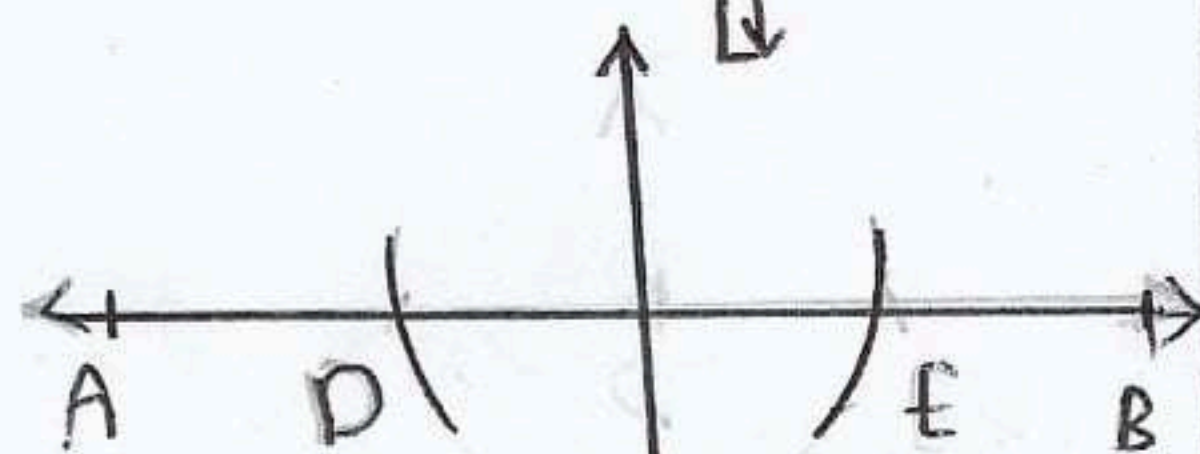
③ Draw \overleftrightarrow{CL}



② Drawing a perpendicular from a point belongs to the straight line

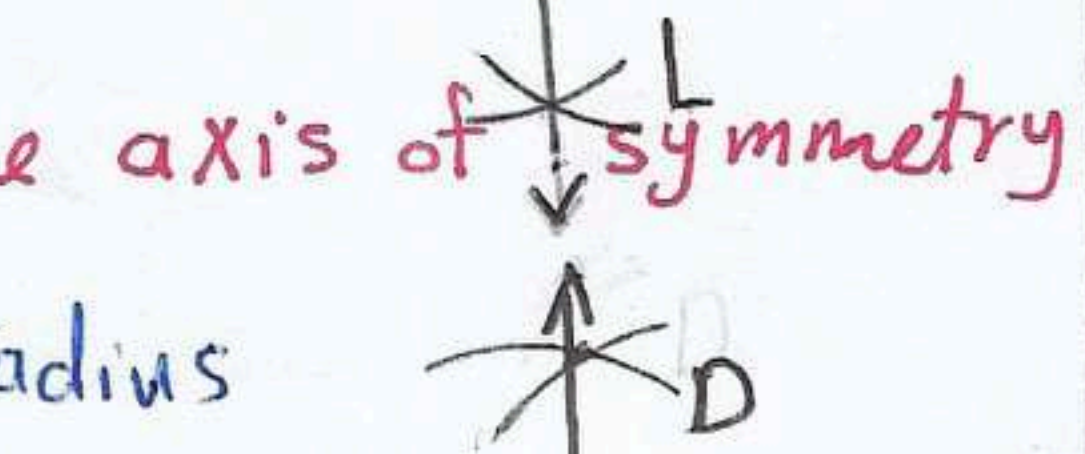
\overleftrightarrow{AB} is given and $C \in \overleftrightarrow{AB}$

We do the same steps



③ Bisecting a given line segment or drawing the axis of symmetry

① using the compasses at A as a centre with a radius greater than $\frac{1}{2} AB$ draw two arcs in the opposite side of \overleftrightarrow{AB}



② Do the same step at B

③ Draw \overleftrightarrow{DE} to cut \overleftrightarrow{AB} at C

C is the mid point of \overleftrightarrow{AB} and $\overleftrightarrow{DE} \perp \overleftrightarrow{AB}$

The axis of symmetry of a line segment is the straight line perpendicular to it from its midpoint

④ Constructing the bisector of a given angle.

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① taking B as a center, draw an arc intersect \vec{BA} and \vec{BC} at D and E

② taking D and E as centres draw two arcs intersect at the point X

③ Draw \vec{BX} to be the bisector of $\angle ABC$

⑤ Constructing an angle to be congruent to a given angle

$\angle ABC$ is a given angle

① Draw \vec{YL} as one side of the angle

② taking B as a center draw an arc intersect \vec{BA} and \vec{BC} at D and E

③ with y as a center and with the same radius draw an arc cut \vec{YL} at X

④ with x as a center and with radius equal the length of \overline{DE} draw another arc to cut the previous arc at Z

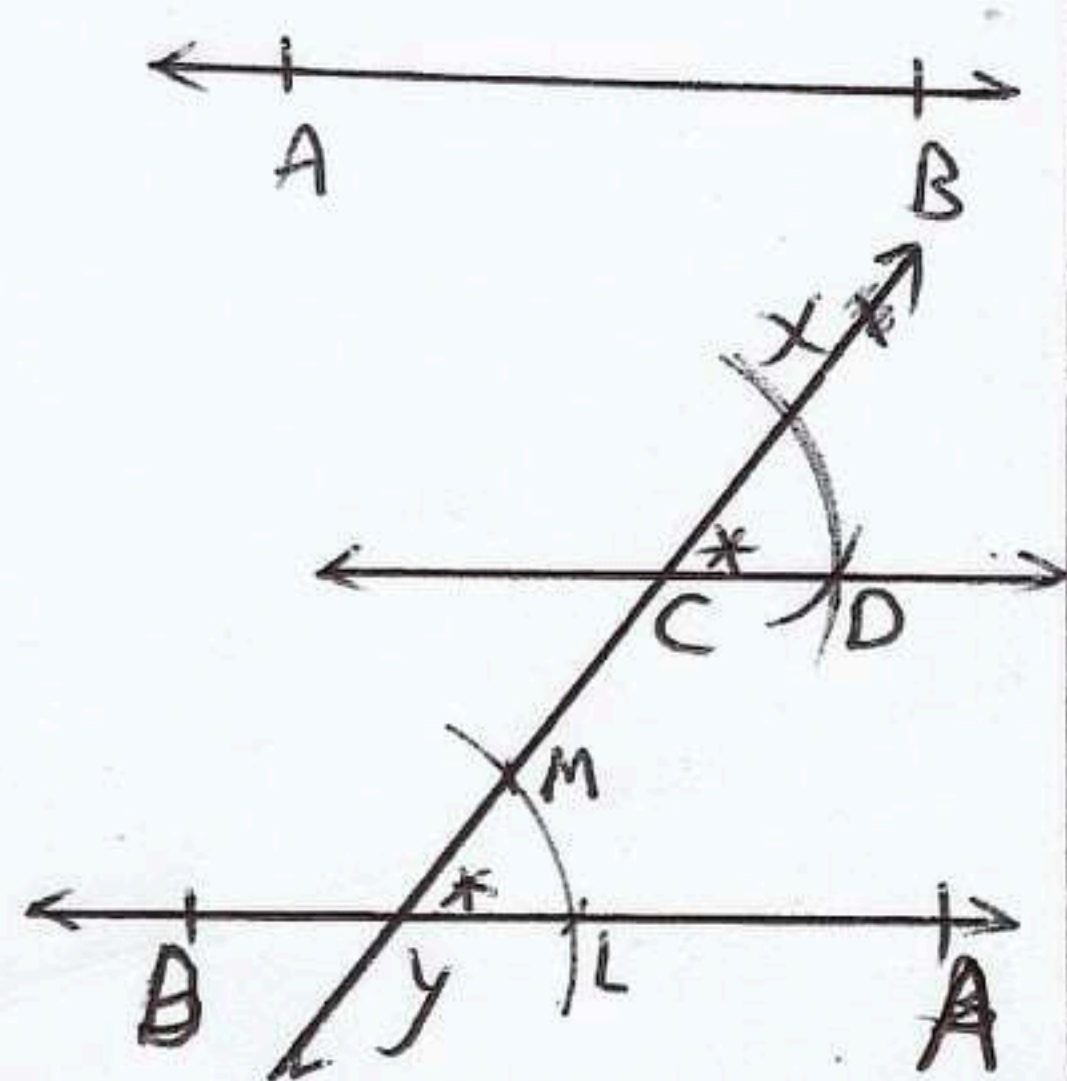
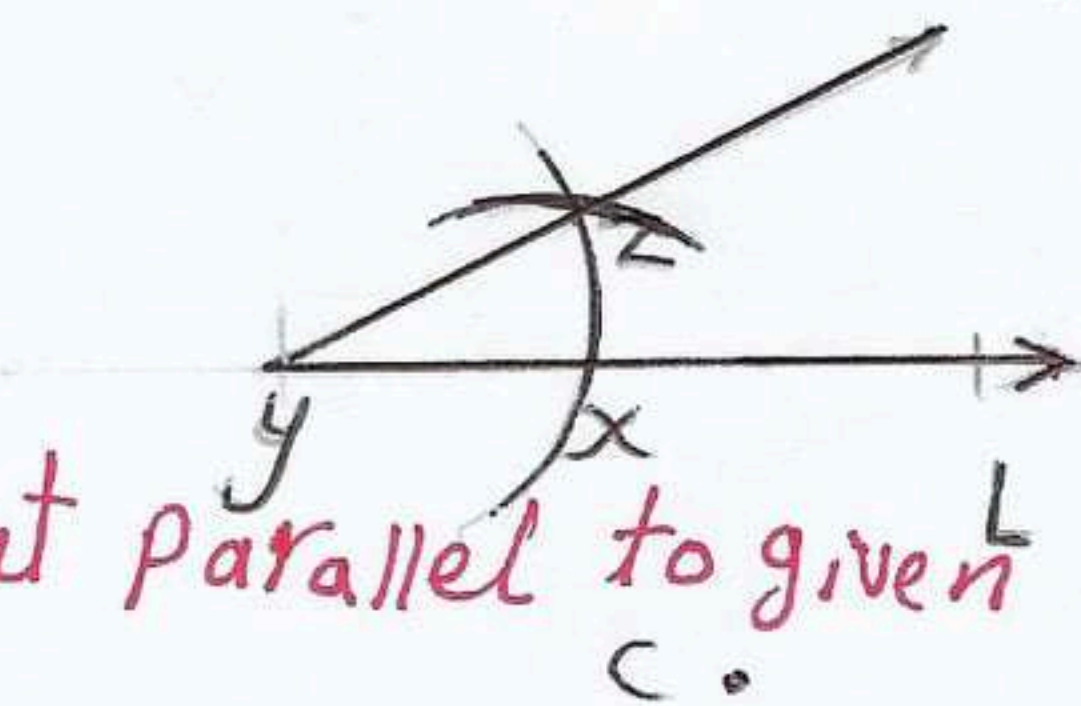
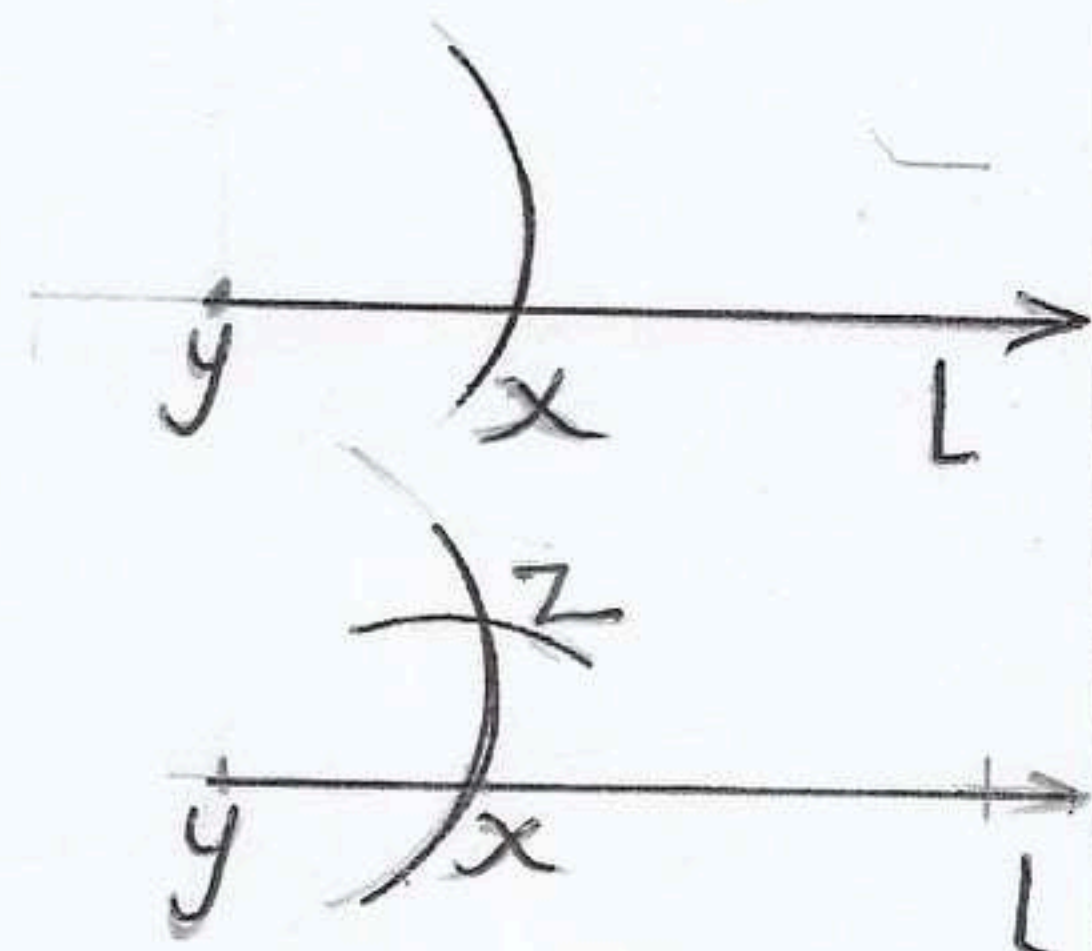
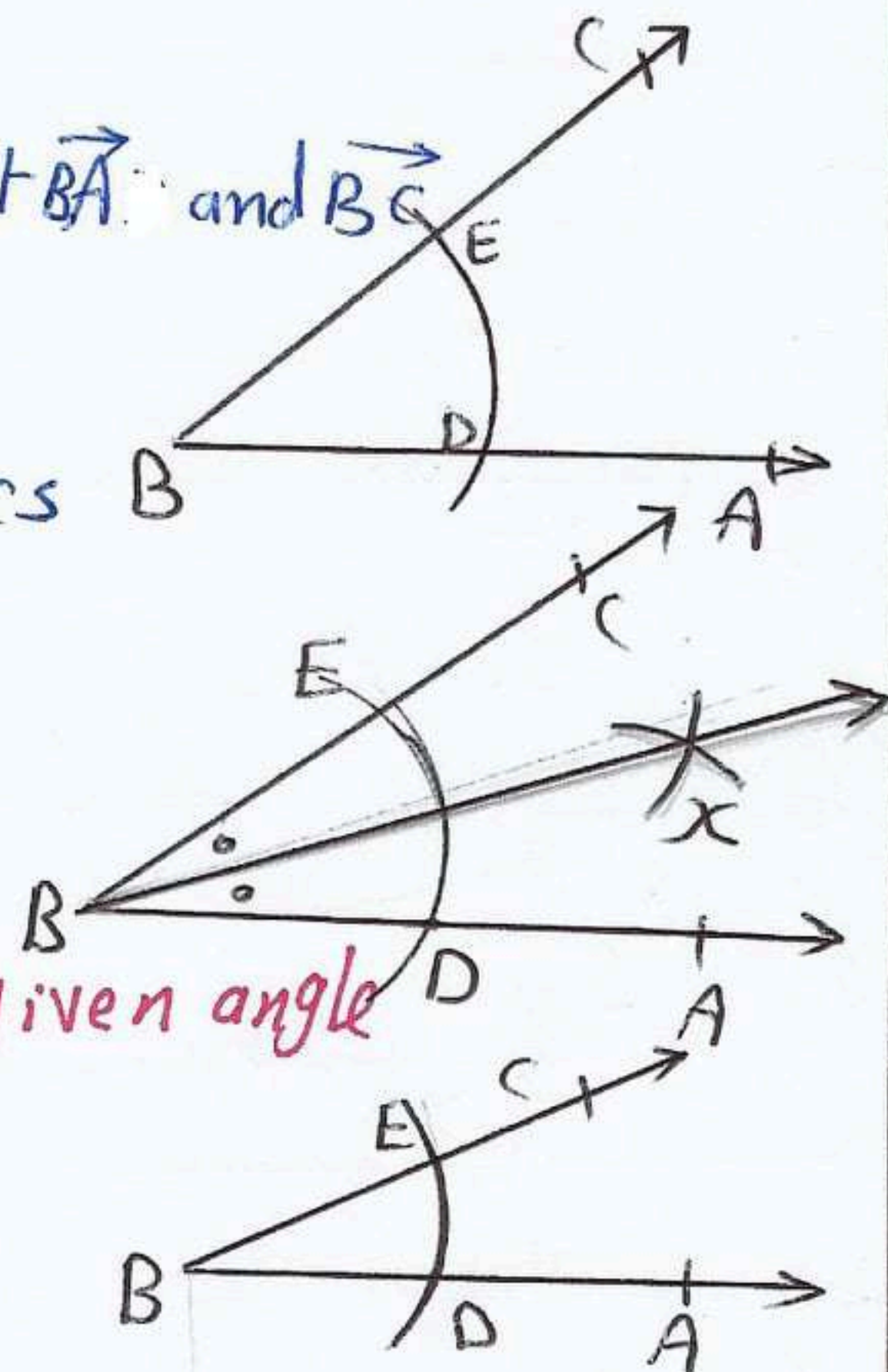
⑤ draw \vec{YZ}

⑥ Drawing a straight line from a given point parallel to given straight line.

\vec{AB} is a given straight line and $C \notin \vec{AB}$

① draw \vec{xy} passing through the point C and cutting \vec{AB} at y

② draw at C the angle $\angle XCD$ corresponding to $\angle AYX$ $\because \angle XCD \equiv \angle XYA$ using the previous construction then $\vec{CD} \parallel \vec{AB}$

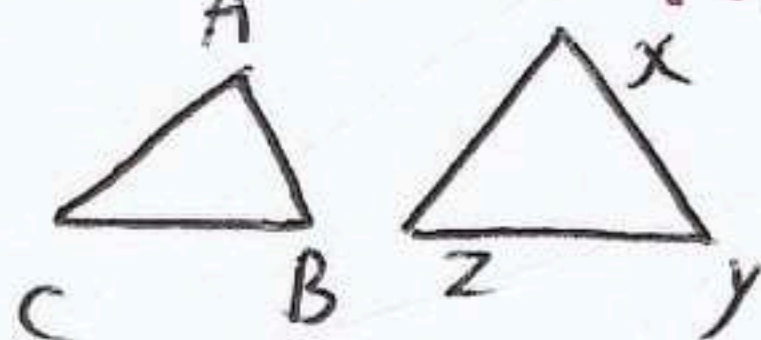


Model 1

1 Complete each of the following:

① The perpendicular bisector of a line segment is called
axis of symmetry.

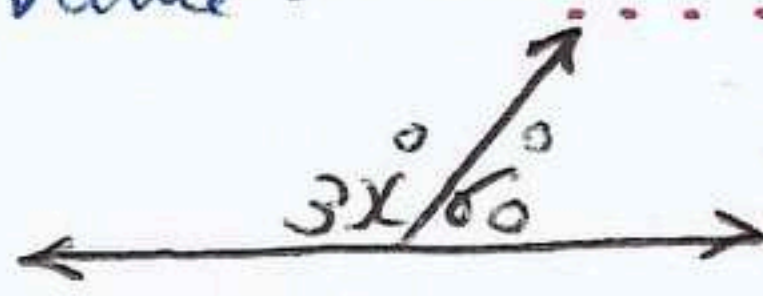
② If $\triangle ABC \equiv \triangle XYZ$, $m(\angle A) + m(\angle B) = 140^\circ$ then $m(\angle Z) = \dots$
 $m(\angle C) = 180 - 140 = 40^\circ$
since $\triangle ABC \equiv \triangle XYZ$ then $m(\angle Z) = m(\angle C) = 40^\circ$



③ If $m(\angle B) = 105^\circ$, then $m(\text{reflex } \angle B) = \dots$

$$m(\text{reflex } \angle B) = 360 - 105^\circ = 255^\circ$$

④ If $\vec{MB} \cap \vec{AC} = \{m\}$, $m(\angle AMB) = 60^\circ$, then the value of $x = \dots$
 $3x = 180^\circ - 60^\circ = 120^\circ$, then $x = \frac{120}{3} = 40^\circ$



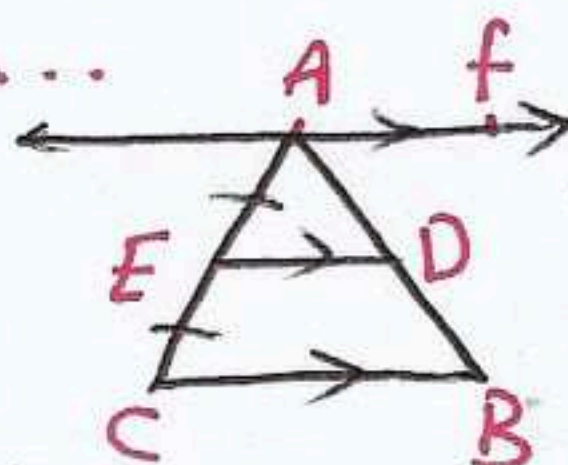
⑤ Two right-angled triangles are congruent if

the hypotenuse and a side of one triangle are congruent to the corresponding parts of the other triangle.

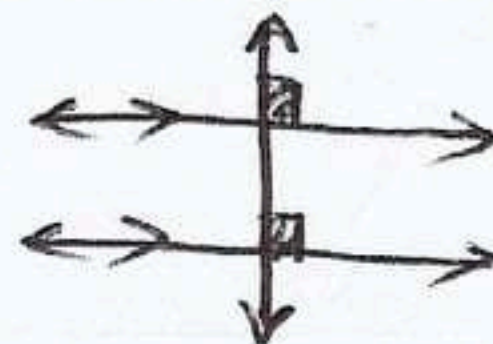
⑥ If $\angle x \equiv \angle y$, $\angle x$ and $\angle y$ are supplementary angles, then $m(\angle x) = \dots$
 $m(\angle x) + m(\angle y) = 180^\circ$ then $m(\angle x) = m(\angle y) = \frac{180}{2} = 90^\circ$

⑦ $\vec{AF} \parallel \vec{DE} \parallel \vec{BC}$, $AE = EC$, then $AD:AB = \dots : \dots$

$$AD = DB \text{ then } AD:AB = 1:2$$



⑧ The two straight lines that are perpendicular to a third one are
Parallel

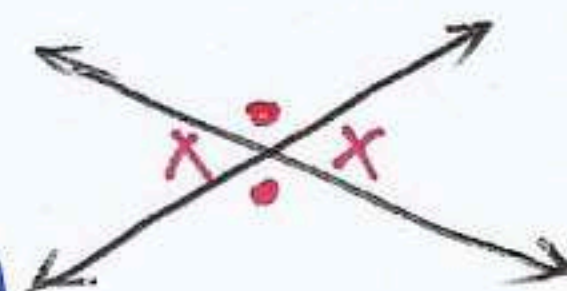


⑨ The measure of each of two equal complementary angles =

$$m(\angle x) + m(\angle x) = 90^\circ \Rightarrow m(\angle x) = \frac{90}{2} = 45^\circ$$

45°

⑩ If two straight lines intersect, then each two angles have the same measure vertically opposite

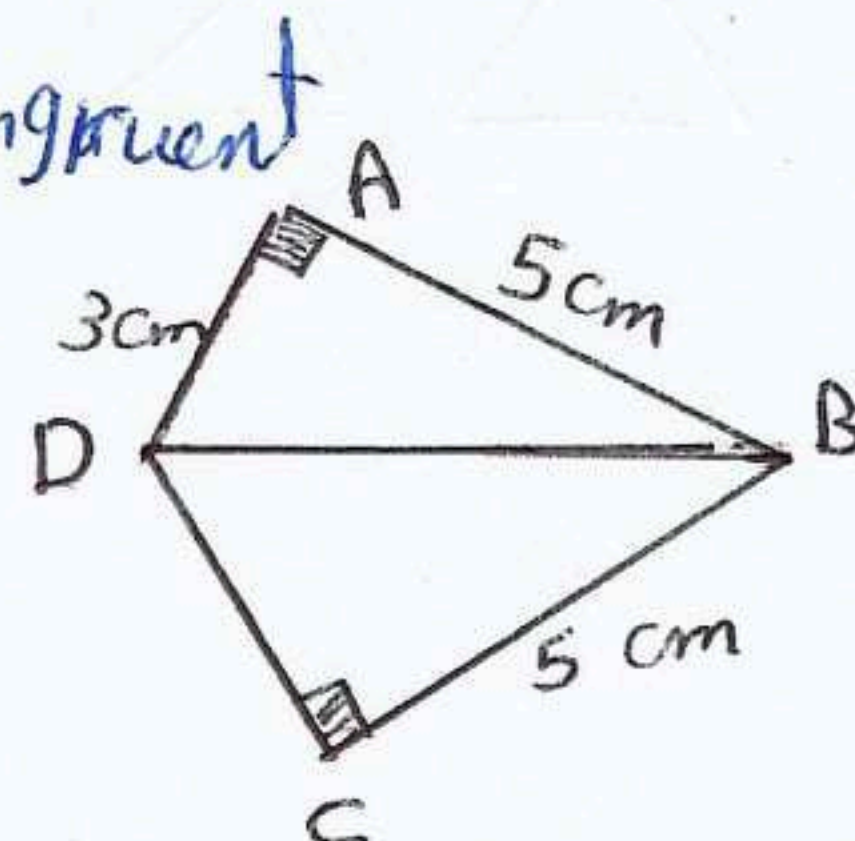


⑪ If $\triangle ABC \equiv \triangle LMN$, then $m(\angle ACB) = m(\angle \dots)$

$$m(\angle ACB) = m(\angle LNM)$$

② In the opposite figure:

mention the conditions for $\triangle ABD$, $\triangle CBD$ to be Congruent
then find the length of \overline{CD}



Solution

In $\triangle ABD$ and $\triangle CBD$

① $m(\angle C) = m(\angle A) = 90^\circ$ R

② \overline{BD} is a common hypotenuse H

$AB = CB$ S

Then $\triangle ABD \equiv \triangle CBD$

Then $CD = AD = 3\text{cm}$

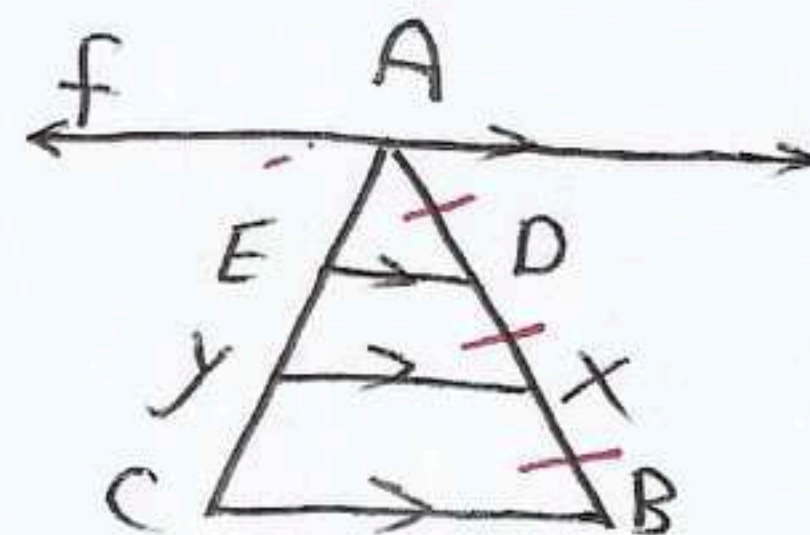
③ in the opposite figure. $AC = 9\text{cm}$

Find the length of \overline{Ay} give the reason

Since $\overrightarrow{Af} \parallel \overrightarrow{DE} \parallel \overrightarrow{xy} \parallel \overrightarrow{BC}$

and $AD = Dx = xB$

Then $AE = Ey = yC = \frac{9}{3} = 3\text{cm}$, then $Ay = 3 + 3 = 6\text{cm}$



Solution

④ In the opposite figure

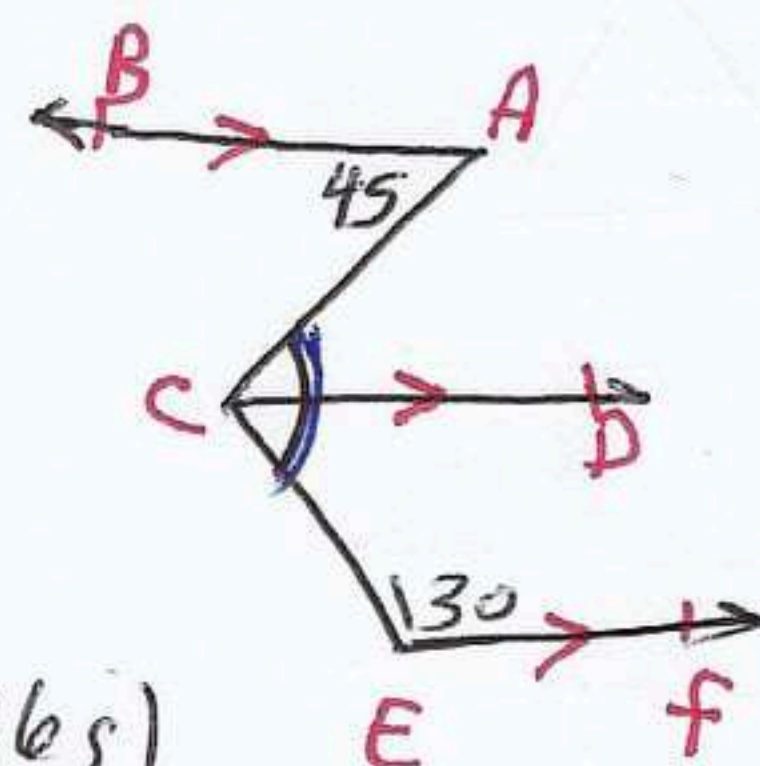
Find $m(\angle ACE)$

Since $\overrightarrow{AB} \parallel \overrightarrow{CD}$

Then $m(\angle A) = m(\angle ACD) = 45^\circ$

Since $\overrightarrow{CD} \parallel \overrightarrow{Ef}$

(alternate angles)



Solution

Then $m(\angle DCE) + m(\angle E) = 180$

$$m(\angle DCE) = 180 - 130 = 50^\circ$$

interior angles

, then $m(\angle ACE) = 45 + 50 = 95^\circ$

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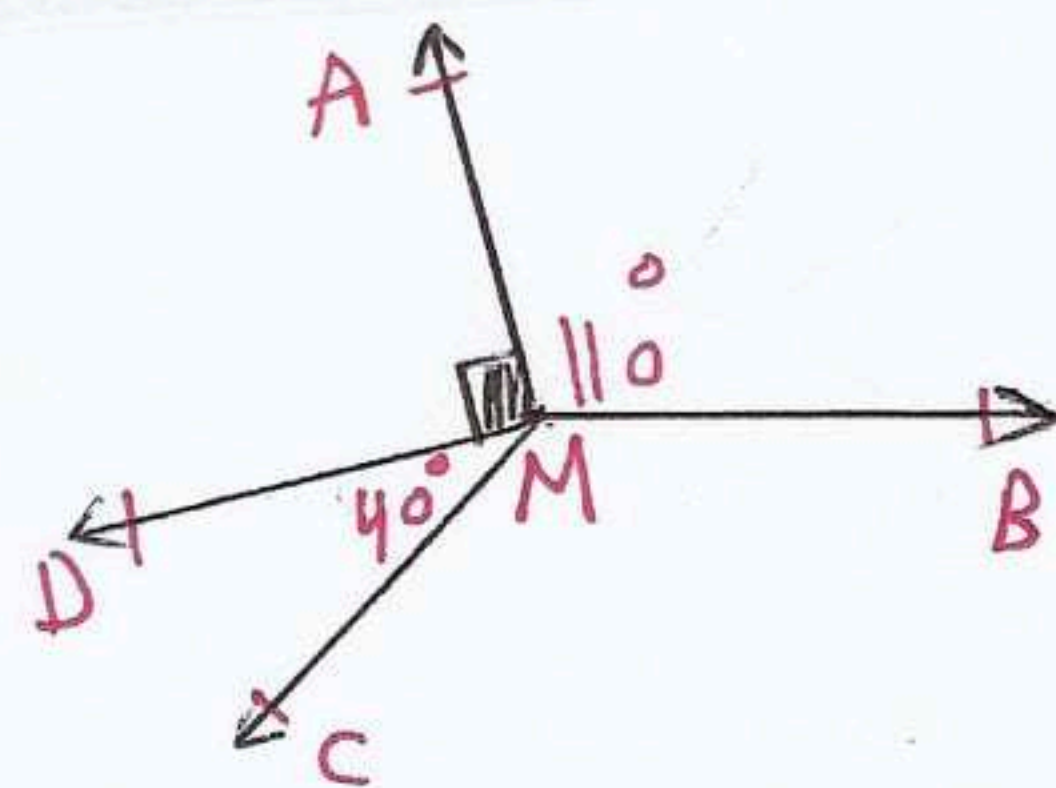
⑥ In the opposite figure

Find with steps $m(\angle BMC)$

Solution

Since sum of measures of accumulative angles at point M is 360°

$$\text{Then } m(\angle BMC) = 360 - (110^\circ + 90^\circ + 40^\circ) = 120^\circ$$



⑤a In the opposite figure

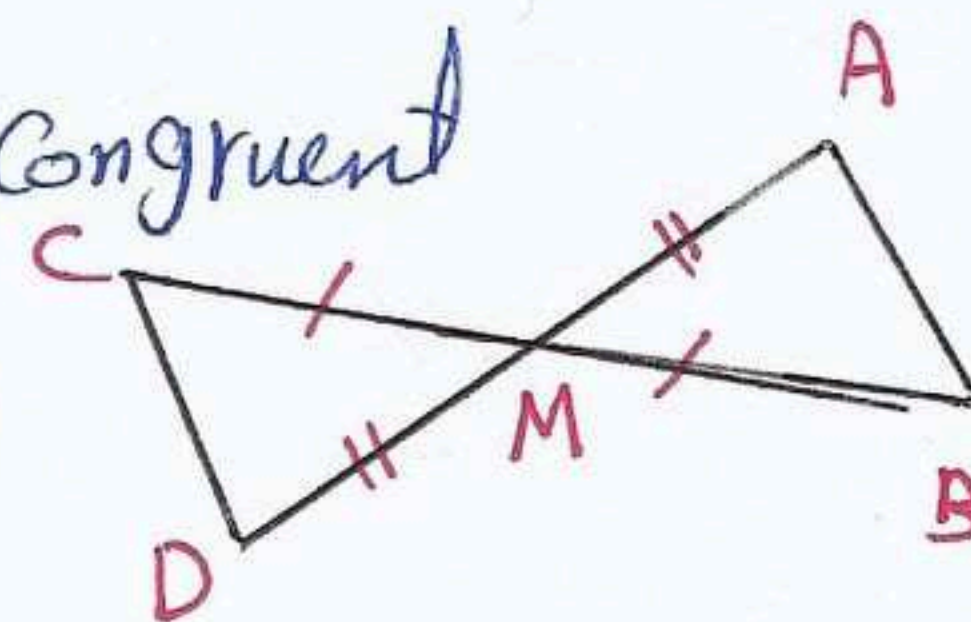
write the conditions for $\triangle AMB$, $\triangle DMC$ to be Congruent

In $\triangle AMB, DMC$

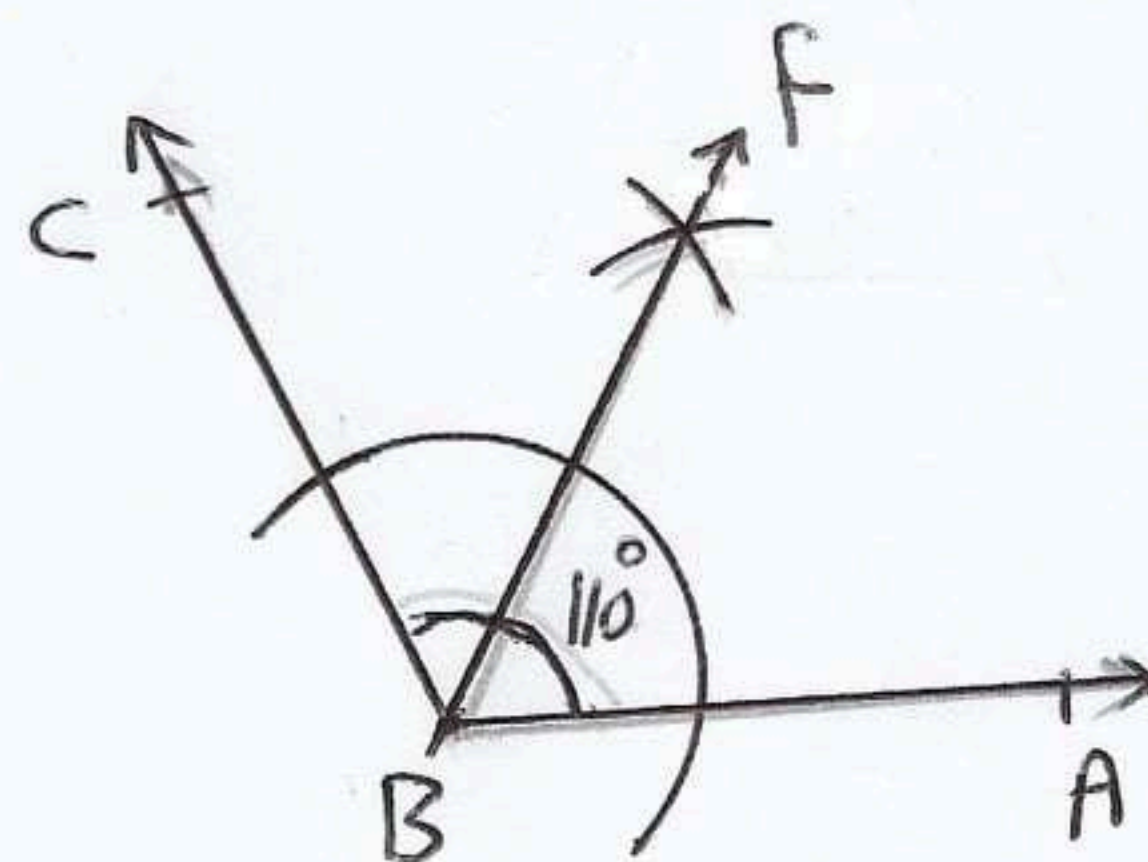
Solution

$$\begin{cases} AM = DM \\ m(\angle AMB) = m(\angle DMC) \quad (\text{V.O.A}) \\ BM = CM \end{cases}$$

Then $\triangle AMB \cong \triangle DMC$



⑥ Using the geometric instruments, draw $\angle ABC$ of measure 110° , then draw \vec{BF} to bisect the angle.



الرسومات غير دقيقة

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① Complete each of the following Model 2

① The sum of the measures of the accumulative angles at a point = 360°

② If a straight line intersects two parallel straight lines, then each two corresponding angles are equal in measure.

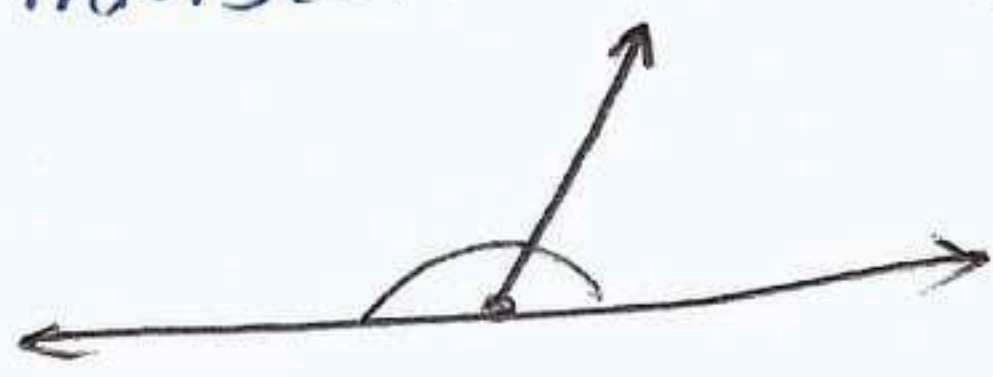
③ If $m(\angle A) = 110^\circ$ then $m(\text{reflex } \angle A) = \dots\dots\dots$

$$360 - 110 = 250^\circ$$

④ Two right angled triangles are congruent if $\dots\dots\dots$

hypotenuse and a side of one triangle are congruent to the corresponding parts of the other triangle

⑤ The two adjacent angles formed by the intersection of a straight line and a ray are $\dots\dots\dots$ supplementray



⑥ If $\angle x$ complements $\angle y$ and $\angle x \equiv \angle y$ then $m(\angle x) = \dots\dots\dots$

$$m(\angle x) + m(\angle y) = 90 \quad \& \quad m(\angle x) = m(\angle y) = \frac{90}{2} = 45^\circ$$

⑦ The number of triangle in the figure  equals $\dots\dots\dots 8$

⑧ If the ratio between the measures of two supplementray angles is $5:13$, then the measure of the smaller angles equals $\dots\dots\dots$

1st angle: 2nd angle: sum

5 : 13 : 18

? : : 180

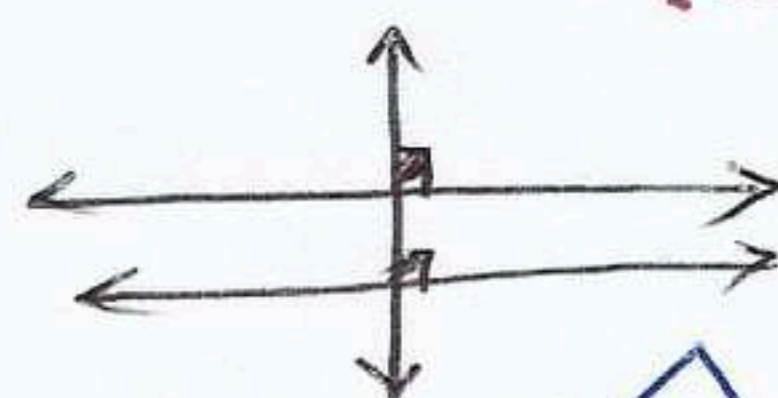
$$\text{supplementray} \Rightarrow 1^{\text{st}} \text{ angle} + 2^{\text{nd}} \text{ angle} = 180^\circ$$

$$\Rightarrow \text{smaller angles} = \frac{180 \times 5}{18} = 50^\circ$$

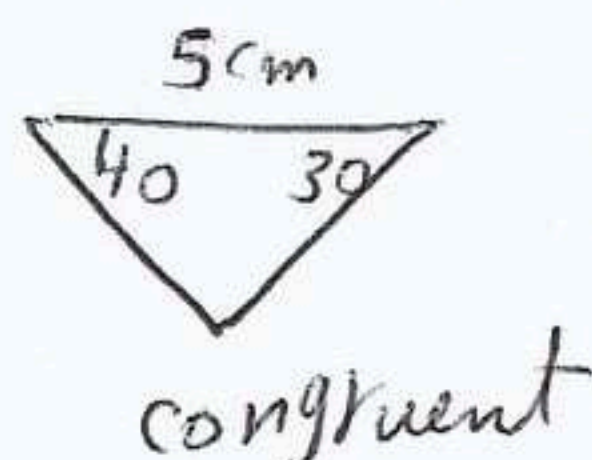
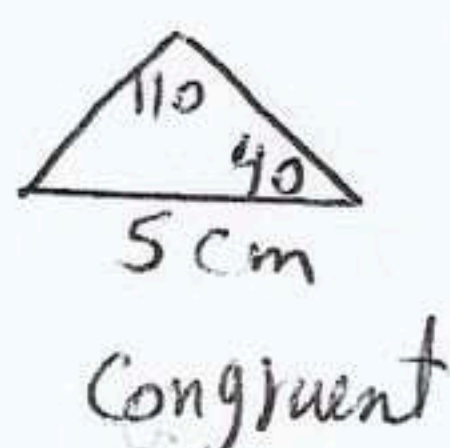
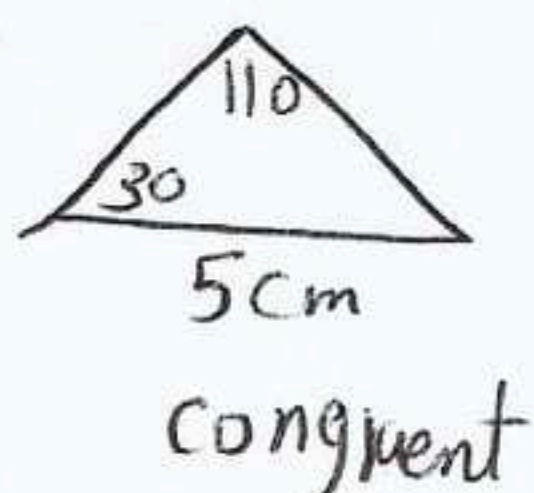
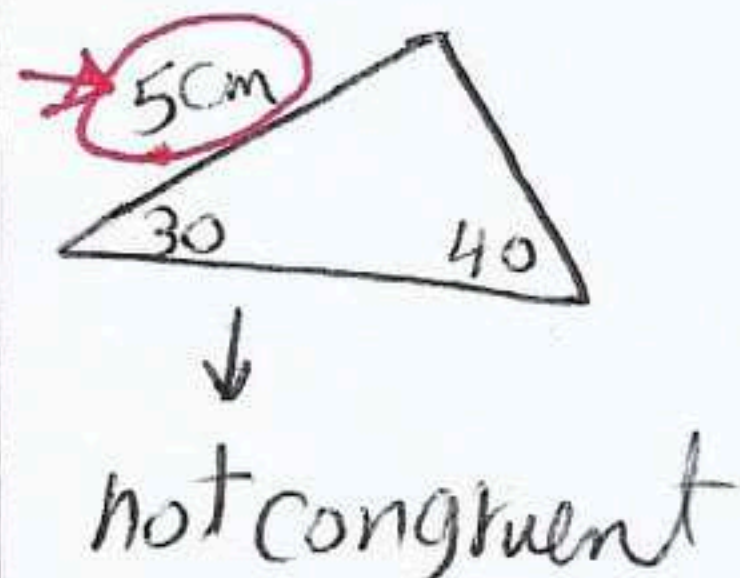
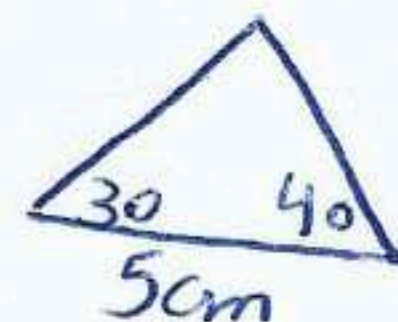
⑨ $\triangle ABC \equiv \triangle xyz$, $m(\angle A) + m(\angle B) = 100$ then $m(\angle z) = \dots\dots\dots$

$$m(\angle z) = m(\angle C) = 180 - 100 = 80^\circ$$

10) The two straight lines that are perpendicular to a third one are
Parallel



11) The figure is not congruent to the opposite figure



3) mention two cases of congruent of two triangles

① two triangles are congruent if two sides and the included angle of one triangle are congruent to the corresponding parts of the other triangle

② two triangles are congruent if each side of one triangle is congruent to the corresponding side of the other triangle S-S-S

6) In the opposite figure

Prove that $\triangle CAD \cong \triangle ABD$ and find $m(\angle ABD)$

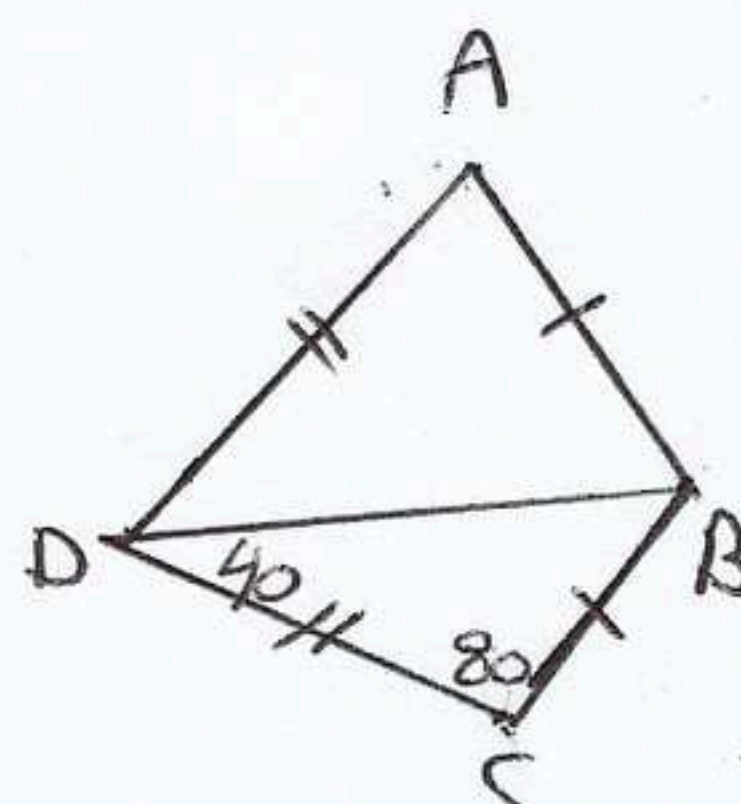
Solution

In $\triangle CAD$ and $\triangle ABD$

$$\begin{cases} AB = CA & (S) \\ AD = CD & (S) \\ DB \text{ is a common side} & (S) \end{cases}$$

Then $\triangle CAD \cong \triangle ABD$

$$\text{Then } m(\angle ABD) = m(\angle CBD) = 180 - (40 + 80) = 60^\circ$$



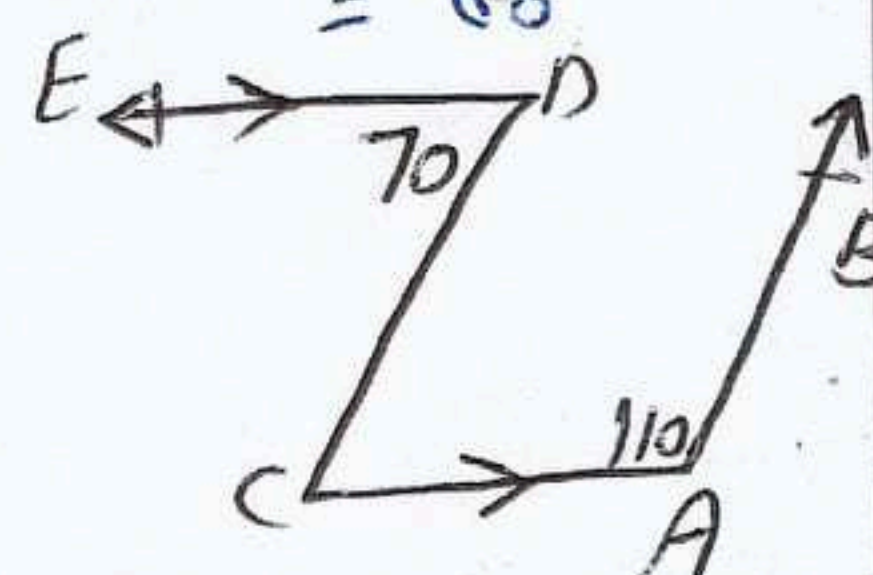
4) In the opposite figure find $m(\angle C)$
is $\overrightarrow{AB} \parallel \overrightarrow{CD}$

Solution

Since $\overrightarrow{DE} \parallel \overrightarrow{CA}$ and \overrightarrow{DC} transversal to them

Then $m(\angle C) = m(\angle D) = 70$ (Alternate angles)

Since $m(\angle C) + m(\angle A) = 70 + 110 = 180$ two interior angles
Then $\overrightarrow{AB} \parallel \overrightarrow{CD}$



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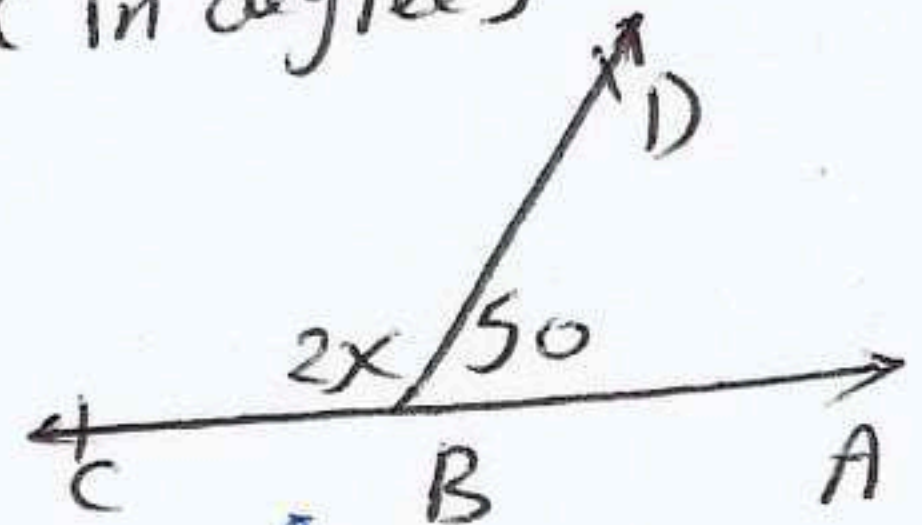
⑥ using the geometric instruments draw $\angle ABC$ where $m(\angle B) = 8^\circ$ then draw \overrightarrow{BD} to bisect it (Don't remove the arcs try by yourself).

5a) In the opposite figure find the value of x in degrees

Solution

$$m(\angle ABD) + m(\angle DBC) = 180$$

$$\text{Then } 2x = 180 - 50 = 130 \quad \text{then } x = \frac{130}{2} = 65^\circ$$



b) In the opposite figure find $m(\angle A)$ in degrees.

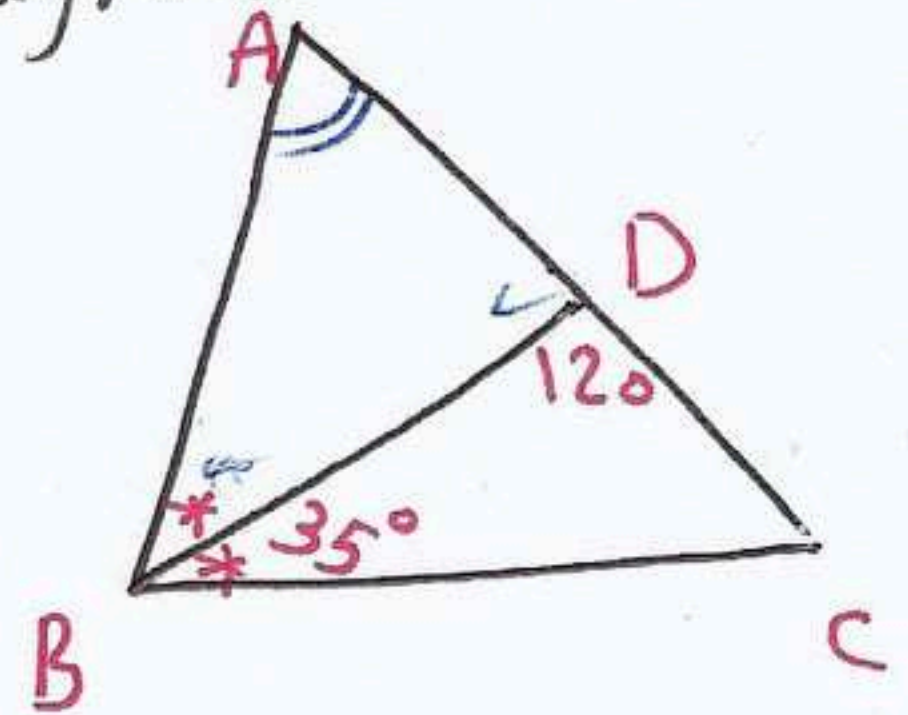
Solution

Since \overrightarrow{BD} bisects $\angle ABC$

$$\text{Then } m(\angle ABD) = 35^\circ$$

$$m(\angle ADB) = 180^\circ - 120^\circ = 60^\circ$$

$$\text{In } \triangle ABD \quad m(\angle A) = 180 - (35^\circ + 60^\circ) = 85^\circ$$



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